Monetary policy and long-term interest rates*

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6 July 2015

Abstract

Long term interest rates can provide valuable information on expectations of future policy rates and inflation rates. The empirical behaviour of long-term rates, however, is a puzzle for linearised new Keynesian models. We show that allowing for regime shifts in the conditional variance of productivity shocks goes a long way in solving this puzzle. In an estimated, nonlinear version of the model, switches between "normal" and "high" levels of volatility are found to be countercyclical and to play an important role in driving cyclical fluctuations in long-term yields. At the onset of recessions, volatility tends to increase to high levels: this leads to both a persistent increase in precautionary saving, which drives down real and nominal yields, and an increase in risk premia. During the recovery, these dynamics are reversed: volatility returns to normal, low levels, nominal yields increase and risk premia become lower. These model implications for both nominal yields and risk premia are consistent with the empirical evidence. Over period of constant volatility, real rates are more stable and long-term yields reflect long-term inflation expectations. Our results suggest that 10year inflation expectations are less firmly anchored than one would conclude, based on survey data.

JEL classification:

Keywords: monetary policy rules, uncertainty shocks, term structure of interest rates, regime switches, Bayesian estimation.

^{*}We thank for comments Haroon Mumtaz and Tao Zha. The opinions expressed are personal and should not be attributed to the Board of Governors of the Federal Reserve System, or to the European Central Bank.

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1 Introduction

Standard macro-models used for monetary policy analysis imply that expected policy rates over the distant future, e.g. 5 to 10-year ahead, should be close to their long run mean. Long-term yields should be approximately constant over time.

This model-implication is in stark contrast to the historically observed, "excess volatility" of yields. Long-term interest rates have undergone both large secular movements—over the 1970s and 1980s—and systematic, cyclical variations—falling in recessions and increasing during expansions. Since "managing expectations" of future interest rates is at the core of the monetary policy transmission mechanism in standard macro-models, their inability to account for the observed movements in long-term yields raises questions as to their suitability for policy analysis (see Atkeson and Kehoe, 2008).

In this paper we show that an estimated, nonlinear version of the standard macromodel can be reconciled with the observed dynamics of yields, provided one allows for
heteroskedasticity in the conditional variance of structural shocks. We refer to unexpected
changes in conditional variances as uncertainty shocks, because these shocks affect expectations of future revisions in consumption growth. We show that uncertainty shocks help
reproduce the observed volatility of yields through two channels: they affect households'
demand for precautionary saving, thus generating variations in equilibrium real interest
rates; and they lead to sizable changes in risk premia.

Since the mid-1960s, U.S. three month forward rates in ten years, a noisy measure of expected future short-term interest rates, have moved between a maximum of almost 15 and a minimum of 4.5 percent—a range of variation roughly comparable to that of the 3-month rate, which peaked at almost 18 percent in 1981 and fell to zero at the end of 2008 (see Figure 1a). Over the same period, long-term yields have moved together with short-term rates, increasing during economic expansions, when policy rates rise, and falling at the beginning of recessions, when short rates decrease. The "term spread" between long and short rates has therefore oscillated less than it would have under roughly constant long-term rates (see Figure 1b).

These two facts are inconsistent with the standard, linearized new Keynesian model where the central bank follows a Taylor rule. In that model, the central bank brings inflation steadily back to target after any exogenous shock. At any point in time, expected inflation far into the future, e.g. 5 to 10-year ahead, should always be "anchored", i.e.

close to target. Expected policy rates 5 to 10-year ahead are approximately constant around their long run mean and long-term yields vary little compared to short-term rates (see e.g. Gürkaynak, Sack and Swanson, 2005).

Of course, the linearized new Keynesian model describes risk-adjusted yields, i.e. yields net of risk premia, while actual yields also reflect changes in risk premia. It is however unlikely that variations in risk premia could in themselves account for the discrepancy between the linearized new Keynesian model and the data (see also the discussion in Cochrane, 2008). In other words, risk-adjusted yields are unlikely to behave more consistently with the implications of the new Keynesian model. For this to be the case, a fall in the risk premium at the beginning of recessions would be necessary to account for the observed reduction in long-term yields. Net of the risk premium, long term yields would then roughly remain constant, as predicted by the model. However, one of the few robust stylized facts emerging from the finance literature is that risk premia are countercyclical (see e.g. Fama and French, 1989, or Cochrane and Piazzesi, 2005). They increase, rather than fall, during recessions. The opposite movement can be observed during cyclical expansion. Risk-adjusted long-term yields are therefore likely to be even more variable than observed yields—thus even more inconsistent with the linearized new Keynesian model.

(a) Current and forward 3m rates

(b) Term spread and 3m rate

Figure 1: Yields and forward rates

Note: zero coupon rates. The term spread denotes the difference between the the 3m rate and the 10y yield. Source: Board data.

If the observed cyclical variation in yields is largely due to changing risk premia, is it caused by monetary policy actions? Which transmission channels produce cyclical variations in risk-adjusted long-term rates and what do they imply for expectations of the future path of monetary policy rates over the business cycle? If long term yields net of risk premia are not constant, are long-term inflation expectations implicit in bond yields also highly variable, i.e. not "anchored"?

In this paper, we provide an answer to these questions through an explicit, general equilibrium model of macroeconomic and yields dynamics. We estimate the model on postwar U.S. data, including data on long term interest rates, and analyze its implications for the monetary transmission mechanism.

We demonstrate that, provided the model is not linearized but solved up to a second order approximation, a single model feature helps account for the "excess volatility" in risk-adjusted long-term interest rates and, at the same time, produces countercyclicality in risk premia. That feature is heteroskedasticity, in the form of regime switching, in the conditional variance of structural shocks.

On the one hand, heteroskedasticity can account for large and persistent changes in long term yields. Specifically, increases in uncertainty over future realizations of technology boost households' demand for precautionary saving. To clear the savings market, current real rates tend to fall. Expected future real rates also fall, because the high-variance regime is estimated to be quite persistent. For roughly constant, long-term inflation expectations, this mechanism also leads to a fall in expected future *nominal* interest rates at current and future horizons. The opposite happens in case of reductions in the conditional variance of technology shocks.

Our empirical estimates suggest that technology uncertainty shocks tend to be countercyclical: they increase during recessions and fall again over economic expansions. This mechanism therefore explains the fall in long-term expected yields during phases of expansionary monetary policy and their increase when monetary policy is tightened.

On the other hand, heteroskedasticity can account for the observed time variation in risk premia. An increase in the variance of technology shocks increases uncertainty over future consumption growth. With non-expected utility preferences as in Epstein and Zin (1989) and Weil (1990), higher uncertainty leads to a higher covariance between bond prices and the economy's stochastic discount factor, and thus higher risk premia. Given the countercyclical nature of technological uncertainty shocks, and consistently with the results in the finance literature, variations in risk premia are also countercyclical.

From an empirical perspective, our simple model specification goes a long way in fitting

both macroeconomic and yields data. The model captures reasonably well the dynamic cross-correlations between all variables. The standard deviations of measurement errors on longer-term yields are about 20 basis points and the model can account for the yields dynamics documented in Figure 1. The model also fits well dimensions of the data which were not directly used in estimation, such as forward rates at various horizons.

Our estimation results shed light on the three questions motivating our analysis.

They suggest that changes in risk premia are not *caused* by monetary policy actions. Specifically, changes in the conditional variance of monetary policy shocks have negligible effects on risk premia. Nevertheless, monetary policy does respond to exogenous, business cycle fluctuations in (technological) risk and, in so doing, it shapes the evolution of inflation, output and interest rates.

The idea of monetary policy reacting systematically to variations in risk may at first sound surprising. It is however less striking when one realizes that increases in risk, i.e. uncertainty shocks, lead to an increase in the demand for precautionary saving during recessions thus to a fall in the demand for consumption goods. Due to monopolistic competition, output is demand determined. The lower demand for consumption generates a persistent fall in output and puts downward pressure on prices. A few years after the beginning of the economic recovery, "confidence" returns and uncertainty over future realizations of technology switches back to normal, lower levels. With lower levels of uncertainty, the demand for precautionary saving falls. Risk-adjusted nominal and real yields return to normal, higher levels.

From this perspective, the monetary policy reaction to uncertainty shocks is in line with standard intuition and fully consistent with a standard Taylor rule. The less conventional feature of the monetary policy reaction to technological uncertainty shocks is that the standard Taylor rule does not internalize the persistent fall in equilibrium real interest rates. Even if policy rates fall in response to the negative inflation pressure, real rates remain too high to discourage the increase in precautionary saving and the policy stance remains relatively tight. Inflation returns towards the target, but output remains below steady state for a prolonged period of time. As a result, policy rates also remain persistently low and risk-adjusted nominal (and real) yields fall.

All in all, cyclical variations in expected future real interest rates and in risk premia, both induced by uncertainty shocks, play an important role in driving long-term yields. For example, when the beginning of the monetary policy tightening phase coincides the typical fall in technological uncertainty during the recovery, as in 2004, risk premia fall in the face of expectations of increasing future policy rates. This explains why observed long-term yields remained unchanged over that period—an apparent "conundrum", compared to previous cyclical experiences. If, in contrast, technological uncertainty remains unchanged when the monetary policy tightening phase begins, as in 1994, the response of long-term rates conforms to the (weak) expectations hypothesis. For unchanged risk premia, an increase in yields is associated with an increase in long-term inflation expectations—an "inflation scare".

Once the real interest rates and risk premia components have been isolated, the remaining changes in long-term yields reflect movements in long-term inflation expectations. Our model contributes to account for the secular change in yields over the 1970s and 1980s through a standard, "level" technology shock. To affect long-term nominal yields, this shock needs to produce extremely persistent effects on inflation. According to our estimates this is the case due to two features: an extremely high persistence of the shock process; and a significantly higher degree of inertia in the monetary policy rule than typically estimated. These features of our estimates reflect our explicit inclusion of long-term yields in the econometrician's information set.

We can compare 10-year inflation expectations derived from our model to those available from the Federal Reserve Bank of Philadelphia's quarterly Survey of Professional Forecasters. Over the 1980s, the two measures are quite similar, showing a progressive fall in inflation expectations from the 1980 peaks. Over the 2000s, however, yields dynamics suggest a much less tight anchoring of inflation expectations compared to surveys. The latter fall steadily towards 2.5 percent over the 1990s and remain constant at that level thereafter. In contrast, model-implied measures, fall faster than surveys during the policy tightening phase which started in spring 1988, then increase sharply during the "inflation scare" of 1993. They hover closely around 2.5 percent at the turn of the millennium, but fall sharply to levels close to 1 during the recession of the early 2000s and even below 1 ahead of the Great recession. In sum, bond prices suggest that 10-year inflation expectations are less firmly anchored than one would conclude, based on survey data.

¹The term conundrum was famously used first by Greenspan (2005).

²Goodfriend (1993) defines an inflation scare as a significant increase in long term nominal interest rates in the absence of an increase in policy rates.

Our paper is related to a recent literature exploring the term structure implications of macro-models. Many of these papers are theoretical and look at the asset pricing implications of macro models-see e.g. Piazzesi and Schneider (2006), Rudebusch and Swanson (2012), Swanson (2014). De Graeve, Emiris and Wouters (2007) estimate a standard DSGE model using both macroeconomic and term structure data, but rely on the loglinearized version of that model and must therefore introduce additional parameters to allow for constant risk-premia. Christoffel, Jaccard and Kilponen (2011) also estimate the linearized version of a new Keynesian model, but draw bond pricing implications using a higher order approximation. Bekaert, Cho and Moreno (2010) and Campbell, Pflueger and Viceira (2013) follow an intermediate route and study asset prices in a linearized New Keynesian model assuming a stochastic discount factor that is related to the new Keynesian model's equations in a reduced-form manner. The papers more similar to ours in this literature are Doh (2011, 2012), van Binsbergen et al. (2012) and Andreasen (2012), which estimate nonlinear models with macroeconomic and term structure data. In contrast to all these papers, we allow for regime switches in the variance of shocks and argue that this is an essential model feature to fit bonds and macro data. Moreover, van Binsbergen et al. (2012) rely on a model with flexible prices, where inflation is modelled as an exogenous process. This prevents an analysis of the relationship between bond yields and monetary policy. Doh (2011) focuses on a comparison of the model's performance under flexible or sticky prices. In Doh (2012) a large explanatory role of yields dynamics is played by a drifting inflation target, which needs to be filtered by private agents. We offer an alternative explanation based on a constant target. Finally, Andreasen (2012) relies on a more complete, medium-scale DSGE model, but focuses on a shorter sample of UK data.

Our paper is also related to the literature documenting time variation in macroeconomic volatility in a reduced form setting, including e.g. McDonnell and Perez-Quiros (2000), Sims and Zha (2006), Primiceri (2005). Justiniano and Primiceri (2008) allow for shifts in the volatility of structural shocks in a linearized, medium-scale DSGE model applied to the U.S. economy. In contrast, we rely on a smaller, but non-linear model, which allows us to explore the effects of changes in volatility on households' demand for precautionary saving. Conditional on our model, including bond price data in the estimation set also provides us with additional information to sharpen the inference on regime change, since changes in regime have implications on the level of yields.

Finally, our paper is related to the literature on uncertainty shocks spawned from Bloom (2009). In Bloom (2009), an increase in uncertainty induces firms to temporarily reduce investment and hiring. In our model, higher uncertainty over future technology shocks induces households to increase their precautionary saving. Consumption demand will tend to fall. Due to monopolistic competition and sticky prices, this will bring down output and inflation. Uncertainty shocks therefore act like demand shocks. This is consistent with the results in Basu and Bundick (2012), which relies on a more comprehensive, calibrated model of the U.S. economy and analyses uncertainty shocks in both technology and preferences. Bianchi, Ilut and Schneider (2014) put forward a model with ambiguity averse investors, where regime shifts generate large low frequency movements in asset prices.

The rest of the paper is organized as follows. Section 2 describes the model, focusing on its distinguishing features: the distribution of the shocks and the utility function, which is of the class proposed by Epstein and Zin (1989) and Weil (1990), but extended to allow for habit persistence in consumption. The methods that we adopt to solve and estimate the model are described next, in section 3. Such methods are non-standard, because we need to solve the model to a second order approximation in order to capture precautionary savings effects. We demonstrate that the reduced form of the model is quadratic in the state variables with continuous support and includes regime-switching intercepts, as well as variances. We then estimate the non-linear reduced form using Bayesian methods. Section 4 described the estimation results and presents a few goodness-of-fit measures. The implications of our estimates for the relationship between monetary policy and risk premia and for the transmission of monetary policy to long-term rates are discussed in Section 5. Section 6 concludes.

2 The model

We start from a simple version of the new-Keynesian model that has been shown to account relatively well for the dynamics of key nominal and real macroeconomic variables—see e.g. Smets and Wouters (2007). We thus assume nominal price rigidities, external habit persistence, inflation indexation, and a monetary policy rule with partial adjustment—or

"interest rate smoothing". Since our interest is on the model's implications for longterm interest rates, we simplify it by abstracting from capital accumulation and real wage rigidities. Our results suggest that even our simple model can go a long way in explaining the data of interest to us.

