### Sectoral Credit Allocation, Capital Requirements and Financial Stability

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### Introduction

- Motivation
  - ▶ Not all credit booms are alike.
  - ▶ Rapid **credit growth** in **real estate** sectors associated with:
    - Higher probability of banking distress.
    - Lower future GDP growth. [Jorda, Shularick and Taylor, 2014; Muller and Verner, 2021].
  - ▶ Bank capital regulation (limit on bank leverage):
    - Mortgages individually **safer** than corporate non real estate loans  $\rightarrow$  existing regulation requires **less** bank capital per unit of loans (roughly 3.4% vs 6.7% in calibration period).

### • This paper:

- ► Study the **macroprudential** implications of the **microprudential** design of bank capital regulation.
- Assess the effectiveness of different regulatory designs at preventing and mitigating banking crises.
- ▶ Two sector DSGE model with structural credit risk and bank level distortions.

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### Preview of results

- Expansions in real estate credit are predictive of lower future GDP growth:
  - ▶ A 1 percentage point increase in the real estate credit to GDP ratio predicts lower future GDP growth (about 0.1%) after 4 years.
- **2** Policy analysis (assessment of regulatory tools):
  - Higher average levels of capital requirements (post GFC reforms) reduce the probability of banking crises roughly by half.
  - However, crises are characterized by sharper reallocation towards real estate credit and larger GDP losses.
  - Stabilizing effectiveness of countercyclical macroprudential buffers:
    - Generic countercyclical buffers only partially successful  $\rightarrow$  fail to prevent cross sector reallocation towards real estate.
    - Sector specific countercyclical buffers reduce cumulative output losses by three percentage points during crises episodes, while keeping the probability of distress low.

### Related Literature

• Literature on credit cycles: excessive credit expansion in real estate sector/non tradeable sectors. [Gorton and Ordonez, 2020; Asriyan, Laeven, Martin, 2022; Schmitt-Grohe and Uribe, 2018,...]

• This paper: Bank level distortions and capital regulation.

- Macro-banking papers with bank capital requirements [Malherbe (2020), Mendicino, Nicolov, Supera and Suarez (2018,2021),...]
  - ▶ This paper: Combine structural approach in credit risk and bank default with a multisectoral setup + Evaluation of sector specific capital buffers.
- Cyclical effects of risk based regulation [Repullo and Suarez, 2013; Andersen, 2013].
  - ► This paper: DSGE model, calibrated to Euro Area targets (quantification of effects).



### 1 Introduction

### 2 Model Overview







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### Dissecting the mechanism

- Competitive banks with **limited liability** and **insured deposit funding**.
- **Risk shifting incentives** in response to volatility of a **non diversifiable** driver of returns:
  - $\blacktriangleright$  Increase in non-diversifiable risk + no risk pricing of deposits  $\rightarrow$
  - $\blacktriangleright$  Risk taking profitable for banks  $\rightarrow$
  - **Expand** balance sheet as much as possible.
- Where can banks expand leverage the most?
  - ▶ Sector with **lower** capital requirements.
- Consequences:
  - Looser lending standards  $\rightarrow$  increase in borrower leverage.
  - Reallocation of credit towards sectors with low capital requirements (real estate) during episodes of increased volatility.
  - ▶ Amplification of small downturns in real estate markets, causing large losses (presence of bankruptcy costs + net worth channel).

### Model - Financial Flows



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### Risk layers

- Two layers of **cross sectional risk:** 
  - ▶ Borrower specific shocks: mean one **idiosyncratic shocks** to the terminal value of firm and household assets. Notation:  $\omega_f, \omega_h$ .
  - Non diversifiable island shock: mean one shock to all assets of class i in island j. Notation: ω<sup>j</sup><sub>f</sub>, ω<sup>j</sup><sub>h</sub>.

