OPTIMAL EXCHANGE RATE TARGETS AND MACROECONOMIC STABILIZATION

Enrique Alberola Ila

OPTIMAL EXCHANGE RATE TARGETS AND MACROECONOMIC STABILIZATION

Enrique Alberola Ila (*)

(*) The author acknowledges the comments of Michael Artis, Andrew Hughes Haelet, Mark Salmon, Berthold Herrendorf, Juanjo Dolado, José Ramón Martínez Resano and participants in seminars at University Pompeu Fabra, the EEA Congress in Prag and the Bank of Spain. Help from Trini Casasús is especially appreciated. The usual disclaimer applies.

> Banco de España - Servicio de Estudios Documento de Trabajo nº 9615

In publishing this series the Banco de España seeks to disseminate studies of interest that will help acquaint readers better with the Spanish economy.

The analyses, opinions and findings of these papers represent the views of their authors; they are not necessarily those of the Banco de España.

> ISSN: 0213-2710 ISBN: 84-7793-488-6 Depósito legal: M. 20869-1996 Imprenta del Banco de España

Abstract

Exchange rate targets in a stabilization game are considered. The targeting strategy consists on the choice of a desired level for the exchange and the weight assigned to such target in the loss function. The exchange rate target appears then as an intermediate objective and acts as a surrogate to policy coordination. The targeting solution reveals that the targeting strategy can be embedded on a straight line in the policy-instruments space (the respective money supplies), which greatly facilitates the analysis. It turns out that the targeting strategy is optimal when the reaction of the countries exert a positive externality on the other country. In this case, policymakers have some flexibility in the choice of the target as long as the optimal commitment to such target is selected accordingly.

Introduction

This article deals with the design of exchange rate targets and their use as stabilizing devices in the face of economic shocks. The exchange rate plays in our framework a role of intermediate target, acting as an instrument for implicit cooperation. Countries agree on the exchange rate target and -conditional upon it- maximise (non-cooperatively) their individual loss function.

Incentive compatibility turns out to be the necessary condition to render credible the arrangement, otherwhise private agents would realise the incentive to renege that a return to a non-cooperative equilibrium provides. Pareto optimality is a complementary condition which maximises the quality of the arrangement and, in our reference model, delivers the explicit coordination solution.

After presenting the model and the targeting framework in the first two sections, the search for an optimal targeting strategy is developed in two stages. In the first stage (section III), we explore the <u>possibility</u> of targeting the exchange rate for different types of shocks. This is formally done by delimiting the type of shocks for which the exchange rate arrangement is incentive compatible and Pareto optimal. It turns out that the feasibility of targeting the exchange rate depends on the type of shock and that it may be counterproductive in certain circumstances.

The second stage (section IV) directly tackles the question of <u>designing</u> optimal exchange rate targets within the relevant shock subset. We will observe that there is some scope for the discretion for the policymakers who can choose between a wide range of exchange rate targets, provided that they also choose the optimal commitment to the selected target. Section V interprets the results and the conclusions sum up our results and compares them with other targeting schemes.

I-Model and definitions

We consider two identical and interdependent economies (home and foreign countries,

labelled with subscripts 1,2). The policy makers aim at minimising their respective loss functions (L_1, L_2) which penalise the deviations of employment (n) and consumer prices (q) from their desired levels, which we assume, without loss of generality, that are set to zero:

$$L_{1} = \frac{1}{2} [\sigma n_{1}^{2} + \eta q_{1}^{2}]$$

$$L_{2} = \frac{1}{2} [\sigma n_{2}^{2} + \eta q_{2}^{2}]$$

$$\sigma > 0, \ \eta > 0$$
[1]

The instrument for the policy makers is the money supply $[m_1, m_2]$. The characteristics of the economy are defined by the model developed in Canzoneri & Henderson (1988,91), which is summed up in appendix A.

At the beginning of the game, workers and firms enter into wage contracts which specify nominal wages and employment. Firms employ labour up to the point that real wages equal the marginal product of labour. Workers agree to supply whatever quantity of labour firms want at the nominal wages specified in the contracts. The result is that nominal wages are set so that the expected employments are at their full-employment levels of zero. Since, as it is shown in appendix B, the expected money supplies equal zero, the employment level in each country is determined by the respective money supply surprises (m_1, m_2) .

After contracts are set, these economies may suffer shocks on the demand (u_1, u_2) or the supply side (x_1, x_2) . Consumer prices and the real exchange rate z are affected by these shocks, as it can be observed in the reduced forms of the model:

$$n_{1}=m_{1} \; ; \quad n_{2}=m_{2}$$

$$q_{1}=(\sqrt{\eta})^{-1}[m_{1}-2\theta m_{2}+(1-\tau)x_{1}+\tau x_{2}-(u_{1}-u_{2})]$$

$$q_{2}=(\sqrt{\eta})^{-1}[m_{2}-2\theta m_{1}+(1-\tau)x_{2}+\tau x_{1}+(u_{1}-u_{2})]$$

$$z=(\zeta\sqrt{\eta})^{-1}[2\theta(m_{1}-m_{2})-\tau(x_{1}-x_{2})-(u_{1}-u_{1})]$$

$$0<\theta<\frac{1}{2}; \; 0<\tau<\frac{1}{2}; \; 0<(\sqrt{\eta})^{-1}<1; \; \zeta<\frac{1}{2}$$

For instance, a negative symmetric supply shock $(x_1=x_2>0)$, due for instance to a commodity shock, will increase domestic and foreign consumer prices, because it reduces labour

productivity in both countries and wages are already set; the real exchange rate remains at the same level though. The case of a demand shock is less intuitive in this model. A shift in demand from country two to country one $(u_1-u_2>0)$ does not modify nominal incomes, but it creates an excess demand on country one and an excess supply in country two. The currency of the excess demand country must appreciate in real terms (z>0) to eliminate the imbalance. This reduces consumer prices at home and increases them abroad.