Compared to the new Keynesian benchmark, we introduce two key modifications.

The first is to allow for stochastic regime switching in the variance of structural shocks. The evidence of time variation in the variance of macroeconomic shocks is well-established—see e.g. Justiniano and Primiceri (2008), McDonnell and Perez-Quiros (2000), Primiceri (2005) and Sims and Zha (2006). The novelty in our paper is to explore the implications of time varying variances on bond prices.

Our second modification, which is already common in the consumption-based asset pricing literature, is to adopt the non-expected utility specification for preferences proposed by Epstein and Zin (1989) and Weil (1990). Here we extend this specification to a general equilibrium model in which we also allow for habit persistence in consumption and labour-leisure choice.

2.1 Structural shocks

A key distinguishing feature of our model are changes in the demand for precautionary saving induced by variations in the conditional variance of the structural shocks. We therefore start the description of our model from the distribution of structural shocks.

In macroeconomic applications, exogenous shocks are almost always assumed to be (log-)normal, partly because models are typically log-linearized and researchers are mainly interested in characterizing conditional means. However, Hamilton (2008) argues that a correct modelling of conditional variances is always necessary, for example because inference on conditional means can be inappropriately influenced by outliers and high-variance episodes. The need for an appropriate treatment of heteroskedasticity becomes even more compelling when models are solved nonlinearly, because conditional variances have a direct impact on conditional means.

In this paper, we assume that variances are subject to stochastic regime switches. We will allow for shocks to the level and growth rates of technology, government spending shocks, mark-up shocks and monetary policy shocks. The conditional variance of any of these shocks could in principle be subject to regime switching, but in this paper we adopt a

parsimonious specification such that only (level) productivity and monetary policy shocks have regime switching variances. This assumption is loosely inspired by the finding of the literature on the "Great moderation" (see e.g. McDonnell and Perez-Quiros, 2000) that has emphasized the reduction in the volatility of real aggregate variables starting in the second half of the 1980s. We conjecture that this phenomenon could be captured by a reduction in the volatility of technology shocks in our structural setting. The heteroskedasticity in policy shocks aims to capture the large increase in interest rate volatility in the early 1980s, the time of the so-called "monetarist experiment" of the Federal Reserve.

More specifically, we will assume that the technology shock z_t , the government spending shock G_t and the monetary policy shocks η_t have standard deviations that can independently switch between a high and a low regime.³ Denoting the low variance regime by 1 and the high variance regime by 0, we write

$$\sigma_{z,s_{z,t}} = \sigma_{z,0}s_{z,t} + \sigma_{z,1} (1 - s_{z,t})$$

$$\sigma_{G,s_{G,t}} = \sigma_{G,0}s_{G,t} + \sigma_{G,1} (1 - s_{G,t})$$

$$\sigma_{\eta,s_{\eta,t}} = \sigma_{\eta,0}s_{\eta,t} + \sigma_{\eta,1} (1 - s_{\eta,t})$$

where the variables $s_{z,t}$, $s_{G,t}$ and $s_{\eta,t}$ can assume the discrete values 0 and 1. For each variable $s_{j,t}$ $(j=z,G,\eta)$, the probabilities of remaining in states 0 and 1 are constant and equal to $p_{j,0}$ and $p_{j,1}$, while the probabilities of switching to the other state will be $1-p_{j,0}$ and $1-p_{j,1}$, respectively.

2.2 Households

We assume that each household i provides $N\left(i\right)$ hours of differentiated labor services to firms in exchange for a labour income $w_{t}\left(i\right)N_{t}\left(i\right)$. Each household owns an equal share of all firms j and receives profits $\int_{0}^{1}\Psi_{t}\left(j\right)\mathrm{d}j$. As in Erceg, Henderson and Levin (2000), an employment agency combines households' labor hours in the same proportions as firms would choose. The agency's demand for each household's labour is therefore equal to the sum of firms' demands. The labor index L_{t} has the Dixit-Stiglitz form $L_{t}=\left[\int_{0}^{1}N_{t}\left(i\right)^{\frac{\theta_{w,t}-1}{\theta_{w,t}}}\mathrm{d}i\right]^{\frac{\theta_{w,t}}{\theta_{w,t}-1}}$, where $\theta_{w,t}>1$ is subject to exogenous shocks. At time t, the employment agency minimizes the cost of producing a given amount of the aggregate labor

³We have also estimated versions of the model allowing for regime-switching in the variance of mark-up and technology growth shocks. These dimensions of regime switching receive little support from the data.

index, taking each household's wage rate $w_t(i)$ as given and then sells units of the labor index to the production sector at the aggregate wage index $w_t = \left[\int_0^1 w(i)^{1-\theta_{w,t}} di\right]^{\frac{1}{1-\theta_{w,t}}}$. The employment agency's demand for the labor hours of household i is given by

$$N_t(i) = L_t \left(\frac{w_t(i)}{w_t}\right)^{-\theta_{w,t}} \tag{1}$$

Each household i maximizes its intertemporal utility with respect to consumption, the wage rate and holdings of contingent claims, subject to the demand for its labour (1) and the budget constraint

$$P_t C_t(i) + \mathbb{E}_t Q_{t,t+1} W_{t+1}(i) \le W_t(i) + w_t(i) N_t(i) + \int_0^1 \Psi_t(j) \, \mathrm{d}j$$
 (2)

where C_t is a consumption index satisfying

$$C_{t} = \left(\int_{0}^{1} C_{t}(z)^{\frac{\theta-1}{\theta}} dz\right)^{\frac{\theta}{\theta-1}}$$
(3)

In the budget constraint, W_t denotes the beginning-of-period value of a complete portfolio of state contingent assets, $Q_{t,t+1}$ is their price and $\Psi_t(j)$ are the profits received from investment in firm j. The price level P_t is defined as the minimal cost of buying one unit of C_t , hence equal to

$$P_t = \left(\int_0^1 p(z)^{1-\theta} dz\right)^{\frac{1}{1-\theta}}.$$
 (4)

Equation (2) states that each household can only consume or hold assets for amounts that must be less than or equal to its salary, the profits received from holding equity in all the existing firms and the revenues from holding a portfolio of state-contingent assets.

Households' preferences are described by the Kreps and Porteus (1978) specification proposed by Epstein and Zin (1989). In that paper, utility is defined recursively through the aggregator U such that

$$U\left[C_{t}, \left(E_{t}V_{t+1}^{1-\gamma}\right)\right] = \left\{ (1-\beta) C_{t}^{1-\psi} + \beta \left(E_{t}V_{t+1}^{1-\gamma}\right)^{\frac{1-\psi}{1-\gamma}} \right\}^{\frac{1}{1-\psi}}, \quad \psi, \gamma \neq 1$$
 (5)

where β , ψ and γ are positive constants. Using a specification equivalent to that in equation (5), Weil (1990) shows that β is, under certainty, the subjective discount factor, but time preference is in general endogenous under uncertainty. The parameter γ is the relative risk aversion coefficient for timeless gambles. The parameter $1/\psi$ measures the elasticity of intertemporal substitution for deterministic consumption paths.

The distinguishing feature of the Epstein-Zin-Weil preferences, compared to the standard expected utility specification, is that the coefficient of relative risk aversion can differ from the reciprocal of the intertemporal elasticity of substitution. In addition, Kreps and Porteus (1978) show that, again contrary to the expected utility specification, the timing of uncertainty is relevant in their class of preferences. The specification in equation (5) displays preferences for an early resolution of uncertainty when the aggregator is convex in its second argument, i.e. when $\gamma > \psi$. Any source of risk will be reflected in asset prices not only if it makes consumption more volatile, but also if it affects the temporal distribution of consumption volatility.

We generalize the utility function in equation (5) by allowing for habit formation and a labour-leisure choice, as in standard, general equilibrium macro-models. The generalization to allow for the labour-leisure choice has already been used, for example, in Rudebusch and Swanson (2012). We additionally allow for habit formation because it has been shown to be important to match the dynamic behavior of aggregate consumption—see e.g. Fuhrer (2000).

As a result, time-t utility will not only depend on consumption C_t but it will be a more general function of consumption and leisure

$$U_{t}(j) = u \{C_{t}(j) - h\Xi_{t}C_{t-1}, 1 - N_{t}(j)\}$$

where leisure is written as $1 - N_t$ because total hours are normalized to 1, the h parameter represents the force of external habits and Ξ_t is the rate of growth of technology.⁴

With our more general preferences specification, γ is no-longer related one-to-one to risk aversion. Swanson (2012) discusses the appropriate measures of risk aversion in a dynamic setting with consumption and leisure entering the utility function. However, $1/\psi$ continues to measure the elasticity of intertemporal substitution of consumption.⁵

The appendix shows that the first order conditions include

$$\frac{u_{N,t}}{u_{c,t}} = \mu_{w,t} \frac{w_t(j)}{P_t}$$

⁴Guariglia and Rossi (2002) also use expected utility preferences combined with habit formation to study precautionary savings in UK consumption. Koskievic (1999) studies an intertemporal consumption-leisure model with non-expected utility.

⁵See the appendix.

and

$$Q_{t,t+1} = \beta \left[E_t \left(\frac{J_{t+1}}{J_t} \right)^{1-\gamma} \right]^{\frac{\gamma-\psi}{1-\gamma}} \left(\frac{J_{t+1}}{J_t} \right)^{-(\gamma-\psi)} \left(\frac{u_{t+1}}{u_t} \right)^{-\psi} \frac{u_{c,t+1}}{u_{c,t}} \frac{1}{\Pi_{t+1}}$$
 (6)

where Π_t is the inflation rate between t and t-1, and the mark-up $\mu_{w,t} \equiv (\theta_{w,t}-1)/\theta_{w,t}$ follows an exogenous autoregressive process

$$\mu_{w,t+1} = \mu_w^{1-\rho_{\mu}} \left(\mu_{w,t}\right)^{\rho_{\mu}} e^{\varepsilon_{t+1}^{\mu}}, \qquad \varepsilon_{t+1}^{\mu} \approx N\left(0, \sigma_{\mu}\right)$$

The gross interest rate, I_t , equals the conditional expectation of the stochastic discount factor, i.e.

$$I_t^{-1} = \mathcal{E}_t Q_{t,t+1} \tag{7}$$

Note that we will focus on a symmetric equilibrium in which nominal wage rates are all allowed to change optimally at each point in time, so that individual nominal wages will equal the average w_t .

Equation (6) highlights how our model nests the standard power utility case, in which $\psi = \gamma$ and the maximum value function J_t disappears from the first order conditions. The same equations also demonstrate that the parameter γ only affects the dynamics of higher order approximations. It is straightforward to see that, to first order, the term $\left[\mathbb{E}_t \left(J_{t+1}/J_t\right)^{1-\gamma}\right]^{(\gamma-\psi)/(1-\gamma)} \left(J_{t+1}/J_t\right)^{-(\gamma-\psi)} \text{ cancels out in the interest rate equation (7)}.$

2.3 Firms

We assume a continuum of monopolistically competitive firms (indexed on the unit interval by j), each of which produces a differentiated good. Demand arises from households' consumption and from government purchases G_t , which is an aggregate of differentiated goods of the same form as households' consumption. It follows that total demand for the output of firm i takes the form $Y_t^D(j) = \left(\frac{P_t(i)}{P_t}\right)^{-\theta} Y_t^D$. Y_t^D is an index of aggregate demand which satisfies $Y_t^D = C_t + G_t$.

Firms have the production function

$$Y_t(i) = A_t L_t^{\alpha}(i)$$

where L_t is the labour index L_t defined above and A_t is a mixture of two shocks $A_t = Z_t B_t$ such that

$$\begin{array}{lll} b_t & = & b_{t-1} + \xi + \varepsilon_t^{\xi}, & & \varepsilon_{t+1}^z \approx N\left(0, \sigma_{\xi}\right) \\ \\ z_t & = & \rho_z z_{t-1} + \varepsilon_t^z, & & \varepsilon_{t+1}^z \approx N\left(0, \sigma_{z, s_{z, t}}\right) \end{array}$$

where ξ is the long run productivity growth rate. This specification allows for both a standard, stationary technology shock and for a stochastic trend, represented by B_t . For the solution and estimation of the model, we will work with de-trended variables.

As in Rotemberg (1982), we assume the firms face quadratic costs in adjusting their prices. This assumption is also adopted, for example, by Schmitt-Grohé and Uribe (2004b). It is known to yield first-order inflation dynamics around a zero inflation steady state equivalent to those arising from the assumption of Calvo pricing.⁶ From our viewpoint, it has the advantage of greater computational simplicity, as it allows us to avoid having to include an additional state variable in the model, i.e. the cross-sectional dispersion of prices across firms.

The specific assumption we adopt is that firm j faces a quadratic cost when changing its prices in period t, compared to period t-1. Consistently with what is typically done in the Calvo literature, we modify the original Rotemberg (1982) formulation for partial indexation of prices to lagged inflation. More specifically, we assume that

$$\frac{\zeta}{2} \left(\frac{P_t^j}{P_{t-1}^j} - (\Pi^*)^{1-\iota} \Pi_{t-1}^{\iota} \right)^2 Y_t$$

where Π^* is the central bank's inflation target. In a symmetric equilibrium, firms' profits maximization problem leads to

$$(\theta - 1) Y_t + \zeta \left(\Pi_t - (\Pi^*)^{1-\iota} \Pi_{t-1}^{\iota} \right) Y_t \Pi_t = \frac{\theta}{\alpha} \frac{w_t}{P_t} \left(\frac{Y_t}{A_t} \right)^{\frac{1}{\alpha}} + \mathbb{E}_t Q_{t,t+1} \zeta \left(\Pi_{t+1} - (\Pi^*)^{1-\iota} \Pi_t^{\iota} \right) Y_{t+1} \Pi_{t+1}$$

2.4 Monetary policy and market clearing

We close the model with the simple Taylor-type policy rule

$$I_{t} = \left(\frac{\Pi^{*}}{\beta}\right)^{1-\rho_{I}} \left(\frac{\Pi_{t}}{\Pi^{*}}\right)^{\psi_{\Pi}} \left(\frac{\widetilde{Y}_{t}}{\widetilde{Y}}\right)^{\psi_{Y}} I_{t-1}^{\rho_{I}} e^{\eta_{t+1}}$$

$$(8)$$

where $\widetilde{Y}_t \equiv Y_t/B_t$ is detrended aggregate output, \widetilde{Y} its steady state level, Π^* is the constant inflation target and η_{t+1} is a policy shock such that

$$\eta_{t+1} = e^{\varepsilon_{t+1}^{\eta}}, \qquad \varepsilon_{t+1}^{\eta} \approx N\left(0, \sigma_{\eta, s_{\eta, t}}\right).$$

⁶The equivalence does not hold exactly around a positive inflation steady state – see Ascari and Rossi (2010). Moreover two pricing models have in general different welfare implications – see Lombardo and Vestin (2008).