### • Time variation:

- ► Standard AR(1) aggregate productivity shocks.
- Shocks to the dispersion of  $\omega_f, \omega_h$ .

$$\log\left(\frac{\sigma_{s,t+1}}{\bar{\sigma}_s}\right) = \varrho_i \log\left(\frac{\sigma_{s,t}}{\bar{\sigma}_s}\right) + \varsigma_s \varepsilon_{s,t+1},\tag{1}$$

• Shock to the dispersion of  $\omega_f^j, \omega_h^j$ .

$$\log\left(\frac{\sigma_{s,t+1}^{j}}{\bar{\sigma}_{s}^{j}}\right) = \varrho_{s}^{j}\log\left(\frac{\sigma_{s,t}^{j}}{\bar{\sigma}_{s}^{j}}\right) + \varsigma_{s}^{j}\varepsilon_{t+1}, \qquad (2)$$

### **Financial Sector**

Banksspecialized in sector sDiversify across borrowersi in island j

Bank s balance sheet		
Loans $B_{s,t}$	$\begin{array}{ c c }\hline \text{Deposits } D_{s,t}\\ \hline \text{Equity } EQ^b_{s,t} \end{array}$	$\Pi_{t+1}^{b}(\omega_s^j) = \tilde{R}_{t+1}^{l}(\omega_s^j)B_{s,t} - R_{d,t}D_{s,t}$
$\phi_{s,t}B_{s,t}$	$\leq EQ^b_{s,t}$	

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### **Financial Sector**

• Bankers' returns:  $\Pi^b_{s,t+1} = \int_0^\infty \max[\Pi^b_{s,t+1}(\omega^j_s), 0] dF^j_{s,t+1}(\omega^j_s).$ 

• Participation constraint of banks:



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Higher (lower) capital charges  $\phi_{s,t}$  tighten (relax) the participation constraint in (3).

### Loan Contracts

- Borrowers (firms and households) decide on investment, consumption and borrowing taking into account the participation constraints of banks.
- Loan terms specify both a promised loan rate and the leverage of the borrower.



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### Calibration

- Calibration is done in two steps:
  - ▶ First step: pre-set parameters from the literature.
  - ▶ Second step: Internally calibrate parameters using SMM.
- Real and financial data from Euro Area in the period 2003:Q1-2013:Q4.
- Baseline calibration fits Basel II period.
- Model matches credit exuberance in the housing sector in the buildup of financial crises and the subsequent busts.

### Calibration of capital requirements

• Regulators set capital requirements following Basel Committee on Banking Supervision standards.

$$\phi_{s,t} = \eta \phi_{s,t-1} + (1-\eta) \phi_{s,t}^*, \tag{4}$$

where  $\eta$  is a smoothing parameter.

- Regimes
  - Basel I:  $\phi_{f,t}^* = 0.08, \ \phi_{h,t}^* = 0.04.$
  - Basel II:  $\dot{\phi}_{s,t}^* = IRB_s(PD_{s,t}).$
  - ▶ Basel III:  $\phi_{s,t}^* = M_{s,t} \times IRB_s(PD_{s,t})$ , where  $M_{s,t}$  is the impact of additional buffers (capital conservation and counter-cyclical buffers).

Details

### Calibration

Moment	Data	Model	Moment	Data	Model
Mean NFC Loans/GDP	1.785	2.046	Std. NFC Loans/GDP	0.128	0.237
Mean HH Loans/GDP	2.014	2.638	Std. HH Loans/GDP	0.053	0.059
Mean Spread NFC Loans	2.279	1.494	Std. Spread NFC Loans	0.493	0.907
Mean Spread HH Loans	1.331	0.5457	Std. Spread HH Loans	0.376	0.344
Mean write-off rate NFC Loans	0.543	0.584	Std. write-off NFC Loans	0.334	0.455
Mean write-off rate HH Loans	0.126	0.277	Std. write-off HH Loans	0.057	0.162
Mean Housing Wealth/ Total Non Financial wealth	0.947	0.633	Std. GDP	0.023	0.022
Mean ROE NFCs	4.706	4.223	Std. ROE NFCs	8.148	3.238
Mean ROE Banks	4.619	11.21	Std. ROE Banks	12.201	11.017
Mean Capital held by Households	0.185	0.153	Std. Investment/GDP	0.008	0.004
			Std. Housing prices	0.054	0.033

Table 2: Targeted Moments

Notes: This table displays the targeted moments in the calibration and their model counterparts. Spreads, write-off rates and returns on equity are reported in annualized percentage points. The standard deviation of GDP corresponds to the standard deviation of the log of GDP, in quarterly terms. All variables are linearly detrended before computing standard deviations.