Consequently, shocks lead to a welfare loss which can be observed in figures one and two. The welfare loss just after the shock, that is, before any reaction of the authorities, corresponds to the origin The quadratic loss function defines elliptical indiference curves in the instrument space $[m_1, m_2]$. Policy makers will make then use of monetary policy to minimise welfare losses, offseting the effects of the shocks on the domestic consumer prices. In particular, for the supply shock we are considering both countries would contract their money supplies to reduce the consumer price inflation; in the case of a shift in demand, the foreign country would contract its money supply, while the home country would expand. This policy action has a cost, however in terms of employment. Furthermore, the effects of the monetary action will spillover to the other country and this is taken into account by both policymakers.

At this point, the outcome of the game depends on the strategic position of the countries¹. If countries do cooperate, they would use their money supplies to minimise the joint loss function given by:

$$L^{c} = \delta L_{1} + (1-\delta)L_{2}$$

where δ , l- δ are the weights assigned to each country. An Pareto optimal outcome is obtained for each value δ , which are embedded in the contract curve $(C(\delta))$. Setting $\delta = l$, $(\delta = 0)$, the instruments of both countries are chosen to maximise the welfare of the first (second) country. These solutions are known as bliss points (B_1, B_2) . Since the bliss points correspond to zero welfare losses, B_1, B_2 are placed at the center of the ellipses.

When countries act non-cooperatively, each country takes the actions of the other player as given and try to minimise their own welfare loss, for each possible choice of the second country.

¹-The following solutions are derived in appendix C.

This set of outcomes is contained in the reaction function for each country (R_1^N, R_2^N) . The Nash or non-cooperative equilibrium (N) is given by the intersection of these reaction functions.

We can observe in the figures that the outcomes are in this case inefficient: there are other solutions which would be welfare-improving for both countries. This set of incentive compatible points is called the bargaining area, labelled A in the figures. It is delimited by the ellipses intersecting at the Nash equilibria and it obviously includes a segment of the contract curve.

II-The exchange rate as intermediate target

While both countries would gain from cooperation, this solution faces a "cheating problem" (Canzoneri & Gray (1985)), because monetary cooperative arrangements are difficult to verify and they are easily altered in subtle ways.

Our strategy attempts to overcome this problem, emphasising the value of exchange rate targets as adequate surrogates for explicit cooperation because of its direct observability. In this sense, Kenen (1989,p.54) notes that "governments are prone to cheat and will not engage in optimal coordination because they cannot trust each other. A government cannot cheat on a firm commitment to exchange rate pegging without being caught. Therefore, exchange rate pegging is viewed as a viable alternative to full-fledged coordination". Notwithstanding this, in the policy coordination literature, the choice of the exchange rate usually appears as a by-product of the coordination solution and it is not explicitly considered. We follow here Hughes Hallet et. al (1989) and, in particular, Hughes Hallet (1993) where exchange rate targets are included in the policymakers' optimization problem. We can justify this inclusion more formally using an analogy with the optimal contract literature, adapted to the context of policy coordination².

Two countries on an equal strategic footing decide to commit to a contract in order to minimise the welfare losses derived from unanticipated shocks. Of course, they will only stick to the contract if they expect to gain from it, hence the need for the arrangement to be incentive compatible. Reneging on the arrangement opens up the possibility of retaliation by the second

²-See Rogoff (1985) and, for more recent developments, Baron (1989), Walsh (1995) and Persson & Tabellini (1993).

country and the suspension of an agreement which is in general benefitial for both countries. This punishment strategy is assumed to eliminate the incentive to renege, so that the time inconsistency problem does not arise and the game can be considered as static. Finally, we have to specify the content of the contract, denoted by V. The contract is defined in terms of deviations from the desired real exchange rate (z^d) , which enters in the loss function of both countries with a weight equal to β : $V = \frac{12}{3}\beta(z-z^d)^2$

Thus, the function which each country considers is then modified to become:

$$W_1 = L_1 + V$$
; $W_2 = L_2 + V$

Note that the exchange rate is just an intermediate target in the modified loss functions (W_1, W_2) . The values of β and z^d should be chosen so as to induce the optimal response of policymakers to attain their final goals: consumer prices and employment stability.

Following Rogoff (1985) we can define the parameter or weight β as the optimal degree of commitment to the intermediate target, in this case the desired real exchange rate. The parameter β is constrained to be positive, otherwise what is being targeted is the exchange rate to avoid!. When β equals zero, no constraint is imposed on the exchange rate and the result corresponds to the non-cooperative free-float solution³. The second element to determine is the choice of the exchange rate target (z^d). How do players agree on the desired level for the real exchange rate? We take as benchmarks the Exchange Rate Mechanism (ERM) of the EMS-a nominal exchange rate target- and the target zone proposed by Williamson (1985)- a real exchange rate target, and allow for a continuum of exchange rate targets, spanning between both alternatives. This setup allows for flexibility in the design of the contract, adding new insights to the question of exchange rate targeting.

Let us take the real exchange rate identity, in terms of purchasing power parity:

$$z=e-(p_1-p_2)$$

where p_i is the price of goods in the respective country and the nominal exchange rate e, is

³-Since positive values of β penalize deviations from the desired values, it represents a soft band of fluctuation for the desired exchange rate target; the larger the value of β , the narrower will be the implied band. This specification allows us to think of the targeting strategy as a target zone with soft bands, where z^d represents the central parity.

defined as the price of country 2 currency in terms of country 1 currency. The ERM regime aims at maintaining a fixed nominal exchange rate parity, i.e. $e^d = 0$, which is equivalent to a real exchange rate target equal to the negative of price differentials: $z^d = -(p_1 - p_2)$. The Williamson target zone on the contrary implies a desired value for the real exchange rate equal to zero $z^d = 0$ or, equivalently, a depreciation of the nominal exchange rate to completely offset price differentials, that is, $e^d = (p_1 - p_2)$.

Let us now define the parameter ρ , such that $e^d = (l-\rho)(p_1-p_2)$, where $(l-\rho)$ is then the offsetting degree of price differentials. Thus, we can write the exchange rate target in general form as a function of the price differentials

$$z^{d} = e^{d} - (p_1 - p_2) = -\rho(p_1 - p_2)$$

It immediately follows that $\rho = I$ corresponds to a nominal exchange rate target, and $\rho = 0$ corresponds to a real exchange rate target. The intermediate values present special interest because they will provide flexibility in the choice of exchange rate target, according to the preferences of policymakers.