Market clearing in the goods market requires

$$Y_t = C_t + G_t + \frac{\zeta}{2} \left(\Pi_t - (\Pi^*)^{1-\iota} \Pi_{t-1}^{\iota} \right)^2 Y_t$$

where government spending is an exogenous stochastic process which we specify in deviation from the stochastic growth trend B_t , so that

$$\frac{G_t}{B_t} = \left(\frac{gY}{B}\right)^{1-\rho_g} \left(\frac{G_{t-1}}{B_{t-1}}\right)^{\rho_g} e^{\varepsilon_t^g} \qquad \varepsilon_{t+1}^G \approx N\left(0, \sigma_{G, s_{G, t}}\right)$$

where the long run level g is specified in percent of output, so that $g \equiv G/Y$.

In the labour market, labour demand will have to equal labour supply. In addition, the total demand for hours worked in the economy must equal the sum of the hours worked by all individuals. Taking into account that at any point in time the nominal wage rate is identical across all labor markets because all wages are allowed to change optimally, individual wages will equal the average w_t . As a result, all households will chose to supply the same amount of labour and labour market equilibrium will require that

$$L_t = \left(\frac{Y_t}{A_t}\right)^{\frac{1}{\alpha}}$$

3 Solution and estimation methods

3.1 Solution

To solve the model, we first approximate the system around a deterministic steady state in which all real variables are detrended by the technological level B_t . For example, detrended output is $\widetilde{Y}_t \equiv Y_t/B_t$. In the solution, we expand variables around their natural logarithms, which are denoted by lower-case letters.

We collect all detrended, predetermined variables (including both lagged endogenous predetermined variables and exogenous states with continuous support) in a vector \mathbf{x}_t and all the non-predetermined variables in a vector \mathbf{y}_t (note that \mathbf{y}_t is different from output y_t).

The macroeconomic system can thus be written in compact form as

$$\mathbf{y}_t = g(\mathbf{x}_t, \widetilde{\sigma}, \mathbf{s}_t) \tag{9}$$

$$\mathbf{x}_{t+1} = h\left(\mathbf{x}_{t}, \widetilde{\sigma}, \mathbf{s}_{t}\right) + \widetilde{\sigma} \Sigma\left(\mathbf{s}_{t}\right) \mathbf{u}_{t+1} \tag{10}$$

for matrix functions $g(\cdot)$, $h(\cdot)$, and $\Sigma(\cdot)$ and a vector of i.i.d. innovations \mathbf{u}_t . The vector \mathbf{s}_t includes the state variables that index the discrete regimes and $\widetilde{\sigma}$ is a perturbation parameter.

Following Hamilton (1994), we can write the law of motion of the discrete processes \mathbf{s}_t as

$$\mathbf{s}_{t+1} = \kappa_0 + \kappa_1 \mathbf{s}_t + \nu_{t+1} \tag{11}$$

for a vector κ_0 and a matrix κ_1 . The law of motion of state $s_{z,t}$, for example, is written as $s_{z,t+1} = (1 - p_{z,0}) + (-1 + p_{z,1} + p_{z,0}) s_{z,t} + \nu_{z,t+1}$, where $\nu_{z,t+1}$ is an innovation with mean zero and heteroskedastic variance.

For the solution, we follow the approach described in Amisano and Tristani (2011), which exploits the model property that regime switches only affect the shock variances. We can therefore apply standard perturbation methods (as in, for example, Schmitt-Grohé and Uribe, 2004a, or Gomme and Klein, 2011) and approximate the solution as a function of the state vector \mathbf{x}_t and perturbation parameter $\widetilde{\sigma}$, but keep it fully nonlinear as a function of the vector \mathbf{s}_t . More specifically, we seek a second-order approximation to the functions $g(\mathbf{x}_t, \widetilde{\sigma}, \mathbf{s}_t)$ and $h(\mathbf{x}_t, \widetilde{\sigma}, \mathbf{s}_t)$ around the non-stochastic steady state, namely the point where $\mathbf{x}_t = \overline{\mathbf{x}}$ and $\widetilde{\sigma} = 0$.

Due to the presence of the discrete regimes in the system, both the steady state and the coefficients of the second order approximation could potentially depend on \mathbf{s}_t in a nonlinear fashion. Since the discrete states only affect the variance of the shocks, however, they disappear when $\tilde{\sigma} = 0$ so that the non-stochastic steady state is not regime-dependent. Amisano and Tristani (2011) demonstrate that the second order approximation can be written as

$$g(\mathbf{x}_t, \widetilde{\sigma}, \mathbf{s}_t) = F\widehat{\mathbf{x}}_t + \frac{1}{2} \left(I_{n_y} \otimes \widehat{\mathbf{x}}_t' \right) E\widehat{\mathbf{x}}_t + k_{y, s_t} \widetilde{\sigma}^2$$
 (Sol1)

and

$$h\left(\mathbf{x}_{t},\widetilde{\sigma},\mathbf{s}_{t}\right) = P\widehat{\mathbf{x}}_{t} + \frac{1}{2}\left(I_{n_{x}}\otimes\widehat{\mathbf{x}}_{t}'\right)G\widehat{\mathbf{x}}_{t} + k_{x,s_{t}}\widetilde{\sigma}^{2}$$
(Sol2)

where F, E, P and G are constant vectors and matrices and only the vectors k_{y,s_t} and k_{x,s_t} are regime dependent.

Note that regime-switching plays no role to a first order approximation. The quadratic terms in the vector of predetermined variables with continuous support are also regime invariant. Changes in volatility only have an impact on the quadratic terms in the per-

turbation parameter $\tilde{\sigma}$. Such terms would be constant in a model with homoskedastic shocks.

3.2 Estimation

Exploiting this feature of the solution, the reduced form system of equations (9) and (10) can be re-written as

$$\mathbf{y}_{t+1}^{o} = k_{y,j} + F\hat{\mathbf{x}}_{t+1} + \frac{1}{2} \left(I_{n_y} \otimes \hat{\mathbf{x}}_{t+1}' \right) E\hat{\mathbf{x}}_{t+1} + D\mathbf{v}_{t+1}$$
(12)

$$\mathbf{x}_{t+1} = k_{x,i} + P\hat{\mathbf{x}}_t + \frac{1}{2} \left(I_{n_x} \otimes \hat{\mathbf{x}}_t' \right) G\hat{\mathbf{x}}_t + \widetilde{\sigma} \Sigma_i \mathbf{w}_{t+1}$$
(13)

$$\mathbf{s}_t \backsim \text{Markov switching}$$
 (14)

where

$$k_{y,j} = k_{y,s_{t+1}=j}$$

$$k_{x,i} = k_{x,s_t=i}$$

$$\Sigma_i = \Sigma(s_t=i).$$

The vector \mathbf{y}_t^o includes all observable variables, and \mathbf{v}_{t+1} and \mathbf{w}_{t+1} are measurement and structural shocks, respectively. In this representation, the regime switching variables affect the system by changing the intercepts $k_{y,j}$, $k_{x,i}$ and the loadings of the structural innovations Σ_i (we indicate here with i the value of the discrete state variables at t and with j the value of the discrete state variables at t+1).

If a linear approximation were used, we would have a linear state space model with Markov switching (see Kim, 1994, Kim and Nelson, 1999, and Schorfheide, 2005). In the quadratic case, however, the likelihood cannot be obtained in closed form. One possible approach to compute the likelihood is to rely on Sequential Monte Carlo techniques (see Amisano and Tristani, 2010a, for an application of these techniques in a DSGE setting with homoskedastic shocks). The convergence of these methods, however, can be very slow in a case, such as the one of our model, in which both nonlinearities and non-Gaussianity of the shocks characterise the economy. Based on the observation that quadratic terms $1/2 \left(I_{n_y} \otimes \hat{\mathbf{x}}'_{t+1} \right) E\hat{\mathbf{x}}_{t+1}$ and $1/2 \left(I_{n_x} \otimes \hat{\mathbf{x}}'_t \right) G\hat{\mathbf{x}}_t$ in equations (12) and (13) tend to be small, we therefore proceed as follows.

At any point in time, we first linearise the two quadratic terms around the conditional mean of the continuous state variables. In a homoskedastic setting, this would correspond to applying the extended Kalman filter. In our model with regime switching, the linearisation must be conditional on the prevailing regime. As a result, at any point in time we can rewrite equations (12) and (13) as

$$\mathbf{y}_{t+1}^{o} = \widetilde{k}_{y,t+1}^{(i,j)} + \widetilde{F}_{t+1}^{(i,j)} \mathbf{\hat{x}}_{t+1} + Dv_{t+1}$$

$$\widehat{\mathbf{x}}_{t+1} = \widetilde{k}_{x,t}^{(i)} + \widetilde{P}_{t}^{(i)} \widehat{\mathbf{x}}_{t} + \Sigma_{i} \mathbf{w}_{t+1}$$

$$(15)$$

where

$$\begin{split} \widetilde{k}_{y,t+1}^{(i,j)} &= \widetilde{k}_{y,j} + \frac{1}{2} \left(I_{n_y} \otimes \hat{\mathbf{x}}_{t+1|t}^{(i)'} \right) E \hat{\mathbf{x}}_{t+1|t}^{(i)} - \boldsymbol{\Delta}_{i,t+1} \hat{\mathbf{x}}_{t+1|t}^{(i)} \\ \widetilde{F}_{t+1}^{(i,j)} &= F + \boldsymbol{\Delta}_{i,t+1} \hat{\mathbf{x}}_{t+1|t}^{(i)} = E(\mathbf{x}_{t+1} | \underline{\mathbf{y}}_{1:t}^{o}, s_t = i, \boldsymbol{\theta}) \\ \boldsymbol{\Delta}_{i,t+1} &= \left[\frac{\partial \left(\frac{1}{2} \left(I_{n_y} \otimes \hat{\mathbf{x}}_{t+1}^{i} \right) E \hat{\mathbf{x}}_{t+1} \right)}{\partial \hat{\mathbf{x}}_{t+1}} \right]_{\hat{\mathbf{x}}_{t+1} = \hat{\mathbf{x}}_{t+1|t}^{(i)}} \\ \widetilde{k}_{x,t}^{(i)} &= \widetilde{k}_{x,i} + \frac{1}{2} \left(I_{n_x} \otimes \hat{\mathbf{x}}_{t|t}^{(i)'} \right) G \hat{\mathbf{x}}_{t|t}^{(i)} - \boldsymbol{\Delta}_{i,t} \hat{\mathbf{x}}_{t|t}^{(i)} \\ \widetilde{P}_{t}^{(i)} &= P + \boldsymbol{\Delta}_{i,t} \hat{\mathbf{x}}_{t|t}^{(i)} = E(\hat{\mathbf{x}}_{t} | \underline{\mathbf{y}}_{1:t}^{o}, s_t = i, \boldsymbol{\theta}) \\ \boldsymbol{\Delta}_{i,t} &= \left[\frac{\partial \left(\frac{1}{2} \left(I_{n_x} \otimes \hat{\mathbf{x}}_{t}^{i} \right) G \hat{\mathbf{x}}_{t} \right)}{\partial \hat{\mathbf{x}}_{t}} \right]_{\hat{\mathbf{x}}_{t} = \hat{\mathbf{x}}_{t+t}^{(i)}} \end{aligned}$$

Note that in the above equations both the intercepts $\widetilde{k}_{y,t+1}^{(i,j)}$, $\widetilde{k}_{x,t}^{(i)}$ and the slope coefficients $\widetilde{F}_{t+1}^{(i,j)}$, $\widetilde{P}_t^{(i)}$ become regime-dependent. Nevertheless, we are still in the world of linear state space models with Markov switching.

We can therefore apply Kim's (1994) approximate filter to forecast

$$\hat{\mathbf{x}}_{t+1|t}^{(i,j)} = \tilde{k}_{x,t}^{(i)} + \tilde{P}_{t}^{(i)} \hat{\mathbf{x}}_{t|t}^{(i)} = \hat{\mathbf{x}}_{t+1|t}^{(i)}$$

$$\mathbf{Q}_{t+1|t}^{(i,j)} = \tilde{P}_{t}^{(i)} \mathbf{Q}_{t|t}^{(i,j)} \tilde{P}_{t}^{(i)'} + \Sigma_{i} \Sigma_{i}' = \mathbf{Q}_{t+1|t}^{(i)}$$

and update the vector of continuous state variables

$$\hat{\mathbf{x}}_{t+1|t+1}^{(j)} = \sum_{i=1}^{m} \hat{\mathbf{x}}_{t+1|t+1}^{(i,j)} \times p(s_t = i|s_{t+1} = j, \underline{\mathbf{y}}_{1:t+1})$$

$$\mathbf{Q}_{t+1|t+1}^{(j)} = \sum_{i=1}^{m} \left[\left(\hat{\mathbf{x}}_{t+1|t+1}^{(i,j)} - \hat{\mathbf{x}}_{t+1|t+1}^{(j)} \right) \left(\hat{\mathbf{x}}_{t+1|t+1}^{(i,j)} - \hat{\mathbf{x}}_{t+1|t+1}^{(j)} \right)' + \mathbf{Q}_{t+1|t+1}^{(i,j)} \right] \times p(s_t = i|s_{t+1} = j, \underline{\mathbf{y}}_{1:t+1})$$

and then update the regime probabilities

$$p(s_{t+1} = j, s_t = i | \underline{\mathbf{y}}_{1:t}) = p_{ij,t+1|t} = p_{ij} \times p(s_t = i | \underline{\mathbf{y}}_{1:t})$$

and

$$p(s_{t+1} = j, s_t = i | \underline{\mathbf{y}}_{t+1}) = p_{ij,t+1|t} \times \frac{p(\mathbf{y}_{t+1} | \underline{\mathbf{y}}_t, s_{t+1} = j, s_t = i)}{p(\mathbf{y}_{t+1} | \underline{\mathbf{y}}_t)}$$

$$p(s_{t+1} = j | \underline{\mathbf{y}}_{1:t+1}) = \sum_{i=1}^m p(s_{t+1} = j, s_t = i | \underline{\mathbf{y}}_{1:t+1})$$

$$p(s_t = i | s_{t+1} = j, \underline{\mathbf{y}}_{1:t+1}) = \frac{p(s_{t+1} = j, s_t = i | \underline{\mathbf{y}}_{1:t+1})}{p(s_{t+1} = j | \underline{\mathbf{y}}_{1:t+1})}$$

where
$$p(\mathbf{y}_{t+1}|\underline{\mathbf{y}}_{1:t}) = \sum_{i=1}^{m} \sum_{j=1}^{m} p(\mathbf{y}_{t+1}|\underline{\mathbf{y}}_{1:t}, s_{t+1} = j, s_t = i) \times p(s_{t+1} = j, s_t = i|\underline{\mathbf{y}}_{1:t})$$

The conditional log-likelihood islog $L = \sum_{t=1}^{T} \log p(\mathbf{y}_{t+1}|\underline{\mathbf{y}}_{1:t})$

We then combined the likelihood with a prior and sample from the posterior using a tuned Metropolis-Hastings algorithm. This approach based on the extended Kalman Filter linearisation is computationally much faster than using sequential Monte Carlo methods.