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### Calibration

Parameter	Symbol	Value	Parameter	$\mathbf{Symbol}$	Value
New bankers' endowment	$\chi_b$	0.682	Std. Island risk (Firms)	$\varsigma_f^j$	0.055
New entrepreneurs' endowment	$\chi_f$	0.584	Std. Island risk (HH)	$\varsigma_h^j$	0.035
Housing equity	$\chi_h$	0.388	Std. Firm risk	Sf	0.075
Mean Island risk shock (Firms)	$\bar{\sigma}_{f}^{j}$	0.263	Std. HH risk	Sh	0.025
Mean Island risk shock (HH)	$\bar{\sigma}_{h}^{j}$	0.216	Std. productivity shocks	$\varsigma_A$	0.003
Mean Firm risk shocks	$\bar{\sigma}_f$	0.304	Pers. Island risk (Firms)	$\varrho_f^j$	0.705
Mean HH risk shocks	$\bar{\sigma}_h$	0.047	Pers. Island risk (HH)	$\varrho_h^{\hat{j}}$	0.705
Relative housing preference	$\lambda_h$	0.109	Pers. Firm risk	$\varrho_f$	0.906
HH backyard technology	$\alpha_{hh}$	0.1	Pers. HH risk	$\varrho_h$	0.926
Investment adjustment costs	$\psi$	1.99	Pers. Productivity	$\varrho_A$	0.98
			CR partial adjustment coefficient	$\eta$	0.9

#### Table 1: Internally calibrated parameters

• Model assigns higher (relative) importance of non diversifiable risk in the real estate sector.

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### Results

- Study **banking crises** episodes: Periods with gross deposit insurance outlays greater than 3% of GDP (Laeven and Valencia, 2013).
- Understand the role of capital regulation in the buildup and aftermath of crises.
- Characterization of banking crises (reallocation towards real estate lending).
- **2** Relevance of sector-specific capital buffers.
- **③** Probability of banking crises under different regimes.

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# Risk sensitive capital requirements and the path to crises



Notes: Solid lines correspond to the baseline model. Dashed lines correspond to a version of the model where capital charges are set to 6% and are equal across sectors. Sample paths correspond to shock realizations that generate banking crises in the baseline model.

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### Evaluation of an increase in levels of CRs (CCB)



Figure 4: Assessment of Uniform Increase in Capital Requirements

Notes: Solid lines correspond to the baseline model. Dashed lines correspond to capital requirements equal to 10.5% of risk weighted assets (introducing a 2.5% buffer as in the Capital Conservation Buffer of Basel III). Sample paths correspond to shock realizations that generate banking crises in each model

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Evaluation of CCyB rules

• Evaluate generic counter cyclical buffers

$$M_{s,t} = CCyB$$
(Total Credit/GDP gap at time t) (5)

• Sector specific buffers

 $M_{s,t} = CCyB(\text{Sector } s \text{ Credit/GDP gap at time t})$  (6)

• Parameters in this function are chosen to match existing Basel guidelines on the CCyB.

### Evaluation of CCyB rules (on top of CCB)



Figure 6: Evaluation of Basel III buffers

Notes: Solid lines correspond to Basel III levels of capital requirements. Red dashed lines correspond to a generic CCyB. Green dashed lines correspond to a sectoral CCyB. Sample paths correspond to shock realizations that generate banking crises in each model.

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### Comparison across regimes

Outcome Variable	Baseline	Basel III (extra	Generic	Sectoral
Outcome variable		2.5  pp buffer)	CCyB	CCyB
Frequency of Banking Crises	3.024	1.352	1.4229	1.35
Output Losses in Crises	-13	-14.3	-14.08	-11.28
Capital Charge (Firms)	6.68	8.81	8.99	9.08
Capital Charge (Households)	3.02	4.57	4.68	4.64
Default Rate Banks	1.04	0.96	0.96	0.96
Default Rate Firms	1.54	1.55	1.55	1.54
Default Rate Households	0.81	1	1.02	1.02
Welfare	_	0.055	0.01	0.085

Table 3: Comparison across Regulatory Designs

Notes: Output losses are reported in cumulative percentage points of GDP in the three years following a banking crisis. Welfare is reported as the percentage change in permanent consumption that would leave consumers as well off in the Baseline scenario as in each of the different regimes. Default rates are reported in annualized percentage points. Each column corresponds to simulations of the model for 500,000 periods, under each different regulatory regime.