We can observe that the design of the targeting strategy is then determined by the choice of just two parameters: ρ and β . The range of parameters is constrained to positive values of β and to values of ρ between zero and one, i.e. between real and nominal exchange rate targets. The combination of exchange rate targets and values for β represents the set of targeting strategies (λ):

$$\lambda = \{ [\beta X \rho], \forall \beta \ge 0, 0 \le \rho \le 1 \}$$

which, for latter convenience, can be seen as a a subset of $\Lambda = \{ \beta X \rho \}, \forall \beta, \rho \}$

Since, as mentioned above, the exchange rate arrangement must be incentive compatible, the choice of ρ and β must deliver an equilibrium laying inside the bargaining area A in the figures. Moreover, it would be desirable that the targeting strategy places the economies on the contract curve of Pareto optimal outcomes. Now we are in the position to explore whether targeting the exchange rate pays when countries are placed on an equal strategic footing.

III-Economic shocks and optimal targets

The introduction of an exchange rate target in the optimization problem implies that the

exchange rate target acts as an indirect cooperation device. It is indirect because the optimization problem facing each country is equivalent to the non-cooperative case; each country minimises its own welfare loss, taking as given the actions of the foreign country, but also taking into account the common exchange rate target, that is, the respective money supplies are chosen so as to minimise W_1, W_2 .

We focus in this section on the set Λ , with no constraint on the target parameters⁴. Each combination of β and ρ defines a targeting equilibrium where the modified reaction functions $R_I(\Lambda), R_2(\Lambda)$ intersect. We define this set of solutions in the instrument space: $T(\Lambda) = \{m_I^T, m_2^T\}$; when $\beta = 0$, $\forall \rho$, the exchange rate is not targeted, corresponding to the Nash non-cooperative solution $N = T(0) = \{m_I^N, m_2^N\}$. It turns out that $T(\Lambda)$ is a straight line (target line, hereafter), passing through the Nash equilibrium. More formally, in appendix D we firstly show that:

<u>Proposition 1</u>: The set of targeting equilibria, $T(\Lambda)$, is contained in a straight line with slope equal to -1 in the $[m_1, m_2]$ space, where:

$$T(\Lambda):\{(m_1^T, m_2^T) \mid m_2^T = -\frac{x_1 + x_2}{1 + \sigma - 2\theta} - m_1^T\}$$
 [3]

This proposition is central to the derivation of our results. On the one hand, recall that incentive compatible strategies must be Pareto superior to the Nash solution, that is, the target line must pass through the bargaining area. On the other hand, it would be desirable that the targeting strategy is Pareto optimal. This requirements lead to the following conditions for an optimal exchange rate arrangement, where incentive compatibility is the necessary condition:

INCENTIVE COMPATIBILITY:
$$\exists \Lambda \mid T(\Lambda) \cap A \neq \{\emptyset\}$$

PARETO OPTIMALITY: $\exists \Lambda, \delta \mid T(\Lambda) = C(\delta)$

Now we will explore the feasibility of optimal targets, applying these two optimality conditions to the shocks arising on the demand and on the supply side; note however that the figures advance the conclusions of our formal analysis below for certain types of shocks.

⁴-Therefore, strictly speaking the propositions below are necessary but not sufficient conditions for targeting the exchange rate appropriately. Only when the value of of the targeting parameters are specified, the propositions will be completed. In the next section we will focus in more detail on the conditions for which β is positive when ρ is between zero and one.