4 Empirical results

4.1 Functional forms

In our empirical analysis we need to choose a functional form for the utility aggregator $u\{C_t(j) - h\Xi_tC_{t-1}, 1 - N_t(j)\}$. As shown by King, Plosser and Rebelo (1988), consistency with long run growth requires a functional form of the following type

$$u = (C_t - h\Xi_t C_{t-1}) v(N_t)$$

where $v(N_t)$ is a decreasing function. Various options are available for $v(N_t)$. We rely on the particular specification proposed by Trabandt and Uhlig (2011), which implies a constant Frisch elasticity of labour supply in the absence of habits and with standard, expected-utility preferences. The utility aggregator that we use is therefore

$$u = (C_t - h\Xi_t C_{t-1}) \left(1 - \eta (1 - \psi) N_t^{1 + \frac{1}{\phi}} \right)^{\frac{\psi}{1 - \psi}}$$

4.2 Data and prior distributions

We estimate the model on quarterly US data over the sample period from 1966Q1 to 2009Q1. Our estimation sample starts in 1966, because this is often argued to be the

date when a Taylor rule begins providing a reasonable characterization of Federal Reserve policy.⁷ We end in 2009Q1 when the zero bound constraint, which we do not explicitly include in our model, is likely to have become binding.

Concerning the macro data, we use per capita consumption, per capita GDP and inflation. We use both GDP and consumption to impose some discipline on our estimates of the government spending shock. Given that we abstract from investment, consumption in our model captures all interest-sensitive components of private expenditure. As argued by Giannoni and Woodford (2005), assuming habit persistence for the whole level of private expenditure is a reasonable assumption, given that models with capital typically need adjustment costs that imply inertia in the rate of investment spending. We therefore use total real personal consumption per-capita in the information set. Inflation is measured as the logarithmic first-difference in the consumption deflator (all macro variables are from the FRED database of the St. Louis Fed).

We use continuously compounded yields on 3-month, 3-year and 10-year zero-coupon bonds (from the Federal Reserve Board). Prior to the analysis, we take logarithmic first differences for consumption and GDP, which are assumed to follow a stochastic trend. No other data transformations are applied. All variables are expressed in decimal terms per quarter, so that 0.0025 represents an annualized interest rate, inflation rate, or growth rate equal to 1 percent.

Prior and posterior distributions for our model are presented in Table 1.

Concerning regime switching processes, we assume beta priors for transition probabilities. We expect the states to be relatively persistent, so we centre all distributions around a value of 0.9, which implies a persistence of 2.5 years for each state.

We use inverse gamma priors for the standard deviations of the shocks. With the exception of the technology growth shock, which has a tighter prior centred around a small value because the process is a random walk, we keep the prior distribution relatively dispersed around a mean value around 0.003. The regime-switching standard deviations also have the same prior distribution in the high and low regimes. To ensure identification,

⁷According to Fuhrer (1996), "since 1966, understanding the behaviour of the short rate has been equivalent to understanding the behaviour of the Fed, which has since that time essentially set the federal Funds rate at a target level, in response to movements in inflation and real activity". Goodfriend (1991) argues that even under the period of official reserves targeting, the Federal Reserve had in mind an implicit target for the Funds rate.

however, all draws from the prior are first ordered and then assigned to the high or low state. Table 1 reports the resulting empirical distribution for the prior of regime-switching standard deviations. Concerning the persistence of the shocks, we use beta priors centred around the value of 0.85.

For the policy rule, we use relatively loose priors centred around parameter values estimated from quarterly data over a pre-sample period running from 1953 to 1965, namely $\rho_I=0.85,\,\psi_{_{\rm II}}=0.2$ and $\psi_Y=0.02$.

The priors for all utility parameters are specified broadly in line with the rest of the literature. For the ϕ parameter we rely on a normal prior centred around 1.0, a value in between macro estimates and micro estimates of the Frisch elasticity of labour supply (see e.g. the evidence reviewed in Chetty et al., 2011). We use a translated Gamma distribution for ψ and γ , to ensure that $\psi, \gamma > 1$. We centre the distribution of the inverse of the elasticity of intertemporal substitution, ψ , around a value above but close to 1. For the γ parameter, which contributes to shape risk aversion, we use a very large standard deviation whose 95 percent confidence set goes from 2 to 30. The habit parameter has a beta prior centred around 0.5. Finally, for β we use a relatively tight prior with a mean of 0.9985. This is consistent with assumptions made in models with growth—see e.g. Christiano, Motto and Rostagno (2014).

For the long run parameters Ξ and Π^* we rely on more dogmatic priors. For Ξ , which determines the growth rate of the economy in the non-stochastic steady state, we use a tight prior centred around 0.005. This implies an annualized growth rate of 2 percent, which is consistent with the average per-capita U.S. GDP/GNP growth from the 1870s to the 1950s—see Maddison (2013). For the inflation target, we choose a prior centred around 1.0063 that gives most mass to annualized values between 2 and 3 percent.

The price adjustment cost ζ is typically calibrated based on the implied frequency of adjustment of prices in linearized models. In our model, however, the relationship is more complex due to both the nonlinearity of the model and the presence of steady state inflation. We therefore centre the prior around 15, which is roughly consistent, for example, with the value used in Schmitt-Grohé and Uribe (2004b), but allow for a relatively large standard deviation. For inflation indexation, we rely on a beta prior centred around 0.5.

The elasticity of intratemporal substitution θ , which is weakly identified, is set dogmatically at 6. Similarly, we set $\mu_w = 1.2$.

4.3 Posterior distributions and goodness of fit

The posterior distributions of structural parameters in Table 1 suggest that the data are informative about the estimation of most parameters, as witnessed by the typically smaller standard deviation of the posterior distribution compared to the prior distribution.

More specifically, the different regimes in the volatilities of monetary policy, technology and government spending shocks are clearly identified. For monetary policy, the standard deviations in the low and high regimes are equal to 0.13 percent and 0.39 percent respectively. These values straddle the constant standard deviation of 0.24 percent estimated in Smets and Wouters (2007). The standard deviation of technology shocks change between 1.1 percent in the low volatility regime and 2.7 percent in the high volatility regime. The difference between the two volatility regimes is largest for government spending shocks: its standard deviation shifts between 0.33 and 3.2 percent.

The posterior mode of the transition probabilities suggests that the low-volatility states are more persistent for monetary policy and technology shocks. For policy shocks, the ergodic probability of being in the low-volatility state is approximately 0.69, which is consistent with the idea that policy shocks were small over most of the sample, except for the Volcker disinflation period. Both the low and the high volatility states are more persistent for technology shocks. These states are countercyclical, being persistently high during recessions and low over expansions. The ergodic probability of the low volatility state for technology shocks is 0.71. In contrast, the volatility of government spending shocks is more persistent in the high state, whose ergodic probability is 0.68.

As in estimates solely based on macro data, some shock processes tend be highly serially correlated. At 0.99, the correlation of the level technology shock process is especially high. Together with the features of the monetary policy rule, this implies that technology shock have very persistent effects.

The estimated parameter values of the coefficients of the monetary policy rule are of particular interest. Ceteris paribus different parameters of the policy rule will be associated with different expectations of the future path of short-term interest rates, thus different configurations of the yield curve. Since we explicitly use yields data when estimating the model, our estimates of the policy rule parameters should be more informative than those obtained without including yields in the econometrician's information set. Given the well-known problems of general equilibrium models to match the unconditional volatility of

long-term yields (see e.g. Den Haan, 1995), one would expect the degree of interest rate smoothing to be higher than in estimates ignoring yields data. A higher smoothing coefficient would impart persistence to any movements in the short-term rate. Its variability would thus be transmitted to longer rates (for a discussion of this point, see Hördahl, Tristani and Vestin, 2008).

To compare our estimates to those in the literature, it is useful to rewrite the rule in partial adjustment form. Our parameter estimates then imply:

$$\hat{i}_t = 0.09 \left[3.09 \left(\pi_t - \pi^* \right) + 0.57 \left(\widetilde{y}_t - \widetilde{y} \right) \right] + 0.91 \, \hat{i}_{t-1} + \eta_{t+1}. \tag{16}$$

Equation (16) confirms the above intuition. Compared to the estimates in Smets and Wouters (2007), our parameters imply a somewhat higher, but not exceedingly large, inflation response coefficient.⁸ The more striking feature of our estimates, however, is the increase in the degree of interest rate smoothing (0.91 vs. 0.81 in Smets and Wouters). More inertial movements in short-term rates imply that longer-term yields can be systematically affected by monetary policy. This feature is important for the model to be able to generate sufficient variation at longer maturities in the term-structure of interest rates.⁹

The estimates of the other structural parameters are roughly consistent with the existing literature.

Concerning long-run means, the mode of the quarterly trend growth rate of technology is 0.45 and the quarterly inflation target is 0.61, both within the posterior distribution of estimates obtained in Smets and Wouters (2007).

Amongst preference parameters, the posterior mean of ϕ is 0.6. Our estimate of ψ implies a long-run elasticity of intertemporal substitution of consumption of 0.76, which is in line with other available estimates (see e.g. Basu and Kimball, 2002). The γ parameter is equal to 11.5 and the habit parameter h = 0.86. Together, these two parameters are suggestive of a high level of risk aversion, which is in line with the results in Piazzesi and Schneider (2006), or in Rudebusch and Swanson (2012).

⁸The parameter estimates are not fully comparable, because the policy rule used in Smets and Wouters (2007) includes additional arguments.

⁹De Graeve, Emiris and Wouters (2009) also uses yields data in estimation, but obtains interest rate smoothing estimates similar to Smets and Wouters (2007). In De Graeve, Emiris and Wouters (2009), however, persistent movements in policy interest rates are driven by changes in a stochastic inflation target, which is almost a random walk.

All in all, our model goes a long way in fitting both macroeconomic and yields data. This claim is supported by four pieces of evidence.

First, measurement errors on all variables are small. This is perhaps not surprising for macro variables and for the short-term interest rate, given the results in Smets and Wouters (2007). For longer-term yields, however, one could expect a worse performance. Nevertheless, both 3-year and 12-year rates are fit rather well. The measurement errors on these two variables are equal to 29 and 18 basis points, respectively. This is a comparable fit to the results in more empirically flexible models such as Ang and Piazzesi (2003).¹⁰

Second, we check the implications of our model in terms of the dynamic correlations it implies between observable variables—see panels (a) and (b) in figure 2. Model-implied dynamic correlations at lags and leads up to 20 quarters are compared to sample correlations. Model-implied correlations are computed for all posterior draws and error bands corresponding to a 95 percent confidence set are also displayed in figure 2.

By and large, the figure indicates that our model captures reasonably well the dynamic cross-correlations between all variables. The distribution of model-implied dynamic correlations tends to always include its empirical counterpart. This is specifically the case for autocorrelations, that start from an appropriately high value and tend to decay in line with the empirical measures.

Third, we test the implications of our model for dimensions of the data which were not directly used in estimation, notably for forward rates at various horizons. Model-implied and actual 3-month forward rates in 1, 3 and 10 years are reported in figure 3. Note that the 1-year rate was not used in estimation. Nevertheless, the model tracks well the evolution of all forward rates. More specifically, the model can track well the variations in the long-term forward rate that we documented in figure 1(a).

Our fourth and final goodness-of-fit test is to check the distribution of one-step-ahead forecast errors, that are reported in figure 4. This is a strict test, which highlights if the model occasionally tends to over- or under-predict specific variables over time. Instances of underprediction do occur, for example, for inflation during the two peaks in 1974 and 1980 and, to a lesser extent, for the short term interest rate in 1980. However, these episodes tend to be short-lived. Inflation and yields forecasts are essentially unbiased in the rest of the sample.

 $^{^{10}\}mathrm{Ang}$ and Piazzesi (2003) is however estimated on more volatile, monthly data.

Table 2 reports the forecast error variance decompositions of all endogenous variables over horizons of 1, 4, 12 and 40 quarters ahead. Focusing on 10-year and 3-year yields, it shows that these are mostly driven by technology shocks at 1-quarter to 1-year horizons. At business cycle and lower frequencies, however, technological uncertainty shocks become increasingly important. Over a forecast horizon of 40 quarters, technological uncertainty shocks account for 54% of the variance of 10-year yields and 53% of the variance of 3-year yields.

4.4 Volatility regimes and uncertainty shocks

Figure 5 displays filtered and smoothed estimates of the probability of being in a low-variance regime for the three heteroskedastic shocks.

The government spending shock has high variance in the first part of the sample and lower variance during the Great moderation period.

Concerning the monetary policy shock, our results are consistent with those in Justiniano and Primiceri (2008), where heteroskedasticity takes the form of stochastic volatility, rather than regime switching. The policy shock has a high variance during the mid-1970s and again during the so-called "Volcker disinflation" period in 1979-83. One marginally different feature of our results, is that the increase in volatility in 1979 is estimated to be very rapid in real time. This is arguably consistent with the spikes which can be observed in the short term interest rate over this period. Such sudden increases in volatility can more easily be captured by a regime-switching model than by a stochastic volatility model.

The most striking feature of the regimes for the variance of technology shocks in Figure 5 is that they are strongly cyclical. Starting in 1980, the standard deviation of these shocks tends to increase at the beginning of each recessions and to fall again after a few quarters. This pattern is quite systematic, especially over the 1990s and the 2000s. The period of the Volcker disinflation is therefore unique in being characterized by high variance of government spending, policy and technology shocks.

We next focus on the impulse responses to uncertainty shocks. Changes in the volatility of government spending and policy shocks turn out to have negligible macroeconomic effects. The impact of variations in the standard deviation of technology shocks, however, is large. The impulse responses to an increase in the variance of technology from the low to the high regime is displayed in Figure 6. For illustrative purposes, in this figures we

assume that the high variance regime is an absorbing state.

An increase in the variance of technology shocks generates an immediate increase in the demand for precautionary saving. As a result, the demand for consumption goods falls. Given that prices are sticky and output is demand determined, lower demand for consumption goods generates a fall in output and inflation. The policy rate also falls according to the Taylor rule. To clear the savings market, however, real rates must fall at all future horizons, because the uncertainty shock is expected to be persistent. The fall is marked at short horizons, more muted at longer horizons, when the conditional variance of technology shocks is expected to decline again, due to the probability of it switching back to the low-variance regime. As a result, the expected policy rate remains persistently low as long as the detrended level of output remains below its steady state, which is long after the negative inflationary shock has been reabsorbed.

All in all, and consistently with the results in Basu and Bundick (2012), an uncertainty shock in technology looks like a demand shock, in the sense of being associated with a fall in output, consumption and prices at the same time. Our results also corroborates, in the context of an estimated model, Basu and Bundick's finding that a persistent fall in nominal interest rates is an important part of the macroeconomic adjustment mechanism, following an uncertainty shock. If the fall in the nominal interest rate were prevented by the zero lower bound, the macro-economic effects of the shock would be even larger.