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### Conclusion

- Increasing (just) the **level** of risk sensitive capital requirements (as in Basel III) decreases the probability of financial crises but leads to more severe real state boom and bust episodes ("scarcity" of bank capital).
- Sector specific countercyclical buffers can be effective macroprudential tools as they correct banks' incentives in the buildup of crises.
- The **reallocation** of credit towards real estate and the severity of crises can be **exacerbated by the microprudential design** of bank capital requirements.

## Thank you for your attention!

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# Appendix

### Dynasty

• Dynasty's utility function:

$$V_t = \mathbb{E}_t \sum_{s=t}^{\infty} \beta^{s-t} \left[ \log(C_s) + \lambda_h \log(H_s) - \lambda_L \frac{L_s^{1+\varphi}}{1+\varphi} \right], \quad (7)$$

where

- $C_t$ : consumption of the final good.
- $H_t$ : consumption of housing units.
- $L_t$ : labor supplied by the dynasty.
- $\beta$  is the subjective discount factor;  $\lambda_H$  measures preference for housing;  $\lambda_L$  measures the disutility of labor and  $\varphi$  is the Frisch elasticity of labor.

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### Dynasty

• Dynasty's budget constraint:

$$C_t + D_t + q_{k,t} K_{h,t} \le W_t - EQ_t^h, \tag{8}$$

where

$$W_t = w_t L_t + R_{d,t-1} D_{t-1} + q_{k,t} (1-\delta) K_{h,t-1} + K_{h,t-1}^{\alpha_h} + \Pi_t^h + \Upsilon_t$$
(9)

• Housing units financing constraint:

$$q_{h,t}H_t \le B_{h,t} + EQ_t^h,\tag{10}$$

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where  $EQ_t^h = \chi_h W_t$ .

 $D_t$ : bank deposits;  $R_{d,t}$ : gross rate on deposits;  $q_{k,t}$ : price of physical capital;  $K_{h,t-1}$ : physical capital directly held by the dynasty;  $\alpha_h$ : household backyard technology;  $q_{h,t}$ : price of housing units;  $\chi_h$ : housing equity as fraction of total wealth.  $\Upsilon_t$ : net transfers from entrepreneurs, bankers and producers of capital and housing units.

### Dynasty's problem and mortgage loans

- Housing purchases are chosen by the dynasty jointly with consumption and investment.
- Dynasty chooses  $H_t, B_{h,t}, R_{h,t}^l, C_t, L_t, K_{h,t}$  such that

$$(H_t, B_{h,t}, R_{h,t}^l, C_t, L_t, K_{h,t}) = \operatorname{argmax} V_t, \text{ s.t.}$$
(11)

$$C_t + D_t + q_{k,t} K_{h,t} \le W_t - EQ_t^h, \tag{12}$$

$$q_{h,t}H_t \le B_{h,t} + EQ_t^h,\tag{13}$$

and the real estate banks' participation constraint

$$\mathbb{E}_{t} \underbrace{\Lambda_{t+1}(1-\theta_{b}+\theta_{b}v_{t+1}^{b})}_{\text{Disc. factor bankers}} \underbrace{\Pi_{h,t+1}^{b}}_{\text{loan portfolios }h} \geq \phi_{h,t}B_{h,t} \underbrace{v_{t}^{b}}_{\text{bank equity}}.$$
(14)

### Housing payoffs

• Terminal housing net worth

$$\Pi_{t+1}^{h}(\omega_{h},\omega_{h}^{j}) = \omega_{h}\omega_{h}^{j}R_{h,t+1}q_{h,t}H_{t} - R_{h,t}^{l}B_{h,t}, \quad (15)$$
where  $R_{h,t+1} = \frac{q_{h,t+1}(1-\delta_{h})}{q_{h,t}}$ .
• Aggregate returns on housing

$$\Pi_{t+1}^{h} = \int_{0}^{\infty} \int_{0}^{\infty} \max\left[\Pi_{t+1}^{h}(\omega_{h}, \omega_{h}^{j}), 0\right] dF_{h, t+1}(\omega_{h}) dF_{h, t+1}^{j}(\omega_{h}^{j}),$$
(16)