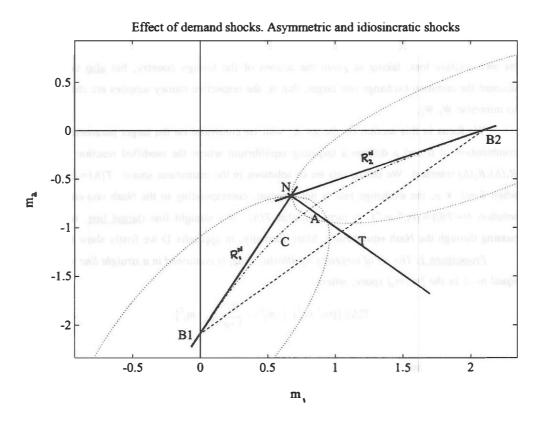


Figure 1 - Strategic behaviour and demand shocks

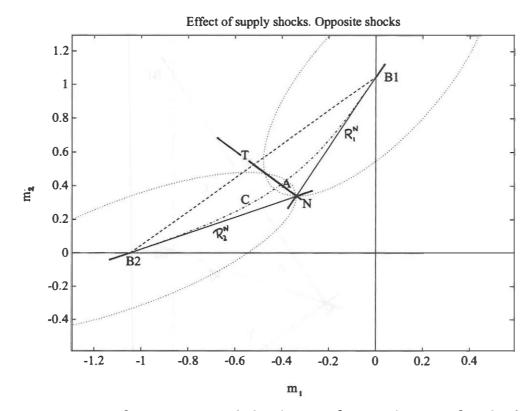


Figure 2.a-Strategic behaviour and opposite supply shocks

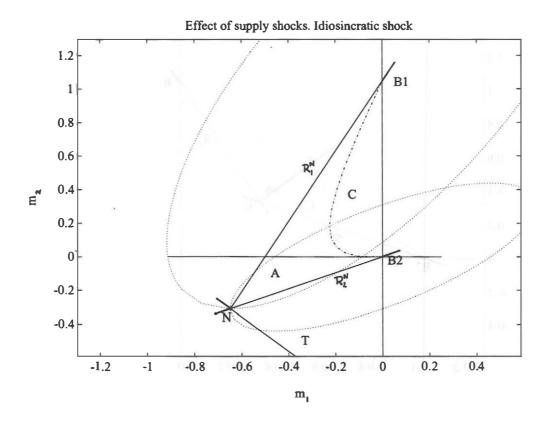


Figure 2.b-Strategic behaviour and idiosyncratic supply shocks

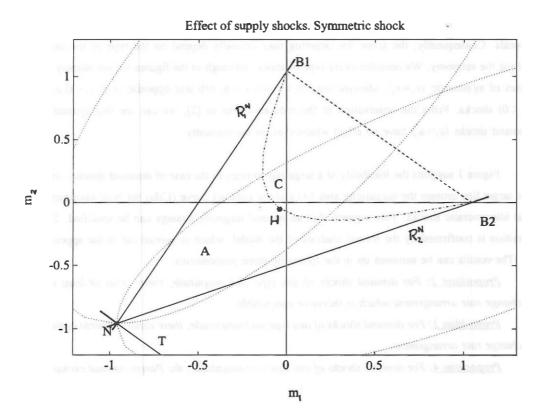


Figure 2.c-Strategic behaviour and symmetric supply shocks

Supply and demand shocks have different effects on welfare as an inspection of [1,2] reveals. Consequently, the scope for targeting may crucially depend on the type of the shock hitting the economy. We consider every type of shock, although in the figures we just display the cases of symmetric $(x_1=x_2)$, idiosyncratic $(x_1>x_2=0,u_1>u_2=0)$ and opposite $(x_1=-x_2<0,u_1=u_2<0)$ shocks. From the observation of the reduced forms in [2], we can see that symmetric demand shocks $(u_1=u_2)$ have no effect whatsoever on the economy.

Figure 1 suggests the feasibility of a targeting strategy in the case of **demand shocks**, since the target line crosses the bargaining area (A) and the contract curve $(C(\delta))$ for both asymmetric and idiosyncratic shocks. This suggests that an optimal targeting strategy can be specified. This intuition is confirmed by the formal analysis of the model, which is carried out in the appendix D. The results can be summed up in the following three propositions:

<u>Proposition 2</u>: For demand shocks of any type and magnitude, there exists at least one exchange rate arrangement which is incentive compatible.

<u>Proposition 3</u>: For demand shocks of any type and magnitude, there exists a Pareto optimal exchange rate arrangement.

<u>Proposition 4</u>: For demand shocks of any type and magnitude, the Pareto optimal exchange rate arrangement is incentive compatible and corresponds to the point C(½), where

$$C(\frac{1}{2}) = \{m_1^*, m_2^*\} \in T(\Lambda)$$

$$m_1^* = \frac{(1+2\theta)(u_1 - u_2)}{[\sigma + (1+2\theta)^2]} = -m_2^*$$
[4]

Therefore, it is formally shown that the targeting equilibrium which intersects the contract curve belongs to the bargaining area, so that the Pareto optimal equilibrium is also incentive compatible, hence making optimal targets feasible for any type of demand shock.

The question is not so straightforward in the case of supply shocks. The plots in figure 2.a-c display a quite different picture: only in the case of opposite supply shocks, the target line crosses A and $C(\delta)$. As above, the results are formalised in three propositions:

<u>Proposition 5</u>: For supply shocks at least one incentive compatible exchange rate target will exists if

$$-\frac{(1+\sigma)-(1+\sigma-2\theta)\tau}{2\theta+(1+\sigma-2\theta)\tau}x_{i} \le x_{j} \le -\frac{2\theta+(1+\sigma-2\theta)\tau}{(1+\sigma)-(1+\sigma-2\theta)\tau}x_{i}, \ \forall x_{i} > 0 \ \{i,j\} = \{1,2\}, i \ne j$$

Proposition 6: For supply shocks there exists an optimal exchange rate target only if

$$-\frac{(1+\sigma)-(1+\sigma-2\theta)\tau}{2\theta+(1+\sigma-2\theta)\tau}x_i\leq x_j\leq -\frac{2\theta+(1+\sigma-2\theta)\tau}{(1+\sigma)-(1+\sigma-2\theta)\tau}x_i,\ \forall x_i>0\ \{i,j\}=\{1,2\}, i\neq j$$

Noting in [2] that the parameters θ and τ are positive and less than $\frac{1}{2}$ and σ is positive, it follows that

$$-\frac{(1+\sigma)-(1+\sigma-2\theta)\tau}{2\theta+(1+\sigma-2\theta)\tau} < -1 < -\frac{2\theta+(1+\sigma-2\theta)\tau}{(1+\sigma)-(1+\sigma-2\theta)\tau} < 0$$

This result supports the existence of optimal targets for opposite supply shocks but rules them out for symmetric and idiosyncratic supply shocks⁵. More precisely,

<u>Proposition 7</u>: For opposite supply shocks $(x_1 = -x_2)$, the Pareto optimal exchange rate arrangement is incentive compatible and corresponds to the point $C(\frac{1}{2})$:

$$\forall x_1 = -x_2 \Rightarrow C(\frac{1}{2}) = \{m_1^*, m_2^*\} \in T(\Lambda)$$

$$m_1^* = -\frac{(1+2\theta)(1-2\tau)x_1}{[\sigma+(1+2\theta)^2]} = -m_2^*$$
[5]

IV-The design of optimal targeting strategies

The feasibility of optimal targeting strategies has just been shown, but we have not yet constrained the target parameters to belong to the relevant targeting set $(\lambda \subset \Lambda)$, where β is positive and $0 \le \rho \le 1$. This constraint is now introduced, so that the issue of designing exchange

⁵- For the rest of supply shocks, we had to proceed by numerical simulation. The outcome depends on the values of σ and θ . In particular, for values close to the extremes of the range the Pareto optimal point does not fall within the bargaining area. In any case, for these latter situations, an exchange rate agreement could be reached because incentive compatibility is the sufficient condition.

rate targets can be tackled. We claim that

<u>Proposition 8</u>: When an optimal targeting strategy exists, the optimal degree of commitment β^* to an exchange rate target is a function of ρ and the parameters of the model, $\beta^* = f(\rho, .)$ and it follows that

$$\forall u_1 - u_2, \ \forall \rho \in [0, 1] \Rightarrow \beta^* > 0, \ \beta_{\rho}^* > 0$$

$$\forall x_1 = -x_2, \ \forall \rho > \frac{2\theta}{+2\theta + \frac{\sigma}{1 + 2\theta} - \zeta\sqrt{\eta}} > 0 \Rightarrow \beta^* > 0, \ \beta_{\rho}^* < 0$$

This result shows that the exchange rate target (and the optimal commitment to it) depends on the type of shock affecting the economy, but not on the magnitude or the sign of the shocks. This is a result which is also found in the existing policy coordination literature, and it greatly facilitates the design of the optimal targeting strategy.