At the same time, however, Figure 6 shows that 3-year rates fall less than what is suggested by the average path of future policy interest rates, and that 10-year rates actually increase after the shock. To understand these impulse responses, it is important to delve more deeply in the dynamics of risk premia.

5 Monetary policy and long term rates

We have shown that uncertainty shocks have macroeconomic effects. We now investigate their effects on bond prices.

5.1 Monetary policy and risk premia

Nominal bonds reflect risk premia associated with both consumption risk and with inflation risk. Hördahl, Tristani and Vestin (2008) demonstrate that models with homoskedastic

shocks solved to a second order approximation can only generate constant risk premia. Consistently with this result, our model can produce changes in risk premia only when there is a change in the standard deviation of the structural shocks. In other words, time variation in risk premia is associated with switches in the variance regimes.

A typically used measure of risk premia which is independent of expected changes in the future path of short term interest rate is the expected excess holding period return on a bond of maturity n. This corresponds to the expected return that can be earned by holding an n-maturity bond for one quarter in excess of the one quarter interest rate. The expected excess holding period return generated by our model for the 3-year and 10-year bonds is displayed in Figure 7.

A notable feature of Figure 7 is that excess holding period returns can be large. At the 10-year maturity, they oscillate between 2 and 13 percentage points per year. This is in the same order of magnitude as estimates from the finance literature—see e.g. Figure 1 in Duffee (2002). Also consistently with the finding in that literature (see e.g. Fama and French, 1989), risk premia are countercyclical.

In contrast to the finance literature, however, we estimate variations in risk premia to be much more infrequent. Our results suggest that they were constant up until the end of the 1970s.

One could expect that regime switches in the volatility of all shocks to possibly lead to variation in risk premia. In the model, however, variations in risk premia must be associated with uncertainty about revisions in the rate of growth of future utility and with their correlations with inflation and with the marginal utility of consumption—see Restoy and Weil (2011) and Piazzesi and Schneider (2006). From a quantitative perspective, monetary policy and government spending shocks have a relatively small impact on the rate of growth of utility over long future horizons. Changes in their variance have therefore a small impact on the size of risk premia. This can be observed through a comparison of Figures 5 and 7, where it becomes apparent that large changes in risk premia are not associated with switches in the regimes of policy or government spending shock.

The key source of quantitatively sizable time-variation in risk premia are switches in the variance of technology shocks. Since these variance regimes are estimated very precisely, also in real time, risk premia oscillate mostly between a high and a low value. Consistently with the cyclicality of technological uncertainty shocks, risk premia increase during every NBER-dated recession, then fall again after a few years.

It goes without saying that considerable uncertainty characterizes any estimates of risk premia, because of estimation and model uncertainty. Figure 7 shows that filtering uncertainty is around 5 percentage points at the 10-year maturity. In a classical econometric setting, the small sample bias in maximum likelihood estimates also plays a role–see e.g. Bauer, Rudebusch and Wu (2014), and Wright (2014).

5.2 Yields and the monetary policy transmission mechanism

We have shown that changes in the conditional variances of technology shocks play an important cyclical role.

At the beginning of recessions, the increase in volatility is tantamount to a persistent fall in confidence. Risk premia become larger, precautionary saving increases, consumption, output and inflation fall. Both current and expected future nominal interest rates also fall, but actual long term yields can increase, due to an increase in risk premia at longer horizons. After the recovery sets in, however, the conditional variance of technology switches back to lower levels and confidence returns. The demand for precautionary saving falls back to normal levels, expected future policy interest rates increase, but long term yields are also affected by the marked reduction in risk premia. During cyclical turning points, a model with constant premia does not provide a good description of long-term yields. Movements in long-term yields are primarily the result of changes in real yields and risk premia.

More specifically, changes in long-term yields need not be related to expected future monetary policy moves. This occurred famously in 2004, when long-term yields did not increase in the face of the increase in expected future policy rates. Such behavior of long term yields would be entirely standard in a linearized version of the new Keynesian model, but it represents an anomaly compared to typical cyclical developments in bond yields. In his semiannual Monetary Policy Report to the Congress, Chairman Greenspan stated that "the broadly unanticipated behavior of world bond markets remains a conundrum"—see Greenspan (2005). From the perspective of our model, the only unanticipated features of bond developments over the conundrum period is the timing of the downward volatility shock—see Figure 8. Otherwise, a reduction in volatility, and thus a reduction in risk premia, during a cyclical upswing is entirely to be expected.

It is important to note that the cyclical fluctuations of real yields and of the term spread are not only a feature of the past. Figure 1 shows that non-negligible changes in 3-month forward rates 10-year ahead are also visible over the 1990s and the 2000s, i.e. periods of low inflation. Dampened fluctuations in the term spread, compared to the model implications, continue being observed over recent recessions.

Over the prolonged periods in which volatility stays constant, however, long-term rates react to changes in monetary policy rates according to the expectations hypothesis. Changes in long term rates reflect variations in *long-term inflation expectations*.

This result sheds light on the ability of the linearized, new Keynesian model to account for the monetary policy transmissions mechanism. Over the years between occasional changes in volatility, that model works well: up to a constant risk premium, long-term yields correspond to average expected future short term rates. The connection between long term yields and monetary policy can then be well understood via a linearized model.

This logic may explain the acceptable forecasting performance of linearized models over specific periods of time. For example, De Graeve *et al.* (2009) finds that a linearized model is competitive with the random walk in forecasting 1-year yields up to 3-year ahead over the 1990:Q1-2007Q1 period, but less successful in forecasting longer maturity yields. This is not so surprising given that, according to our estimates, risk premia tend to be smaller at short horizons and they only increased and fell four times over the 1990:Q1-2007Q1 period.

Over periods of constant risk premia, variations in long-term interest rates and long-term inflation expectations must be accounted for by standard shocks. More specifically, our model relies also on standard Gaussian shocks to account for the secular changes in long-term interest rates and long-term forward rates documented in Figure 1(a). To produce changes in long-term rates, such shocks must be extremely persistent and they need to be coupled with a high degree of inertia in the monetary policy rule. A single shock plays this role in our model: the level technology shock z_t .

Figure 9 shows an impulse response to the technology shock. The shock has the usual opposite effects on output and inflation: real variables increase, while inflation falls. Contrary to typical results, however, the shock generates extremely persistent responses of macroeconomic variables. This is due, first, to the extremely high persistence of the

autoregressive process for z_t , whose half-life is of about 15 years.¹¹ Second, it is due to the high interest rate smoothing coefficient of the Taylor rule, which keeps the short-term real interest rate positive over many quarters after the shock. The increase in the real interest rates reinforces the initial fall in inflation and requires an increasingly loose monetary policy stance over the first year after the shock. It is only after two years that all variables slowly start returning towards their long-run value in a monotonic fashion. In the absence of regime switches, the expectations hypothesis holds and long-term rates fall alongside the policy interest rate.

Both uncertainty shocks and level technology shocks affect inflation over a prolonged period. It is therefore instructive to analyze the overall implications of our estimates for long-term inflation expectations—i.e. expected inflation over the next 10-year. These expectations are important as their stability, or "anchoring", is often interpreted as a measure of central banks' anti-inflationary credibility. As a benchmark for comparison, we use expectations by the Federal Reserve Bank of Philadelphia's quarterly Survey of Professional Forecasters combined with the Blue Chip Economic Indicators, which is available since 1979:Q4.¹²

From a secular perspective, a downward trend can clearly be identified in long-term inflation expectations over the 1980s. Over this period, model-implied 10-year inflation expectations are roughly consistent with the survey data—see Figure 10. The high volatility of the early 1980s kept risk premia and yields high, even as expected future inflation and expected future policy rates were coming down. From this long-term perspective, the improved anchoring of inflation expectations in the U.S. is undoubtable.

From a more cyclical perspective, however, survey and model-implied results differ. Survey expectations fall steadily towards 2.5 percent over the 1990s and then remain constant at that level through the 2000s. In contrast, yields dynamics interpreted through the lens of our model suggest a much less tight anchoring of inflation expectations.

Model-implied measures fall faster than surveys during the policy tightening phase

¹¹ The half-life is defined as the number of periods over which the effect of a unit shock remains above

^{0.5.} For an autoregressive process with serial correlation coefficient ρ , the half-life is $hl = \ln(0.5) / \ln(\rho)$.

¹²Both surveys report forecasts for the average rate of CPI inflation over the next 10 years. The Blue Chip survey reports long-term inflation forecasts taken twice a year (March and October). Prior to 1983, and in 1983:4, the variable was the GNP deflator rather than the CPI. As of 1991:Q4, we rely on the Philadelphia Survey of Professional Forecasters.

which started in spring 1988 and was followed by the 1990 Gulf War and the ensuing recession. The fall in long-term inflation expectations is smaller than the fall in 10-year yields, because it is accompanied by a surge in volatility and a fall in real rates.

Model-implied inflation expectations increase again sharply in 1993. An increase in long-term inflation expectations is in line with the idea of an "inflation scare", which was put forward by some commentators in this period. For example, Goodfriend (2002) states: "Starting from a level of 5.9 percent [in October 1993], the 30-year bond rate rose through 1994 to peak at 8.2 percent just before election day in November. The nearly 2 1/2 percentage point increase in the bond rate indicated that the Fed's credibility for low inflation was far from secure in 1994."

Following this period, model-implied inflation expectations remain roughly close to the survey measures. However, model-implied expectations diverge again during the recession of the early 2000s, when they fall sharply to levels around 1. These dynamics are arguably consistent with the views of Federal Reserve officials, who expressed concerns about the, albeit remote, possibility of deflation from late 2002 through 2003. In November 2002, the then Governor Bernanke (2002) judged that "the chance of significant deflation in the United States in the foreseeable future is extremely small", but added that "having said that deflation in the United States is highly unlikely, I would be imprudent to rule out the possibility altogether."

After a return towards 2.5 percent, model-implied long-term inflation expectations fall again ahead of the Great recession, i.e. a period when the possibility of a protracted, low-inflation period was difficult to rule out.

To summarise, our model-implied estimate of long-term inflation expectations implicit in bond prices complements comparable information available from survey data. It suggests that long-term inflation expectations are less firmly anchored than one would conclude, based on survey data.

6 Conclusions

We have presented the results of the estimation of a nonlinear macro-yield curve model with Epstein-Zin-Weil preferences, in which the variance of structural shocks is subject to changes of regime. We have argued that the model fits the data well: measurement errors are small; the dynamic cross-correlation matrix of the data is closely replicated; long-term forward rates are matched.

An important role to account for this performance is played by changes in variance regimes, or uncertainty shocks, which tends to occur during recessions. On the one hand, uncertainty shocks induce changes in the demand for precautionary savings. Expected real and nominal yields also fall, which is consistent with the empirical evidence. On the other hand, the increase in volatility during recessions also boosts uncertainty over future consumption growth. Risk premia increase in a countercyclical fashion, which is consistent with results from the finance literature.

Our results suggest that movements in long-term yields can reflect both variations in long-term inflation expectations, and changes in *real* yields induced by uncertainty shocks. Compared to survey evidence, our measures of long-term inflation expectations are more variable over the economic cycle. They fall to low levels over the 1980s, but are subject to cyclical "scares"—either upwards or downwards. They suggest that the Federal Reserve's credibility for low inflation is less firmly established than one would conclude, based on survey data.

Appendix

A The household problem

The optimization problem is:

$$\max U\left[u_{t}, E_{t}V_{t+1}\right] = \left\{ (1 - \beta) u_{t}^{1-\psi} + \beta \left(E_{t}V_{t+1}^{1-\gamma}\right)^{\frac{1-\psi}{1-\gamma}} \right\}^{\frac{1}{1-\psi}}$$

where u_t is shorthand for $u\left\{C_t\left(j\right) - h\Xi_tC_{t-1}, 1 - N_t\left(j\right)\right\}$, subject to

$$P_{t}C_{t}(j) + \mathbb{E}_{t}Q_{t,t+1}W_{t+1}(j) \leq W_{t}(j) + w_{t}(j)N_{t}(j) + \int_{0}^{1} \Psi_{t}(i)di - T_{t}$$

and

$$N_{t}\left(j\right) = L_{t}\left(\frac{w_{t}\left(j\right)}{w_{t}}\right)^{-\theta_{w,t}}$$

where the choice variables are w_s and c_s

Bellman equation is

$$J(W_{t}) = \max \left\{ (1 - \beta) u_{t}^{1 - \psi} + \beta \left[E_{t} J^{1 - \gamma} (W_{t+1}) \right]^{\frac{1 - \psi}{1 - \gamma}} \right\}^{\frac{1}{1 - \psi}}$$
$$-\Lambda_{t} \left[P_{t} C_{t} + E_{t} Q_{t, t+1} W_{t+1} - W_{t} - w_{t} N_{t} - \int_{0}^{1} \Psi_{t} (i) di + T_{t} \right]$$

where

$$N_{t}\left(j
ight) = L_{t}\left(rac{w_{t}\left(j
ight)}{w_{t}}
ight)^{- heta_{w,t}}$$

and

$$\frac{\partial N_{t}(j)}{\partial w_{t}(j)} = -\theta_{w,t} \frac{N_{t}(j)}{w_{t}(j)}$$

Using the aggregator function $U = \left\{ (1 - \beta) u_t^{1-\psi} + \beta v_t^{1-\psi} \right\}^{\frac{1}{1-\psi}}$, where $v_t \equiv \left[\mathbf{E}_t J^{1-\gamma} \left(W_{t+1}, C_t \right) \right]^{\frac{1}{1-\gamma}}$ define

$$U_{u,t} = (1 - \beta) \left\{ (1 - \beta) u_t^{1-\psi} + \beta v_t^{1-\psi} \right\}^{\frac{\psi}{1-\psi}} u_t^{-\psi}$$
$$U_{v,t} = \beta \left\{ (1 - \beta) u_t^{1-\psi} + \beta v_t^{1-\psi} \right\}^{\frac{\psi}{1-\psi}} v_t^{-\psi}.$$

The FOCs include

$$U_{u,t}u_{c,t} = \Lambda_{t}P_{t}$$

$$u_{N,t}U_{u,t}\frac{\partial N_{t}\left(j\right)}{\partial w_{t}\left(j\right)} = -\Lambda_{t}\left[N_{t}\left(j\right) + w_{t}\left(j\right)\frac{\partial N_{t}\left(j\right)}{\partial w_{t}\left(j\right)}\right]$$

and state-by-state

$$U_{v,t} \left[E_t J^{1-\gamma} (W_{t+1}) \right]^{\frac{\gamma}{1-\gamma}} J^{-\gamma} (W_{t+1}) J_W (W_{t+1}) = \Lambda_t Q_{t,t+1}$$

plus envelope

$$J_{W}\left(W_{t}\right) = \Lambda_{t}$$

The FOCs can be rewritten as

$$\begin{array}{lcl} \frac{\Lambda_{t}P_{t}}{u_{c,t}} & = & U_{u,t} \\ \\ \frac{u_{N,t}}{u_{c,t}} & = & \frac{1-\theta_{w,t}}{\theta_{w,t}}\frac{w_{t}\left(j\right)}{P_{t}} \\ \\ Q_{t,t+1} & = & U_{v,t}\left[\operatorname{E}_{t}J_{t+1}^{1-\gamma}\right]^{\frac{\gamma}{1-\gamma}}J_{t+1}^{-\gamma}\frac{\Lambda_{t+1}}{\Lambda_{t}} \end{array}$$

or

$$Q_{t,t+1} = \beta \left(\frac{\left[\mathbf{E}_t J_{t+1}^{1-\gamma} \right]^{\frac{1}{1-\gamma}}}{J_{t+1}} \right)^{\gamma-\psi} \frac{u_{t+1}^{-\psi}}{u_t^{-\psi}} \frac{u_{c,t+1}}{u_{c,t}} \frac{1}{\Pi_{t+1}}$$