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### Firms

• Firms produce the final consumption good according to

$$Y_{t+1} = A_{t+1} K_{f,t}^{\alpha} L_t^{1-\alpha}, \tag{17}$$

- Firms' financing constraint:  $q_{k,t}K_{f,t} + w_tL_t = B_{f,t} + EQ_{f,t}$
- The terminal net worth of a firm f in island j is given by

$$\Pi_{t+1}^{f}(\omega_{f},\omega_{f}^{j}) = \omega_{f}\omega_{f}^{j}\left[Y_{t+1} + q_{k,t+1}(1-\delta)K_{f,t}\right] - R_{f,t}^{l}B_{f,t}, \quad (18)$$

• Aggregate firm payoffs

$$\Pi_{t+1}^f = \int_0^\infty \int_0^\infty \max\left[\Pi_{t+1}^f(\omega_f, \omega_f^j), 0\right] dF_{f,t+1}(\omega_f) dF_{f,t+1}^j(\omega_f^j)$$

Entrepreneurs

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### Firms' problem and Corporate loans

• Corporate loans: choose  $K_t, L_t, B_{f,t}, R_{f,t}^l$  such that

$$(K_t, L_t, B_{f,t}, R_{f,t}^l) = \operatorname{argmax} \mathbb{E}_t \underbrace{\Lambda_{t+1}(1 - \theta_f + \theta_f v_{t+1}^f)}_{\text{Disc. factor}} \Pi_{t+1}^f, \text{ s.t.}$$
(19)

$$q_{k,t}K_t + w_t L_t \le B_{f,t} + EQ_{f,t},\tag{20}$$

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and the banks' participation constraint



### Banks

- Specialized island-sector bank subsidiaries.
- Issue equity and fully insured deposits.
- Invest in diversified portfolio of loans.
- Capital requirements  $\phi_{s,t}$  (binding in equilibrium).
- Bank *i* payoffs

$$\Pi^{b}_{s,t+1}(\omega^{j}_{s}) = \tilde{R}^{l}_{s,t+1}(\omega^{j}_{s})B_{s,t} - R_{d,t}D_{s,t}, \qquad (22)$$

• Aggregate banks payoff (diversification across islands)

$$\Pi^{b}_{s,t+1} = \int_{0}^{\infty} \max\left[\Pi^{b}_{s,t+1}(\omega^{j}_{s}), 0\right] dF^{j}_{s,t+1}(\omega^{j}_{s}),$$
(23)

Bankers 🔪 Return on loan

### Bankers

- Bankers manage their wealth and invest it in corporate and mortgage banks.
- They exit with probability  $1 \theta_b$ .
- When exiting, they rebate their terminal net worth  $n_{b,t+1}$  to the dynasty.
- Value function of individual banker

$$V_{t+1}^{b}(n_{t}^{b}(i)) = \max_{\operatorname{div}_{t}^{b}(i), EQ_{h,t}^{b}(i)} \left\{ \operatorname{div}_{t}^{b}(i) + \mathbb{E}_{t}\Lambda_{t+1} \left[ (1-\theta_{b})n_{t+1}^{b}(i) + \theta_{b}V_{t+1}^{b}(n_{t+1}^{b}(i)) \right] \right\},$$
  
$$EQ_{f,t}^{b}(i), n_{t+1}^{b}(i)$$

s.t. 
$$\operatorname{div}_{t}^{b}(i) + EQ_{h,t}^{b}(i) + EQ_{f,t}^{b}(i) = n_{t}^{b}(i),$$
 (25)

$$n_{t+1}^{b}(i) = \rho_{h,t+1}^{b} E Q_{h,t}^{b}(i) + \rho_{f,t+1}^{b} E Q_{f,t}^{b}(i), \qquad (26)$$
  
$$\operatorname{div}^{b}(i) > 0 \qquad (27)$$

$$\operatorname{div}_t^b(i) \ge 0, \tag{27}$$

### Bankers II

• Gertler and Kiyotaki (2010)  $\rightarrow$  value function linear in net worth +

$$v_t^b n_t^b = \max_{\operatorname{div}_t^b, EQ_{f,t}^b, EQ_{h,t}^b} \{ \operatorname{div}_t^b + \mathbb{E}_t \underbrace{\Lambda_{t+1} \left[ (1 - \theta_b) + \theta_b v_{t+1}^b \right]}_{\text{Stoch. disc.}} n_{t+1}^b \} (28)$$