Secondly, for demand shocks nominal and real exchange rates can be targeted, while for opposite supply shocks real exchange rate targets are ruled out $(\rho > 0)$ and, for certain parameter values, nominal exchange rate targets could be inadequate, too⁶.

The third conclusion of this section is that there is not an unique optimal design for the exchange rate target. It ultimately depends on the preferences of policy makers, who can choose between different combinations of commitment and exchange rate targets given the function $f(\rho, .)$. This trade-off is conveyed in β_{ρ} , the derivative of β^* with respect to ρ . If the policymaker's goal is to design a target zone which minimises exchange rate volatility relative to the desired target, the higher β^* , the better. On the contrary, if the aim is to provide exchange rate flexibility reaping the full benefits of coordination, the value of ρ which allows for the highest exchange rate flexibility will be chosen. According to this second criterion, a real exchange rate target would be the optimal choice in the case of demand shocks while for the case opposite supply shocks, a

⁶-We can observe in [5] that the optimal response to an opposite supply shock $(x_1=-x_2<0)$ requires a change of the opposite sign in the money supplies $(m_1=-m_2>0)$. From the expression of the real exchange rate in [2], this in turn implies further deviations from the <u>real</u> exchange rate target.

nominal peg would be the solution.

V-Interpretation of the results

The cases for which a targeting strategy is feasible have some features in common. Comparison of figure 1 (demand shocks) with figure 2.c (opposite supply shocks) actually reveals an equivalent outcome in graphical terms. Note that in both cases, the solution requires manipulation of the money supplies in different directions. This causes a positive externality because, from [2], both countries are moving the exchange rate in the same direction. It is in these cases when targeting the exchange rates pays. More formally:

<u>Proposition 9</u>: The necessary condition for the existence of an optimal exchange rate arrangement is that, for any type of shocks

$$sign(m_T^1) = sign(m_N^1) \neq sign(m_N^2) = sign(m_T^2)$$

Let us explain why an exchange rate target is optimal in the case of a shift in demand towards the home good $(u_1 - u_2 > 0)$. As we have mentioned above, the shift in demand provokes an exchange rate appreciation which reduces (increases) consumer prices at home (abroad). Consequently, the home (foreign) country will expand (contract) its money supply, but if countries do not cooperate, this individual effort to reverse the exchange rate appreciation derived from the shock is too cautious with respect to the optimal solution. In other words, a smaller deviation from the pre-shock zero exchange rate levels is required to attain an efficient equilibrium. Since including an additional target in the loss function has the effect of reducing the deviation of the new target from its desired level, targeting the real or nominal exchange rate in the loss function will induce the right response.

Note that this implies a more activist role for monetary policy derived from the targeting strategy. Comparing the expressions for the Nash solution (expression [VI] in the appendix) and the optimal targeting strategy for demand and opposite supply shocks (expressions [4] and [5] respectively), we can express the latter as a function of the Nash solution. It turns out that:

on a real target or vice-versa has not been shown. Indeed, we have proved that in certain cases (demand shocks) both are valid and in others neither of them is (a wide range of supply shocks).

The assumption of an identical strategic role for each country in the targeting strategy is central to our results. This is revealed when comparing them with the conclusions of Canzoneri and Henderson (1991), who use an identical model. In their case however an asymmetric targeting strategy is considered, where one country (the follower) pegs the exchange rate to the leader. The leader sets the value of its money supply to minimise its own welfare function and the follower only cares about maintaining the parity. This asymmetric strategy would pay in the case of symmetric supply shocks. In this case, as it is apparent in figure 2.a both countries non-cooperatively respond by changing their money supplies in the same direction, provoking an overshooting of the exchange rate with respect to the efficient solution. Therefore, the result of a leader-follower strategy is to offset this negative externality and place the economy on the point H, which is optimal.

In this case, the existence of a leader exerts a disciplinary effect on the actions of the follower because changes in the money supplies are smaller. Thus, when the optimal response to a shock requires a restraint or discipline in the management of the money supply a leader-follower strategy is desirable because the leader provides an anchor to the monetary policy. However, when countries act on an equal strategic basis no disciplinary effect can be attained. Therefore, the optimal contract strategy may only be beneficial when a more activist response is required. This implies that our alternative dominates for demand and opposite supply shocks.

All in all then the optimal arrangement depends on the type of shock hitting the economy, highlighting the case for flexibility in the design of exchange rate arrangements. In any case, it is the economic and not the political environment which should dictate the strategic environment.

$$|m_i^N| = \frac{(1-2\tau)x_i + u_i - u_j}{1+\sigma+2\theta} < |m_i^*| = \frac{(1+2\theta)(1+\sigma+2\theta)}{\sigma+(1+2\theta)^2} |m_i^N| < (1-2\tau)x_i + u_i - u_j$$

$$\{i,j\} = \{1,2\}, i \neq j$$

Therefore, the optimal strategy will always imply a larger change in the money supply, both for the expansionary and the deflationary country. This result is confirmed by the graphical analysis where we can observe that, in the relevant figures, the optimal solution is more distant from the origin than the Nash solution.

Finally, the slope of the target line being equal to -1 implies that the global money supply does not change when the solution shifts from the Nash to the targeting equilibrium. More formally, the expression for the target line in [3] reveals that at the targeting equilibrium the global money supply remains constant and equal to the Nash solution. For supply shocks $m_1+m_2=-(1-2\tau)(x_1+x_2)/(1+\sigma+2\theta)$ and for demand shocks the global money supply is simply zero, that is, the effect of the targeting strategy is to allocate more efficiently a given global money supply than in a non-cooperative situation, which reminds McKinnon's proposal for monetary stabilization (MacKinnon 1984,88).