Using the definition of $\mu_{w,t}$, we obtain, as in the text,

$$-\frac{u_{N,t}}{u_{c,t}} = \mu_{w,t} \frac{w_t(j)}{P_t}$$

and

$$Q_{t,t+1} = \beta \left[E_t \left(\frac{J_{t+1}}{J_t} \right)^{1-\gamma} \right]^{\frac{\gamma-\psi}{1-\gamma}} \left(\frac{J_{t+1}}{J_t} \right)^{-(\gamma-\psi)} \left(\frac{u_{t+1}}{u_t} \right)^{-\psi} \frac{u_{c,t+1}}{u_{c,t}} \frac{1}{\Pi_{t+1}}$$

A.1 Detrending

Given the stochastic trend B_t , define a detrended variable as $\tilde{x}_t \equiv x_t/B_t$. It follows that we can rewrite the conditions above as

$$\begin{split} &-\frac{\widetilde{u}_{N,t}}{u_{c,t}} &= \frac{\theta_{w,t}-1}{\theta_{w,t}} \frac{\widetilde{w}_t\left(j\right)}{P_t} \\ &\widetilde{J}_t^{1-\psi} &= \left(1-\beta\right) \widetilde{u}_t^{1-\psi} + \beta \left[\operatorname{E}_t \Xi_{t+1}^{1-\gamma} \widetilde{J}_{t+1}^{1-\gamma} \right]^{\frac{1-\psi}{1-\gamma}} \\ &\widetilde{u}_t &= u \left(\widetilde{C}_t\left(j\right) - h \widetilde{C}_{t-1}, 1 - N_t\left(j\right) \right) \\ &Q_{t,t+1} &= \beta \left(\frac{\left[\operatorname{E}_t \widetilde{J}_{t+1}^{1-\gamma} \Xi_{t+1}^{1-\gamma} \right]^{\frac{1}{1-\gamma}}}{\widetilde{J}_{t+1} \Xi_{t+1}} \right)^{\gamma-\psi} \left(\frac{\widetilde{u}_{t+1}}{\widetilde{u}_t} \right)^{-\psi} \frac{u_{c,t+1}}{u_{c,t}} \frac{1}{\Pi_{t+1} \Xi_{t+1}^{\psi}} \end{split}$$

B Firms' optimization problem

Under Rotemberg prices, firm j maximizes real profits

$$\max_{P_t^j} E_t \sum_{s=t}^{\infty} Q_{t,s} \left[\frac{P_s^j Y_s^j}{P_s} - \frac{w_s}{P_s} \left(\frac{Y_s^j}{A_s} \right)^{\frac{1}{\alpha}} - \frac{\zeta}{2} \left(\frac{P_s^j}{P_{s-1}^j} - (\Pi^*)^{1-\iota} \Pi_{s-1}^{\iota} \right)^2 Y_s \right]$$

subject to the total demand for its output

$$Y_t(j) = \left(\frac{P_t(j)}{P_t}\right)^{-\theta} Y_t$$

and to the production function

$$Y_t(j) = A_t L_t^{\alpha}(j)$$

where L_t is the labour index defined above.

The FOC is

$$0 = (1 - \theta) \left(\frac{P_t^j}{P_t}\right)^{-\theta} Y_t \frac{1}{P_t} + \frac{\theta}{\alpha} \frac{w_t}{P_t} \left(\frac{Y_t}{A_t}\right)^{\frac{1}{\alpha}} \left(\frac{P_t^j}{P_t}\right)^{-\frac{\theta}{\alpha} - 1} \frac{1}{P_t} - \zeta \left(\frac{P_t^j}{P_{t-1}^j} - (\Pi^*)^{1-\iota} \Pi_{t-1}^{\iota}\right) Y_t \frac{1}{P_{t-1}^j} + E_t Q_{t,t+1} \zeta \left(\frac{P_{t+1}^j}{P_t^j} - (\Pi^*)^{1-\iota} \Pi_t^{\iota}\right) Y_{t+1} \frac{P_{t+1}^j}{P_t^j} \frac{1}{P_t^j}$$

or, noting that all firms will set the same price and expressing variables in detrended form,

$$(\theta - 1)\widetilde{Y}_t + \zeta \left(\Pi_t - (\Pi^*)^{1-\iota} \Pi_{t-1}^{\iota}\right) \widetilde{Y}_t \Pi_t = \frac{\theta}{\alpha} \frac{\widetilde{w}_t}{P_t} \frac{1}{Z_t^{\frac{1}{\alpha}}} \widetilde{Y}_t^{\frac{1}{\alpha}} + \operatorname{E}_t Q_{t,t+1} \zeta \left(\Pi_{t+1} - (\Pi^*)^{1-\iota} \Pi_t^{\iota}\right) \widetilde{Y}_{t+1} \Xi_{t+1} \Pi_{t+1}$$

C Equilibrium

Equilibrium is described by the following system:

• households

$$\begin{split} \frac{\Lambda_t P_t}{u_{c,t}} &= (1-\beta) \, \widetilde{u}_t^{-\psi} \widetilde{J}_t^{\psi} \\ -\frac{\widetilde{u}_{N,t}}{u_{c,t}} &= \frac{\theta_{w,t} - 1}{\theta_{w,t}} \frac{\widetilde{w}_t}{P_t} \\ \widetilde{J}_t^{1-\psi} &= (1-\beta) \, \widetilde{u}_t^{1-\psi} + \beta \left[\mathbb{E}_t \Xi_{t+1}^{1-\gamma} \widetilde{J}_{t+1}^{1-\gamma} \right]^{\frac{1-\psi}{1-\gamma}} \\ \widetilde{u}_t &= u \left(\widetilde{C}_t - h \widetilde{C}_{t-1}, 1 - N_t \right) \\ Q_{t,t+1} &= \beta \left[\mathbb{E}_t \widetilde{J}_{t+1}^{1-\gamma} \Xi_{t+1}^{1-\gamma} \right]^{\frac{\gamma-\psi}{1-\gamma}} \frac{\widetilde{J}_t^{\psi}}{\widetilde{J}_{t+1}^{\gamma} \Xi_{t+1}^{\gamma}} \frac{\Lambda_{t+1}}{\Lambda_t} \end{split}$$

• firms

$$(\theta - 1) \widetilde{Y}_{t} = -\zeta \left(\Pi_{t} - (\Pi^{*})^{1-\iota} \Pi_{t-1}^{\iota} \right) \widetilde{Y}_{t} \Pi_{t} + \frac{\theta}{\alpha} \frac{\widetilde{w}_{t}}{P_{t}} \frac{1}{Z_{t}^{\frac{1}{\alpha}}} \widetilde{Y}_{t}^{\frac{1}{\alpha}}$$

$$+ \operatorname{E}_{t} Q_{t,t+1} \zeta \left(\Pi_{t+1} - (\Pi^{*})^{1-\iota} \Pi_{t}^{\iota} \right) \widetilde{Y}_{t+1} \Xi_{t+1} \Pi_{t+1}$$

• market clearing

$$\widetilde{Y}_t = \widetilde{C}_t + \widetilde{G}_t + \frac{\zeta}{2} \left(\Pi_t - (\Pi^*)^{1-\iota} \Pi_{t-1}^{\iota} \right)^2 \widetilde{Y}_t$$

$$N_t = \widetilde{Y}_t^{\frac{1}{\alpha}} Z_t^{-\frac{1}{\alpha}}$$

• policy rule

$$I_t = \left(\frac{\Pi^* \Xi_{t+1}^{\psi}}{\beta}\right)^{1-\rho_I} \left(\frac{\Pi_t}{\Pi_t^*}\right)^{\psi_\Pi} \left(\frac{\widetilde{Y}_t}{\widetilde{Y}}\right)^{\psi_Y} I_{t-1}^{\rho_I} e^{\varepsilon_{t+1}^I}$$

• shocks

$$\begin{split} \Xi_t &= \overline{\Xi}^{1-\rho_\xi} \Xi_{t-1}^{\rho_\xi} e^{\varepsilon_t^\xi}, \qquad \varepsilon_{t+1}^\xi \approx N\left(0, \sigma_\xi\right) \\ \widetilde{G}_t &= \left(g\widetilde{Y}\right)^{1-\rho_g} \widetilde{G}_{t-1}^{\rho_g} e^{\varepsilon_t^g}, \qquad \varepsilon_{t+1}^g \approx N\left(0, \sigma_g\right) \\ \mu_{w,t+1} &= \mu_w^{1-\rho_\mu} \left(\mu_{w,t}\right)^{\rho_\mu} e^{\varepsilon_{t+1}^\mu}, \qquad \varepsilon_{t+1}^\mu \approx N\left(0, \sigma_\mu\right) \\ Z_t &= Z_{t-1}^{\rho_z} e^{\varepsilon_t^z}, \qquad \varepsilon_{t+1}^z \approx N\left(0, \sigma_{z,s_{z,t}}\right) \\ \eta_{t+1} &= e^{\varepsilon_{t+1}^\eta}, \qquad \varepsilon_{t+1}^\eta \approx N\left(0, \sigma_{\eta,s_{\eta,t}}\right). \end{split}$$

• standard deviations

$$\sigma_{z,s_{z,t}} = \sigma_{z,0} s_{z,t} + \sigma_{z,1} (1 - s_{z,t})
\sigma_{\eta,s_{\eta,t}} = \sigma_{\eta,0} s_{\eta,t} + \sigma_{\eta,1} (1 - s_{\eta,t})$$

• C_{-1} , I_{-1} , Π_{-1} given.

D Numerical implementation

For the numerical implementation of the model, we scale the maximum value function by a constant κ to increase accuracy. Define a dummy variable $\widetilde{D}_t = \mathrm{E}_t \Xi_{t+1}^{1-\gamma} \widetilde{J}_{t+1}^{1-\gamma} / \kappa^{1-\gamma}$. It follows that $\kappa^{1-\gamma} \widetilde{D}_t = \mathrm{E}_t \Xi_{t+1}^{1-\gamma} \widetilde{J}_{t+1}^{1-\gamma}$. This implies

$$\widetilde{D}_t = \frac{\mathbf{E}_t \Xi_{t+1}^{1-\gamma} \widetilde{J}_{t+1}^{1-\gamma}}{\kappa^{1-\gamma}}$$

$$\widetilde{J}_{t}^{1-\psi} = (1-\beta)\widetilde{u}_{t}^{1-\psi} + \beta\kappa^{1-\psi}\widetilde{D}_{t}^{\frac{1-\psi}{1-\gamma}}$$

$$Q_{t,t+1} = \beta \left(\frac{\kappa\widetilde{D}_{t}^{\frac{1}{1-\gamma}}}{\widetilde{J}_{t+1}}\right)^{\gamma-\psi} \left(\frac{\widetilde{u}_{t+1}}{\widetilde{u}_{t}}\right)^{-\psi} \frac{u_{c,t+1}}{u_{c,t}} \frac{1}{\Xi_{t+1}^{\gamma}} \frac{1}{\Pi_{t+1}}$$

D.1Functional forms

We rely on the Trabandt and Uhlig (2011) form for temporary utility, i.e.

$$u_t = (C_t - h\Xi_t C_{t-1}) \left(1 - \eta (1 - \psi) N_t^{1 + \frac{1}{\phi}}\right)^{\frac{\psi}{1 - \psi}}$$

As a result

As a result
$$\frac{\widetilde{w}_{t}}{P_{t}} = \frac{\eta \psi \left(1 + \frac{1}{\phi}\right) \left(\widetilde{C}_{t} - h\widetilde{C}_{t-1}\right) N_{t}^{\frac{1}{\phi}}}{1 - \eta \left(1 - \psi\right) N_{t}^{1 + \frac{1}{\phi}}} \frac{\theta_{w,t}}{\theta_{w,t} - 1}$$

$$\widetilde{J}_{t}^{1 - \psi} = (1 - \beta) \left(\widetilde{C}_{t} - h\widetilde{C}_{t-1}\right)^{1 - \psi} \left(1 - \eta \left(1 - \psi\right) N_{t}^{1 + \frac{1}{\phi}}\right)^{\psi} + \beta \kappa^{1 - \psi} \widetilde{D}_{t}^{\frac{1 - \psi}{1 - \gamma}}$$

$$Q_{t,t+1} = \beta \left(\frac{\kappa \widetilde{D}_{t}^{\frac{1}{1 - \gamma}}}{\widetilde{J}_{t+1}}\right)^{\gamma - \psi} \left(\frac{\widetilde{C}_{t+1} - h\widetilde{C}_{t}}{\widetilde{C}_{t} - h\widetilde{C}_{t-1}}\right)^{-\psi} \left(\frac{1 - \eta \left(1 - \psi\right) N_{t+1}^{1 + \frac{1}{\phi}}}{1 - \eta \left(1 - \psi\right) N_{t}^{1 + \frac{1}{\phi}}}\right)^{\psi} \frac{1}{\Xi_{t+1}^{\gamma}} \frac{1}{\Pi_{t+1}}$$

$$(\theta - 1) \widetilde{Y}_{t} = -\zeta \left(\Pi_{t} - (\Pi_{t}^{*})^{1 - \iota} \Pi_{t-1}^{\iota}\right) \widetilde{Y}_{t} \Pi_{t} + \frac{\theta}{\alpha} \frac{\widetilde{w}_{t}}{P_{t}} \left(\frac{\widetilde{Y}_{t}}{Z_{t}}\right)^{\frac{1}{\alpha}} + \dots$$

$$+ \operatorname{E}_{t} Q_{t,t+1} \zeta \left(\Pi_{t+1} - (\Pi_{t+1}^{*})^{1 - \iota} \Pi_{t}^{\iota}\right) \widetilde{Y}_{t+1} \Xi_{t+1} \Pi_{t+1}$$

\mathbf{E} Elasticity of intertemporal substitution

We compute the elasticity of intertemporal substitution of consumption as the elasticity of consumption to a change in the real interest rate holding labour supply constant.