- As long as  $v_{t+1}^b > 1$ , we have  $\operatorname{div}_t^b = 0$ .
- No arbitrage type condition:  $\mathbb{E}_t \Lambda_{t+1}^b \rho_{f,t+1}^b = \mathbb{E}_t \Lambda_{t+1}^b \rho_{h,t+1}^b$ .
- Shadow value of bankers' net worth  $v_t^b = \mathbb{E}_t \Lambda_{t+1}^b \rho_{f,t+1}^b = \mathbb{E}_t \Lambda_{t+1}^b \rho_{h,t+1}^b$

### Entrepreneurs

- Entrepreneurs manage their wealth and invest it in firms.
- They exit with probability  $1 \theta_f$ .
- When exiting, they rebate their terminal net worth  $n_{f,t+1}$  to the dynasty.
- Value function of individual entrepreneur

$$V_{t}^{f}(n_{t}^{f}(i)) = \max \underset{\substack{n_{t+1}^{f}(i), \\ n_{t+1}^{f}(i), EQ_{t}^{f}(i)}{\operatorname{div}_{t}^{f}(i) + \mathbb{E}_{t}\Lambda_{t+1}\left[(1-\theta_{f})n_{t+1}^{f}(i) + \theta_{f}V_{t+1}^{f}(n_{t+1}^{f}(i))\right]\right\}$$

(29)

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s.t. 
$$\operatorname{div}_{t}^{f}(i) + EQ_{t}^{f}(i) = n_{t}^{f}(i),$$
 (30)

$$n_{t+1}^f(i) = \rho_{t+1}^f E Q_t^f(i), \tag{31}$$

$$\operatorname{div}_t^f(i) \ge 0 \tag{32}$$

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with 
$$\rho_{t+1}^f \equiv \frac{\Pi_{t+1}^f}{EQ_{t+1}^f}$$
.  
Back to firms

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### Entrepreneurs II

• Gertler and Kiyotaki (2010)  $\rightarrow$  value function linear in net worth then

$$v_t^f n_t^f = \max_{\operatorname{div}_t^f, EQ_t^f} \{ \operatorname{div}_t^f + \mathbb{E}_t \underbrace{\Lambda_{t+1} \left[ (1 - \theta_f) + \theta_f v_{t+1}^f \right]}_{\text{Stoch. disc.}} \rho_{t+1}^f n_t^f \} \quad (33)$$

As long as v<sup>f</sup><sub>t+1</sub> > 1, we have div<sup>f</sup><sub>t</sub> = 0.
Shadow value of entrepreneurial equity v<sup>f</sup><sub>t+1</sub> = E<sub>t</sub>Λ<sup>f</sup><sub>t+1</sub>ρ<sup>f</sup><sub>t+1</sub>.

### Laws of motion

• Law of motion of aggregate bankers' net worth

$$N_{t+1}^{b} = \left[\theta_{b} + (1 - \theta_{b})\chi_{b}\right] \left[\rho_{f,t+1}^{b} E Q_{f,t}^{b} + \rho_{h,t+1}^{b} E Q_{h,t}^{b}\right] - T_{t}, \quad (34)$$

where  $T_t$  are taxes levied by the prudential authority.

• Law of motion of aggregate entrepreneurial net worth

$$N_{t+1}^{f} = [\theta_f + (1 - \theta_f)\chi_f]\rho_{t+1}^{f} E Q_t^{f}.$$
(35)

• Capital and housing stock

$$X_{t+1} = S\left(\frac{I_{x,t}}{X_t}\right)X_t + (1-\delta_x)X_t,\tag{36}$$

with 
$$X = K, H$$
 and  $S\left(\frac{I_{x,t}}{X_t}\right) = \frac{a_1}{1 - 1/\psi} (I_{x,t}/X_t)^{1 - 1/\psi} + a_2$ 

### Market clearing

- Bankers' net worth:  $N_t^b = EQ_{f,t}^b + EQ_{h,t}^b$
- Entrepreneurs' net worth:  $N_t^f = EQ_t^f$
- Capital:  $K_t = K_{f,t} + K_{h,t}$ .
- Final consumption good  $Y_t = C_t + I_{k,t} + I_{h,t} + \Sigma_{f,t} + \Sigma_{h,t} + \Sigma_{b,t}$ , where  $\Sigma_{s,t}$  are bankruptcy costs associated to firms, households and banks.
- Deposits:  $D_t = D_{f,t} + D_{h,t}$ .