VI-Conclusions. The need for flexibility

Welfare considerations should be the basis for any exchange rate arrangement among countries. Consequently, exchange rate targets which do not benefit to each participant cannot be sustained. Upon this idea we have set up a framework to analyse exchange rate targeting in the form of an optimal contract between countries which are on an equal strategic basis.

The exchange rate target is viewed as an intermediate objective on which policymakers agree (optimal contract). As intuition suggests, targeting the exchange rate in such a way may only be appropriate when both countries are interested in moving the exchange rate in the same direction. While for demand shocks of any type or magnitude an optimal target can be devised, for supply shocks the answer depends on their differential impact on each country.

The optimal contract, when feasible, allocates a fixed global money supply more efficiently than in a non-cooperative Nash situation. We have also identified a certain room for discretion in the choice of the exchange rate target but a general dominance of a nominal exchange rate target

Appendix

A. Model of Canzoneri & Henderson (1988, 1991)

Let us consider two economies (home and foreign, subscripts one and two, respectively) with identical structures, but for the good they produce (y_1, y_2) . These economies are subject to shocks on the demand (u_1, u_2) and the supply side (x_1, x_2) . Rational expectations are assumed, so that only unanticipated shocks can affect equilibrium. All the variables except the interest rates are expressed in logs and represent deviations of actual values from equilibrium. The disaggregation of shocks and the treatment of the exchange rates introduce some minor modifications into the original model.

The output of each country (y_i) is obtained through a Cobb-Douglas production function. It is an increasing function of domestic employment n_i and it decreases when some adverse supply shock x'_i , hits the economy¹:

$$y_1 = (1-\alpha)n_1 - x_1'$$
; $y_2 = (1-\alpha)n_2 - x_2'$

Firms hire labour up to the point in which real wages equal the marginal product of labour:

$$w_1 - p_1 = -\alpha n_1 - x'_1$$
; $w_2 - p_2 = -\alpha n_2 - x'_2$

where w_i and p_i are nominal wages and prices, respectively. Contracts are signed at the beginning of each period, so that shocks are unanticipated. These contracts specify nominal wages and employment rules and workers agree to supply whatever quantity of labour firms want at the nominal wage specified in the contracts.

Consumer price indexes q_i are weighted averages of domestic and foreign goods prices:

$$q_1 = (1-\zeta)p_1 + \zeta(e+p_2) = p_1 + \zeta z$$
; $q_2 = (1-\zeta)p_2 - \zeta(e-p_2) = p_2 - \zeta z$

The market equilibrium conditions for the demands of goods are:

$$y_1 = \delta z + (1 - \zeta) \varepsilon y_1 + \zeta \varepsilon y_2 - (1 - \zeta) \nu r_1 - \zeta \nu r_2 + u'_1$$

$$y_2 = -\delta z + \zeta \varepsilon y_1 + (1 - \zeta) \varepsilon y_2 - \zeta \nu r_1 - (1 - \zeta) \nu r_2 + u'_2$$

where r_i are the real interest rates and u_i are positive demand shocks. Uncovered interest parity holds, so that r_i - r_2 = z^e -z. The superscript stands for expected value. Finally, the equilibrium in the

¹-The parameters which appear in the model are all positive and take the following values: $\alpha < I$, capital coefficient in the production function. δ , real exchange rate elasticity, $\varepsilon < I$, marginal propensity to spend; $\delta < I$, demand elasticity to the real exchange rate; ν , interest rate elasticity; $\zeta < \frac{1}{2}$, share of import goods on domestic basket. The rest of parameters are combinations of these: $\gamma = [2\delta + (1-2\zeta)^2 \nu J^I < I; \pi = I - (I-2\zeta)\varepsilon < I; \tau = \zeta \gamma \pi < \frac{1}{2}; \phi = \tau(I-\alpha) < \frac{1}{2}; \sqrt{\eta} = (\alpha + \phi)^{-I} > I; \theta = \frac{1}{2}\sqrt{\eta}\phi < \frac{1}{2}.$

money market is given by the Cambridge equations: $m_1 = p_1 + y_1$; $m_2 = p_2 + y_2$.

Nominal wages are set as follows. From the output and the wages equations above, and using the money market equilibrium equations, employment can be expressed as a function of the money supplies and nominal wages: $n_1 = m_1 - w_1$; $n_2 = m_2 - w_2$. Firms and workers choose the nominal wage that minimizes the expected square deviations of employments from the full-employment value, set equal to zero. Optimizing the square of the expression above, we observe that the respective nominal wages are set equal to the expected money supplies:

$$\frac{\partial (n_1^2)^e}{\partial w_1} = w_1 - m_1^e = 0$$
; $\frac{\partial (n_2^2)^e}{\partial w_2} = w_2 - m_2^e = 0$

The reduced forms are obtained by expressing all the variables of interest in terms of the instruments and the shocks. It is shown below that the expected money supplies are zero. Taking this into account and redefining the shocks: $x_i = \sqrt{\eta x_i}'$ and $u_i = \sqrt{\eta \zeta \gamma u_i}'$, i = 1, 2., the reduced forms for the policy objectives are:

$$n_1 = m_1 \; ; \quad n_2 = m_2$$

$$q_1 = (\sqrt{\eta})^{-1} [m_1 - 2\theta m_2 + (1 - \tau)x_1 + \tau x_2 - (u_1 - u_2)]$$

$$q_2 = (\sqrt{\eta})^{-1} [m_2 - 2\theta m_1 + (1 - \tau)x_2 + \tau x_1 + (u_1 - u_2)]$$

and for the relevant exchange rates:

$$z = \pi \gamma (1 - \alpha) (m_1 - m_2) - (\zeta \sqrt{\eta})^{-1} [\tau(x_1 - x_2) + (u_1 - u_2)]$$

$$z^d = -\rho [\alpha (m_1 - m_2) + (\sqrt{\eta})^{-1} (x_1 - x_2)]$$

$$z - z^d = \sqrt{\rho'} [(m_1 - m_2) + (\sqrt{\eta})^{-1} [(\rho - \frac{\tau}{\xi})(x_1 - x_2) - \frac{u_1 - u_2}{\xi}]]$$

where $\sqrt{\rho'} = [\rho\alpha + \pi\gamma(1-\alpha)]$ and $\{i,j\} = \{1,2\}, i \neq j$.