Define the "consumption surplus" $\stackrel{\longleftrightarrow}{c}_t \equiv \widetilde{C}_t - h\widetilde{C}_{t-1}$. The first order approximation to the nominal stochastic discount factor

$$Q_{t,t+1} = \beta \left(\frac{\kappa \widetilde{D}_{t}^{\frac{1}{1-\gamma}}}{\widetilde{J}_{t+1}}\right)^{\gamma-\psi} \left(\frac{\overleftarrow{c}_{t+1}}{\overleftarrow{c}_{t}}\right)^{-\psi} \left(\frac{1 - \eta \left(1 - \psi\right) N_{t+1}^{1 + \frac{1}{\phi}}}{1 - \eta \left(1 - \psi\right) N_{t}^{1 + \frac{1}{\phi}}}\right)^{\psi} \frac{1}{\Xi_{t+1}^{\gamma}} \frac{1}{\Pi_{t+1}}$$

can be written as 13

$$\widehat{q}_{t,t+1} = -\psi \Delta \widehat{\overrightarrow{c}}_{t+1} - \psi \left(1 + \frac{1}{\phi} \right) \frac{\overline{n}}{1 - \overline{n}} \Delta \widehat{N}_{t+1} - \psi \widehat{\xi}_{t+1} - \widehat{\pi}_{t+1} - (\gamma - \psi) \left(\widehat{\xi}_{t+1} + \widehat{\widetilde{j}}_{t+1} - \operatorname{E}_t \left[\widehat{\xi}_{t+1} + \widehat{\widetilde{j}}_{t+1} \right] \right)$$

where

$$\widehat{\widetilde{j}}_t + \widehat{\xi}_t = \sum_{i=0}^{\infty} \left(\beta \Xi^{1-\psi} \right)^i E_t \left[\widehat{\xi}_{t+i} + \left(1 - \beta \Xi^{1-\psi} \right) \left(\stackrel{\longleftrightarrow}{c}_{t+i} - \frac{\psi}{1-\psi} \left(1 + \frac{1}{\phi} \right) \frac{\overline{n}}{1-\overline{n}} \widehat{N}_{t+i} \right) \right]$$

As a result,

$$\widehat{q}_{t,t+1} = -\psi \Delta \stackrel{\widehat{\leftarrow}}{c}_{t+1} - \psi \left(1 + \frac{1}{\phi} \right) \frac{\overline{n}}{1 - \overline{n}} \Delta \widehat{N}_{t+1} - \psi \widehat{\xi}_{t+1} - \widehat{\pi}_{t+1}$$

and the real rate is

$$\widehat{r}_t = \psi \mathbf{E}_t \Delta \widehat{c}_{t+1} + \psi \left(1 + \frac{1}{\phi} \right) \frac{\overline{n}}{1 - \overline{n}} \mathbf{E}_t \Delta \widehat{N}_{t+1} + \psi \mathbf{E}_t \widehat{\xi}_{t+1}$$

Rearranging terms

$$\widehat{\overrightarrow{c}}_t = -\frac{1}{\psi}\widehat{r}_t + \mathbf{E}_t\widehat{\overrightarrow{c}}_{t+1} + \frac{1}{\psi}\left(1 + \frac{1}{\phi}\right)\frac{\overline{n}}{1 - \overline{n}}\mathbf{E}_t\Delta\widehat{N}_{t+1} + \mathbf{E}_t\widehat{\xi}_{t+1}$$

so that the long-run elasticity of substitution \overline{EIS} , i.e. the elasticity which is obtained after households have adjusted their consumption habits, takes the usual value

$$\overline{EIS} = \frac{1}{\psi}$$

Note that, in the absence of habits, this expression boils down to the usual value $1/\psi$.

To compute the short-run elasticity, we rewrite the consumption surplus in terms of the underlying consumption levels to obtain

$$\widehat{\widetilde{c}}_t = -\frac{1}{\psi} \frac{1-h}{1+h} \widehat{r}_t + \frac{1}{1+h} \operatorname{E}_t \widehat{\widetilde{c}}_{t+1} + \frac{h}{1+h} \widehat{\widetilde{c}}_{t-1} + \frac{1-h}{1+h} \left(1 + \frac{1}{\phi}\right) \frac{\overline{n}}{1-\overline{n}} \operatorname{E}_t \Delta \widehat{N}_{t+1} + \frac{1-h}{1+h} \operatorname{E}_t \widehat{\xi}_{t+1}$$

The short-run elasticity of substitution EIS is therefore

$$EIS = \frac{1}{\psi} \frac{1-h}{1+h}$$

which again boils down to $1/\psi$ when h=0. Note that, since h>0, it is always the case that $EIS < \overline{EIS}$.

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Table 1(a): Structural parameter estimates

	post mean	post sd	prior mean	prior sd
$p_{G,11}$	0.875997	0.055635	0.899727	0.065687
$p_{G,00}$	0.941294	0.035121	0.899437	0.066248
$p_{\eta,11}$	0.959538	0.019619	0.899591	0.065683
$p_{\eta,00}$	0.907894	0.044664	0.899823	0.065774
$p_{z,11}$	0.972819	0.009089	0.901282	0.065122
$p_{z,00}$	0.931666	0.019045	0.899314	0.066243
$\sigma_{G,1}$	0.003269	0.002076	0.002144	0.0008
$\sigma_{G,0}$	0.031624	0.003721	0.003929	0.002788
$\sigma_{\eta,1}$	0.001279	0.000131	0.002135	0.000788
$\sigma_{\eta,0}$	0.003882	0.000538	0.00391	0.002723
$\sigma_{z,1}$	0.010891	0.002059	0.002152	0.000801
$\sigma_{z,0}$	0.02705	0.004998	0.003945	0.002854
σ_{μ}	0.17681	0.021744	0.003056	0.002584
σ_{ξ}	0.006191	0.000326	0.00119	0.0005
$ ho_{\mu}$	0.548747	0.058116	0.855175	0.091594
$ ho_z$	0.988924	0.001815	0.858245	0.089933
$ ho_G$	0.909108	0.029819	0.855938	0.090583
Π	1.006143	0.00069	1.006255	0.00072
ψ_π	0.267607	0.024073	0.199031	0.10011
$\psi_{m{y}}$	0.049662	0.007535	0.02004	0.009968
$ ho_i$	0.913538	0.016879	0.849432	0.10022
Ξ	1.004527	0.000413	1.005008	0.001003
ι	0.733358	0.111614	0.500288	0.189923
ϕ	0.615584	0.084646	1.002252	0.504916
γ	11.51852	3.674717	10.95369	6.972984
ψ	1.307529	0.086758	1.203535	0.28997
ζ	33.80709	3.134418	14.97439	6.981933
h	0.861861	0.026101	0.499611	0.188565
β	0.998395	0.000567	0.998567	0.001429

Table 1(b): Measurement errors

	post mean	post sd	prior mean	prior sd
$\sigma_{me,\pi}$	1.4E-06	1.6E-06	1.4E-06	1.3E-06
$\sigma_{me,\Delta c}$	1.3E-06	6.8E-07	1.4E-06	1.1E-06
$\sigma_{me,\Delta y}$	0.003607	0.000617	0.000505	0.00027
$\sigma_{me,i}$	1.3E-06	7.5E-07	1.4E-06	1.0E-06
$\sigma_{me,i_{12}}$	0.00072	7.6E-05	0.001378	0.001037
$\sigma_{me,i40}$	0.000437	5.0E-05	0.001381	0.000999

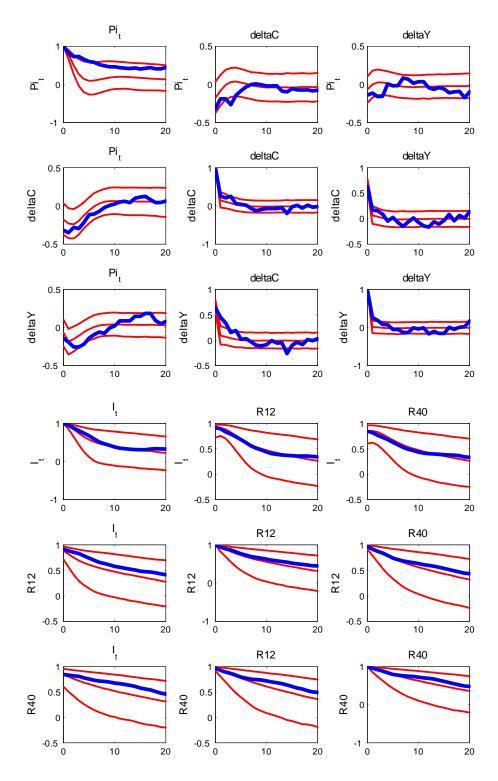
Legend: "sd" denotes the standard deviation; "low q" and "up q" denote the 5th and 95th percentiles of the distribution. Priors: beta distribution for β , h, ι , ζ , ρ_{ξ} , ρ_{g} , ρ_{π} ; gamma distribution for ψ_{π} , ψ_{y} and all standard deviations; shifted gamma distribution (domain from 1 to ∞) for γ , ϕ , Ξ , Π^{*} ; normal distribution for ρ_{i} . Posterior distributions are based on 50,000 draws.

Table 2: Variance decomposition

MS G 3.00 2.16 0.73 0.22 11.15 8.99 3.47 1.21 MS mpol 0.11 0.06 0.03 0.01 0.58 0.34 0.19 0.07 MS zi 0.82 15.97 37.33 53.98 0.62 13.80 36.30 53.31 G 0.03 0.03 0.01 0.00 0.13 0.11 0.05 0.02 mpol 0.04 0.02 0.01 0.00 0.13 0.11 0.05 0.02 mu 1.09 0.50 0.25 0.08 7.07 3.58 1.82 0.68 xi 0.01 0.01 0.00 0.00 0.06 0.04 0.02 0.01 meas err 14.12 3.56 1.09 0.35 17.01 4.74 1.69 0.62 i.c. 4.47 1.31 0.35 0.07 5.56 1.44 0.26 0.06 MS G 3.84 11.08 7.12 3.11 1.82 1.14 3.03 1.91 MS mpol 49.60 14.73 6.48 2.93 13.38 18.80 13.37 8.75 MS zi 0.05 3.02 23.79 45.82 0.15 5.43 18.29 33.15 G 0.04 0.13 0.10 0.05 0.02 0.01 0.04 0.03 mpol 16.54 5.18 2.47 1.17 4.46 6.50 5.08 3.49 z 4.21 25.40 39.90 37.41 14.45 23.78 22.04 26.47 mu 18.17 37.29 19.20 9.13 63.92 41.35 36.42 25.13 xi 4.95 1.55 0.74 0.35 1.34 1.95 1.52 1.04 meas err 0.00 0.00 0.00 0.00 0.00 0.00 0.00 i.c. 2.60 1.62 0.20 0.04 MS g 0.06 0.62 0.71 0.81 0.79 0.17 0.21 0.26 0.27 z 0.02 1.84 3.42 3.39 0.01 0.54 1.11 1.14 mu 0.70 4.13 5.48 5.48 0.19 1.22 1.78 1.84 xi 96.60 89.83 84.36 82.32 41.54 42.25 43.66 44.01 meas err 0.00 0.00 0.00 0.00 0.00 0.62 0.47 0.00 i.c. 0.08 0.11 0.04 0.00 0.62 0.47 0.02 0.00 i.c. 0.08 0.11 0.04 0.00 0.62 0.47 0.00 0.00 i.c. 0.08 0.11 0.04 0.00 0.62 0.47 0.00 0.00 i.c. 0.08 0.11 0.04 0.00 0.62 0.47 0.00 0.00 i.c. 0.08 0.11 0.04 0.00 0.62 0.47 0.00 0.00 i.c. 0.08 0.11 0.04 0.00 0.62 0.47 0.00 0.00 i.c. 0.08 0.11 0.04 0.00 0.06 0.62 0.47 0.00 i.c. 0.08 0.11	i40	1q	4q	12q	40q	i12	1q	4q	12q	40q
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mpol 16.54 5.18 2.47 1.17 4.46 6.50 5.08 3.49 z 4.21 25.40 39.90 37.41 14.45 23.78 22.04 26.47 mu 18.17 37.29 19.20 9.13 63.92 41.35 36.42 25.13 xi 4.95 1.55 0.74 0.35 1.34 1.95 1.52 1.04 meas err 0.00 0.67 MS zi 0.00 0.62 0.24 2.42 0.47 0.50 0.53 <										
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xi 4.95 1.55 0.74 0.35 1.34 1.95 1.52 1.04 meas err 0.00	Z	4.21	25.40	39.90	37.41		14.45	23.78	22.04	26.47
meas err 0.00 0.60 0.69 0.67 MS zi 0.00 0.21 2.59 4.81 0.00 0.06 0.84 1.62 G 0.00 0.01 0.02 0.02 0.47 0.50 0.53 0.54 mpol 0.62 0.71 0.81 0.79 0.17 0.21 0.26 0.27 z 0.02 1.84 3.42 3.39 0.01 0.54 1.11 1.14 mu 0.70 4.13 5.48 5.48 0.19 1.22 1.78 1.84 xi 96.60 89.83 84.36	mu	18.17	37.29	19.20	9.13		63.92	41.35	36.42	25.13
i.c. 2.60 1.62 0.20 0.04 0.46 1.04 0.20 0.03 Δc MS G 0.13 1.15 1.16 1.21 41.41 38.80 35.23 33.93 MS mpol 1.86 2.01 2.13 1.98 0.50 0.60 0.69 0.67 MS zi 0.00 0.21 2.59 4.81 0.00 0.06 0.84 1.62 G 0.00 0.01 0.02 0.02 0.47 0.50 0.53 0.54 mpol 0.62 0.71 0.81 0.79 0.17 0.21 0.26 0.27 z 0.02 1.84 3.42 3.39 0.01 0.54 1.11 1.14 mu 0.70 4.13 5.48 5.48 0.19 1.22 1.78 1.84 xi 96.60 89.83 84.36 82.32 41.54 42.25 43.66 44.01 meas err <td>xi</td> <td>4.95</td> <td>1.55</td> <td>0.74</td> <td>0.35</td> <td></td> <td>1.34</td> <td>1.95</td> <td>1.52</td> <td>1.04</td>	xi	4.95	1.55	0.74	0.35		1.34	1.95	1.52	1.04
Δc Δy MS G 0.13 1.15 1.16 1.21 41.41 38.80 35.23 33.93 MS mpol 1.86 2.01 2.13 1.98 0.50 0.60 0.69 0.67 MS zi 0.00 0.21 2.59 4.81 0.00 0.06 0.84 1.62 G 0.00 0.01 0.02 0.02 0.47 0.50 0.53 0.54 mpol 0.62 0.71 0.81 0.79 0.17 0.21 0.26 0.27 z 0.02 1.84 3.42 3.39 0.01 0.54 1.11 1.14 mu 0.70 4.13 5.48 5.48 0.19 1.22 1.78 1.84 xi 96.60 89.83 84.36 82.32 41.54 42.25 43.66 44.01 meas err 0.00 0.00 0.00 15.10 15.35 15.86 15.99	meas err	0.00	0.00	0.00	0.00		0.00	0.00	0.00	0.00
MS G 0.13 1.15 1.16 1.21 41.41 38.80 35.23 33.93 MS mpol 1.86 2.01 2.13 1.98 0.50 0.60 0.69 0.67 MS zi 0.00 0.21 2.59 4.81 0.00 0.06 0.84 1.62 G 0.00 0.01 0.02 0.02 0.47 0.50 0.53 0.54 mpol 0.62 0.71 0.81 0.79 0.17 0.21 0.26 0.27 z 0.02 1.84 3.42 3.39 0.01 0.54 1.11 1.14 mu 0.70 4.13 5.48 5.48 0.19 1.22 1.78 1.84 xi 96.60 89.83 84.36 82.32 41.54 42.25 43.66 44.01 meas err 0.00 0.00 0.00 0.00 15.10 15.35 15.86 15.99	i.c.	2.60	1.62	0.20	0.04		0.46	1.04	0.20	0.03
MS G 0.13 1.15 1.16 1.21 41.41 38.80 35.23 33.93 MS mpol 1.86 2.01 2.13 1.98 0.50 0.60 0.69 0.67 MS zi 0.00 0.21 2.59 4.81 0.00 0.06 0.84 1.62 G 0.00 0.01 0.02 0.02 0.47 0.50 0.53 0.54 mpol 0.62 0.71 0.81 0.79 0.17 0.21 0.26 0.27 z 0.02 1.84 3.42 3.39 0.01 0.54 1.11 1.14 mu 0.70 4.13 5.48 5.48 0.19 1.22 1.78 1.84 xi 96.60 89.83 84.36 82.32 41.54 42.25 43.66 44.01 meas err 0.00 0.00 0.00 0.00 15.10 15.35 15.86 15.99		Λc				Λv				
MS mpol 1.86 2.01 2.13 1.98 0.50 0.60 0.69 0.67 MS zi 0.00 0.21 2.59 4.81 0.00 0.06 0.84 1.62 G 0.00 0.01 0.02 0.02 0.47 0.50 0.53 0.54 mpol 0.62 0.71 0.81 0.79 0.17 0.21 0.26 0.27 z 0.02 1.84 3.42 3.39 0.01 0.54 1.11 1.14 mu 0.70 4.13 5.48 5.48 0.19 1.22 1.78 1.84 xi 96.60 89.83 84.36 82.32 41.54 42.25 43.66 44.01 meas err 0.00 0.00 0.00 0.00 15.10 15.35 15.86 15.99			1.15	1.16	1.21	<u></u> ;	41.41	38.80	35.23	33.93
MS zi 0.00 0.21 2.59 4.81 0.00 0.06 0.84 1.62 G 0.00 0.01 0.02 0.02 0.47 0.50 0.53 0.54 mpol 0.62 0.71 0.81 0.79 0.17 0.21 0.26 0.27 z 0.02 1.84 3.42 3.39 0.01 0.54 1.11 1.14 mu 0.70 4.13 5.48 5.48 0.19 1.22 1.78 1.84 xi 96.60 89.83 84.36 82.32 41.54 42.25 43.66 44.01 meas err 0.00 0.00 0.00 0.00 15.10 15.35 15.86 15.99										
mpol 0.62 0.71 0.81 0.79 0.17 0.21 0.26 0.27 z 0.02 1.84 3.42 3.39 0.01 0.54 1.11 1.14 mu 0.70 4.13 5.48 5.48 0.19 1.22 1.78 1.84 xi 96.60 89.83 84.36 82.32 41.54 42.25 43.66 44.01 meas err 0.00 0.00 0.00 15.10 15.35 15.86 15.99	•									
z 0.02 1.84 3.42 3.39 0.01 0.54 1.11 1.14 mu 0.70 4.13 5.48 5.48 0.19 1.22 1.78 1.84 xi 96.60 89.83 84.36 82.32 41.54 42.25 43.66 44.01 meas err 0.00 0.00 0.00 15.10 15.35 15.86 15.99	G	0.00	0.01	0.02	0.02		0.47	0.50	0.53	0.54
mu 0.70 4.13 5.48 5.48 0.19 1.22 1.78 1.84 xi 96.60 89.83 84.36 82.32 41.54 42.25 43.66 44.01 meas err 0.00 0.00 0.00 15.10 15.35 15.86 15.99	mpol	0.62		0.81			0.17	0.21	0.26	
xi 96.60 89.83 84.36 82.32 41.54 42.25 43.66 44.01 meas err 0.00 0.00 0.00 15.10 15.35 15.86 15.99	Z	0.02	1.84	3.42	3.39		0.01	0.54	1.11	1.14
meas err 0.00 0.00 0.00 0.00 15.10 15.35 15.86 15.99	mu	0.70	4.13	5.48	5.48		0.19	1.22	1.78	1.84
	xi		89.83	84.36	82.32		41.54	42.25		44.01
i.c. 0.08 0.11 0.04 0.00 0.62 0.47 0.02 0.00	meas err	0.00	0.00	0.00	0.00		15.10	15.35	15.86	15.99
	i.c.	0.08	0.11	0.04	0.00		0.62	0.47	0.02	0.00