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### Realized return on loans

• Realized return on mortgage loans

$$\tilde{R}_{h,t+1}^{l}(\omega_{j_{h}})B_{h,t} \equiv R_{h,t}^{l}B_{h,t} \left[1 - F_{h,t+1}(\bar{\omega}_{h,t+1}(\omega_{h}^{j}))\right] + (1 - \mu_{h})\omega_{h}^{j}R_{h,t+1}q_{h,t}H_{t} \int_{0}^{\bar{\omega}_{h,t+1}(\omega_{h}^{j})} \omega_{h}dF_{h,t+1}(\omega_{h}), \quad (37)$$

• Realized return on corporate loans

$$\tilde{R}_{f,t+1}^{l}(\omega_{f}^{j})B_{f,t} \equiv R_{f,t}^{l}B_{f,t} \left[1 - F_{f,t+1}(\bar{\omega}_{f,t+1}(\omega_{f}^{j}))\right] + (1 - \mu_{f})\omega_{f}^{j} \left[Y_{t+1} + q_{t+1}(1 - \delta)K_{f,t}\right] \int_{0}^{\bar{\omega}_{f,t+1}(\omega_{f}^{j})} \omega_{f} dF_{f,t+1}(\omega_{f}),$$
(38)

Back to banks

EL OQO

### IRB formulas

$$IRB_{s,t} = LGD_s \left[ \Phi \left( \frac{\Phi^{-1} \left( PD_{s,t} \right) + \sqrt{\zeta_{s,t}} \Phi^{-1}(0.999)}{\sqrt{1 - \zeta_{s,t}}} \right) - PD_{s,t} \right], \quad (39)$$

where  $LGD_s$  is the loss given default;  $PD_{s,t}$  is the IRB default probability, and  $\zeta_{s,t}$  is the portfolio correlation coefficient of each class of loans.

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### Role of differences in non-diversifiable risk



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Figure 2: Role of non-diversifiable risk

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### Basel III buffers



Figure 6: Evaluation of Basel III buffers

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### Basel III (CCB only)

Figure 4: Assessment of Uniform Increase in Capital Requirements



Notes: Solid lines correspond to the baseline model. Dashed lines correspond to capital requirements equal to 10.5% of risk weighted assets (introducing a 2.5% buffer as in the Capital Conservation Buffer of Basel III). Sample paths correspond to shock realizations that generate banking crises in each model

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### Sector-specific credit growth and GDP growth

Figure 1: Responses of GDP growth to innovations in Credit to GDP ratios



Notes: Impulse responses of GDP growth over a horizon k years ahead, to innovations in credit to GDP ratios (in levels, not percent) in each sector, computed using local projections estimates of  $\Delta_k GDP_{t+k} = \sum_{j=0}^{J} \beta_{k,j}^{k} \Delta b_{h,t-j} + \sum_{j=0}^{J} \beta_{j,j}^{k} \Delta b_{h,t-j} + \sum_{j=0}^{$ 

- Expansions in residential real estate loans predictive of lower future GDP growth.
- Consistent with empirical evidence in e.g. Muller and Verner (2021).

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### Shocks leading to crises

Figure 5: Shocks leading to a crisis in baseline vs higher levels of capital requirements



Notes: Solid lines correspond to the baseline model. Dashed lines correspond to capital requirements equal to 10.5% of risk weighted assets (introducing a 2.5% buffer as in the Capital Conservation Buffer of Basel III). Sample paths correspond to shock realizations that generate banking crises in each model.

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### Real Estate Credit growth, GDP growth and CRs

Figure 8: Responses of GDP growth to innovations in Credit to GDP ratios



Note: Impulse responses of GDP growth over a horizon of k years ahead, to innovations in the ratio of real estate credit to GDP in different regulatory regimes regimes, computed using local projections estimates of  $\Delta_k GDP_{t+k} = \sum_{j=0}^{k} \beta_{k,j}^{k} \Delta_{b,t-j} + \sum_{j=0}^{j} \beta$ 

- Sector specific buffers help breaking the connection between real estate credit growth and negative future GDP growth.
- Achieved by correcting bank risk shifting incentives + building buffers (also achieved under generic CCyB).