B. Money supply expectations

Substituting the reduced forms in which expectations explicitly appear in the functions to optimize and taking the derivative with respect to the instruments, we obtain:

$$\frac{\partial W_{i}}{\partial m_{i}} = 0 \Rightarrow \sigma(m_{i} - m_{i}^{e}) + \eta(\phi + \alpha)(m + (\phi + \alpha - 1)[(m_{i} - m_{i}^{e}) - \phi(m_{j} - m_{j}^{e}) + (1 - \tau)x_{i}' + \tau x_{j}' - \zeta \gamma(u_{i}' - u_{j}')] + \theta\{\sqrt{\rho}'[(m_{1} - m_{2}) - (m_{1}^{e} - m_{2}^{e})] + (\rho - \frac{\tau}{\xi})(x_{1}' - x_{2}') - \gamma(u_{1}' - u_{2}')\} = 0$$

Taking expectations, and noting that $x_i^e = u_i^e = 0$, i = 1, 2, because they represent unanticipated shocks, it is straightforward to conclude that the expected money supplies equal zero. Setting $m_1^e = m_2^e = 0$ the reduced forms for the modified loss function are, for $\{i,j\} = \{1,2\}$, $i \neq j$:

$$\begin{split} W_i = & L_i + V = \frac{1}{2} \left\{ \sigma(m_i)^2 + [m_i - 2\theta m_j + (1 - \tau) x_i + \tau x_j - (u_i - u_j)]^2 + \right. \\ & + \beta [\sqrt{\rho'} (m_1 - m_2) + \frac{\rho - \tau/\zeta}{\eta} (x_1 - x_2) - \frac{1}{\zeta\sqrt{n}} (u_1 - u_2)]^2 \right\} \end{split}$$

C. Solutions to the model

The standard solutions are obtained setting $\beta=0$, such that $W^C=L^C$. The explicit cooperative solution is obtained by the minimization of the weighted joint loss function, $L^C=\delta L_1+(1-\delta)L_2$ where $\delta, I-\delta$ are the weights assigned to each country. The solutions are contained in the <u>contract curve</u> $(C(\delta))$ whose rate of marginal substitution is equal to minus one $dm_2/dm_1|_{dL=0}=-1$, so as to fulfill the condition of Pareto optimality:

$$C(\delta): \left\{ \begin{array}{l} m_{1}^{C}, m_{2}^{C} \mid \frac{\partial L^{C}}{\partial m_{1}^{C}} = -\frac{\partial L^{C}}{\partial m_{2}^{C}} \Rightarrow \\ \Rightarrow \Sigma_{1} m_{1} - 2\theta m_{2} + \delta [(1-\tau)x_{1} + \tau x_{2}] - (1-\delta)2\theta [(1-\tau)x_{2} + \tau x_{1}] - \\ -(\delta + (1-\delta)2\theta)(u_{1} - u_{2}) = \\ = -[\Sigma_{1} m_{2} - 2\theta m_{1} - \delta 2\theta [(1-\tau)x_{1} + \tau x_{2}] - (1-\delta)[(1-\tau)x_{2} + \tau x_{1}] + \\ +(\delta 2\theta + (1-\delta))(u_{1} - u_{2})] \right\}$$

$$where \quad \Sigma_{1} = \delta (1+\sigma) + (1-\delta)(2\theta)^{2}; \quad \Sigma_{2} = (1-\delta)(1+\sigma) + \delta(2\theta)^{2}$$

Setting $\delta = 1$, $(\delta = 0)$, the instruments of both countries are chosen to maximize the welfare of the first (second) country. These solutions are known as <u>bliss points</u> (B_1, B_2)

$$C(1) = B_1 \big\{_{b=1} = \{m_1^{B_1}, m_2^{B_1}\} = \{0, (2\theta)^{-1} [(1-\tau)x_1 + \tau x_2 - (u_1 - u_2)]\};$$

$$C(0), B_2 \big\}_{b=0} = \{m_1^{B_2}, m_2^{B_2}\} = \{(2\theta)^{-1} [(1-\tau)x_2 + \tau x_1 + (u_1 - u_2)], 0\}$$

Since the bliss points correspond to zero welfare losses, B_1 , B_2 are placed at the center of the ellipses. It is convenient to define the segment which joins the bliss points as the bliss line (B):

$$B: \{m_1, m_2 \subset [B_1 X B_2] \mid m_2 = (\frac{(1-\tau)x_1 + \tau x_2}{2\theta} - \frac{u_1 - u_2}{2\theta}) + bm_1\}$$

$$where \ b = -\frac{(1-\tau)x_1 + \tau x_2}{(1-\tau)x_2 + \tau x_1}, \forall x_i \neq 0; \ b = 1, \forall u_i \neq 0, i = 1, 2$$

Minimising each country loss function with respect to the respective instrument, and taken the action of the other country as given, we obtain the (modified) reaction functions:

$$\begin{split} \frac{\partial W_i}{\partial m_i} &= 0 \implies R_i(\Lambda) \colon \ m_i = \psi_1^{-1} \{ \psi_2 m_j - [(1-\tau) + (\rho - \frac{\tau}{\xi})] \psi_3 x_i + [(\rho - \frac{\tau}{\xi}) - \tau] \psi_3 x_j + \psi_4 (u_i - u_j) \} \\ where \quad \psi_1 &= 1 + \sigma + \beta \rho' \ ; \quad \psi_2 = 2\theta + \beta \rho' \ ; \quad \psi_3 = \frac{\beta \sqrt{\rho'}}{\sqrt{\eta}} \ ; \quad \psi_4 = 1 + \frac{\psi_3}{\xi} \ . \end{split}$$