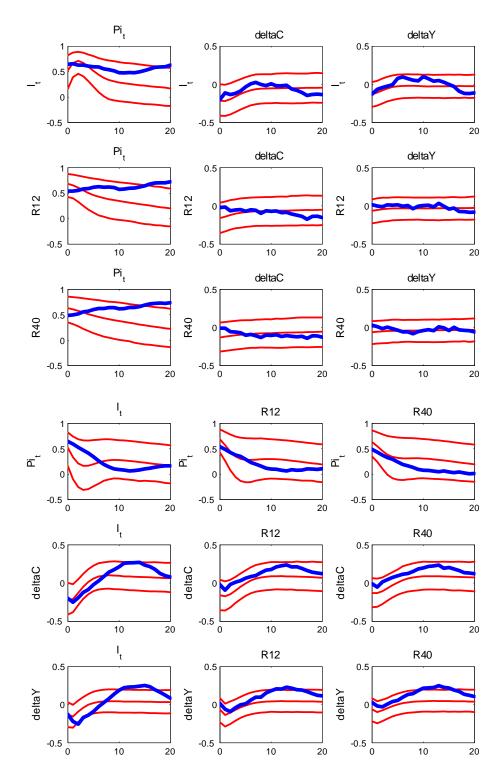
Legend: "i40" denotes the 10-year rate; "i12" is the 3-year rate; "i" is the short-term rate; " π " is the inflation rate; " Δc " denotes the rate of growth of consumption; " Δy " is the rate of growth of GDP. "i.c." is shorthand for initial condition. The variance decomposition is reported 1, 4, 12 and 40 quarters ahead.

Figure 2(a): Dynamic correlations



Note: the green lines display correlation coefficients from the data; the red lines report the mean and the 5th and 95th percentiles of the distribution across parameter draws of the theoretical correlation coefficients implied by the model.

Figure 2(b): Dynamic correlations



Note: the green lines display correlation coefficients from the data; the red lines report the mean and the 5th and 95th percentiles of the distribution across parameter draws of the theoretical correlation coefficients implied by the model.

Figure 3: Actual and model-implied 3-month forward rates

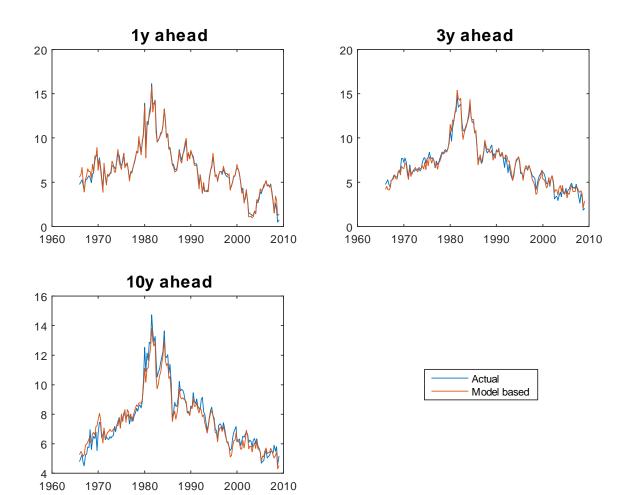


Figure 4: Actual and 1-step ahead forecasts

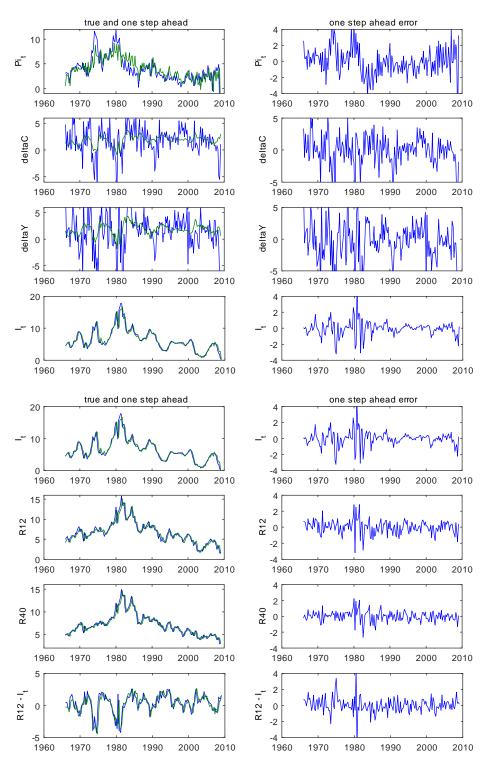
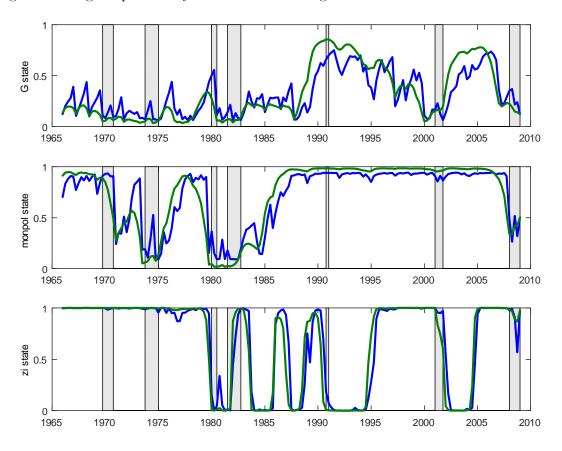
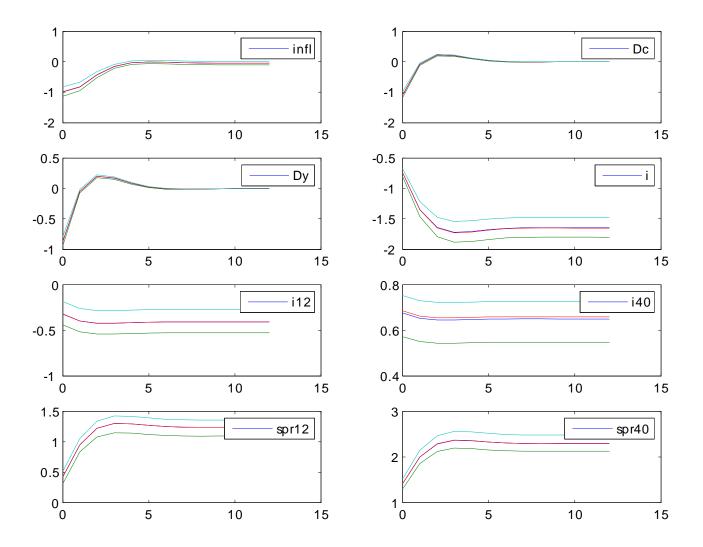


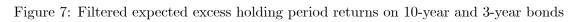
Figure 5: Marginal probability of a low-variance regime



Legend: filtered values in blue; smoothed values in green.

Figure 6: Impulse responses to an increase in the variance of technology shocks





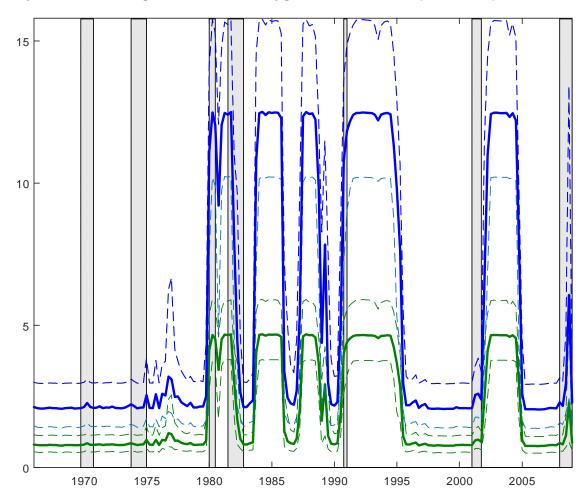


Figure 8: Long-term forward and expected interest rates and risk premia during the conundrum period

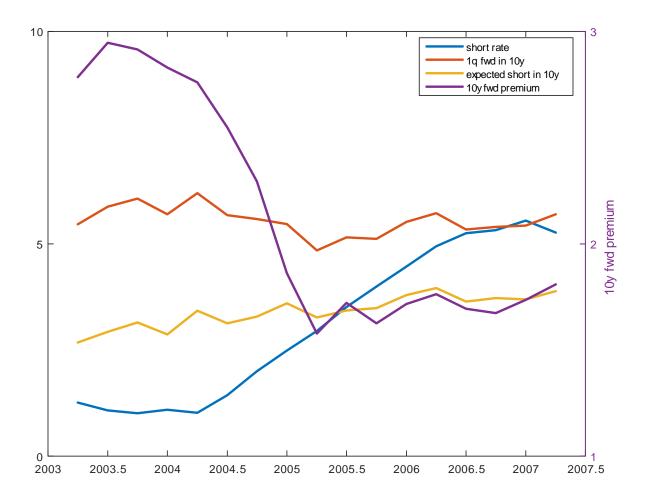
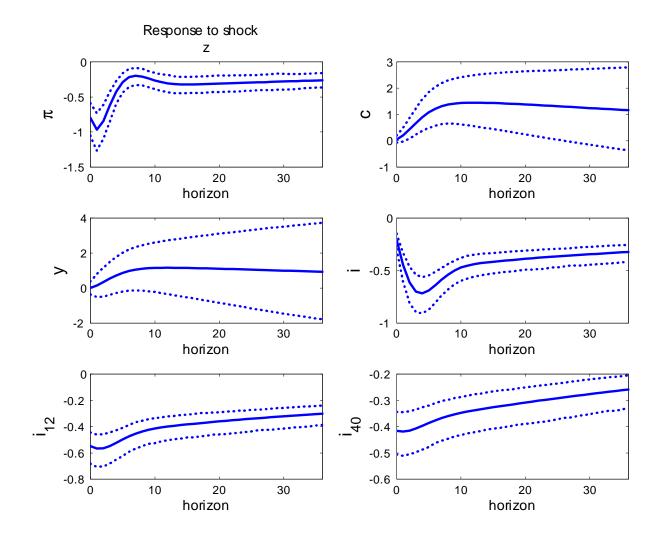


Figure 9: Impulse responses to a technology shock



Note: this impulse response is drawn abstracting from regime switches.

Figure 10: Survey and model-implied inflation expectations in the 1980s