The points where these modified reaction functions $(R_1(\Lambda), R_2(\Lambda))$ intersect represent the targeting solutions, $T(\Lambda) = \{m_1^T, m_2^T\}$:

$$m_{i}^{T} = -\frac{[\psi_{1}(1-\tau) + \psi_{2}\tau]x_{i} + [\psi_{1}\tau + \psi_{2}(1-\tau)]x_{j}}{\psi_{1}^{2} - \psi_{2}^{2}} + \frac{[(\rho - \tau/\xi)(\psi_{2} - \psi_{1})\psi_{3}](x_{i} - x_{j})}{\psi_{1}^{2} - \psi_{2}^{2}} + \frac{[\psi_{4}(\psi_{1} - \psi_{2})](u_{i} - u_{j})}{\psi_{1}^{2} - \psi_{2}^{2}}$$
[V]

The non-cooperative Nash solution is a particular case of the general targeting solution, when $\beta = 0$ and $R_1(\Lambda) = R_1^N$, $R_2(\Lambda)R_2^N$: $N = T(0) = \{m_1^N, m_2^N\}$. In this case, where $\psi_1 = 1 + \sigma$, $\psi_2 = 2\theta$, $\psi_3 = 0$, $\psi_4 = 1$, it is straightforward to see by direct substitution into [V] that²:

$$m_{i}^{N} = -\frac{[(1+\sigma)(1-\tau)+2\theta\tau]x_{i}+[2\theta(1-\tau)+(1+\sigma)\tau]x_{j}-(1+\sigma-2\theta)(u_{i}-u_{j})}{(1+\sigma)^{2}-(2\theta)^{2}}$$
[VI]

D. Proof to the propositions

<u>Proof to proposition 1 (Target line)</u>. The slope of $T(\Lambda)$ in the $[m_1, m_2]$ space is obtained by the cocient of the derivatives of the target solutions appearing in [V] with respect to Λ :

$$dm^{T}_{2}/dm^{T}_{i} = [\partial m^{T}_{2}/\partial \Lambda/[\partial m^{T}_{i}/\partial \Lambda]]$$

²- Canzoneri & Henderson (1991,pgs.21 and 37) only consider symmetric supply shocks $(x_1=x_2)$ and opposite demand shocks $(u_1/2=-u_2/2)$. Substituting in [3] we obtain the same expressions as theirs.

Now we will show that the partial derivatives are of different sign but equal value. Let us consider the different terms in equation [V]. When i=1, j=2 the last two terms in the expression, and consequently their partial derivatives, are equal and of opposite sign than when i=2, j=1, but the first term is different. Let us denote the respective <u>numerators</u> of this first term by Z_1, Z_2 and let us express x_2 in terms of $x_1, x_2=Kx_1, K \in \mathbb{R}$. Simplifying this expression we obtain

$$Z_1 = (a\Psi_1 + b\Psi_2)x_1; Z_2 = (b\Psi_1 + a\Psi_2)x_1$$

where $a=K+\tau(l-K)$, $b=l-\tau(l-K)$. Adding and substracting $a\psi_1x_1$ from Z_1 and $b\psi_2x_2$ from Z_2 , we obtain that

$$Z_1 = [a(\Psi_1 + \Psi_2) + c\Psi_2]x_1; Z_2 = [b(\Psi_1 + \Psi_2) - c\Psi_2]x_1$$

where $c = (I-K)(I-2\tau)$. Again, the last term of this expression is equal and of opposite sign, so that we can concentrate on the first part of the expression. Taking now also into account the denominator, the relevant expression simplifies as follows:

$$\frac{a(\Psi_1 + \Psi_2)}{\Psi_1^2 - \Psi_2^2} = \frac{a}{1 + \sigma + 2\theta} x_1; \quad \frac{b(\Psi_1 + \Psi_2)}{\Psi_1^2 - \Psi_2^2} = \frac{b}{1 + \sigma + 2\theta} x_1$$

But note that the derivative of these expressions with respect to λ is just zero. Hence we infer that $\partial m^T_2/\partial \Lambda - \partial m^T_1/\partial \Lambda$ and $\partial m^T_2/\partial m^T_1 = -1$. Finally, the Nash solution is known to represent one point in this line, so that we can derive the equation of the straight line:

$$T(\Lambda):\{(m_1^T, m_2^T) \mid m_2^T = -\frac{x_1 + x_2}{1 + \alpha - 2\theta} - m_1^T\}$$
 [VII]

Proofs to propositions 2 and 5. (Incentive compatibility) Takingas reference the m_i -axis, the slope of the target line is equal to -1, so that $tg(\omega_T)$ =-1, where ω_T =135°,315°. The bargaining area, A, is formed by the area within the ellipses crossing at the Nash solution (N). Thus, A is placed between the tangent lines to the two ellipses at N. Secondly, N is known to be a point on the target line. Therefore, as the figures suggest, if the target line lies between the angle formed by those two tangents: $\omega_W < \omega_T < \omega_{WP} \{i,j\} = \{1,2\}, i \neq j$, the target line will cross the bargaining area. The general expressions for the ellipses slope at Nash equilibrium are:

$$\frac{dm_2}{dm_1}\Big|_{dW_i=0} = -\frac{\partial W_i/\partial m_i}{\partial W_i/\partial m_j} = \frac{(1+\sigma)m_i^N - 2\theta m_j^N + (1-\tau)x_i + \tau x_j - (u_i - u_j)}{2\theta [m_i^N - 2\theta m_j^N + (1-\tau)x_i + \tau x_j - (u_i - u_j)]}$$

Let us consider first demand shocks $(x_1=x_2=0)$. Substituting the Nash solution [VI] into

the previous expression, we obtain

$$\frac{dm_2}{dm_1}\big|_{dW_1=0} = -\frac{0}{\sigma}(u_1 - u_2) = 0 \; ; \quad \frac{dm_2}{dm_1}\big|_{dW_2=0} = \frac{\sigma}{0}(u_1 - u_2) = \infty$$

The angles formed by these tangent lines depend on the sign of $(u_1 - u_2)$. In particular, for the ellipse corresponding to W_i :

$$\begin{split} \forall u_1, u_2, & \lim_{m_1 \to m_1^N} \frac{dm_2}{dm_1} \big|_{dW_1 = 0} = 0 \Rightarrow tg(\omega_{W_1}) = 0 \\ and & \exists \varepsilon > 0 \ | \ \forall u_1 - u_2 < 0, m_1 \in \ + [m_1^N - \varepsilon, m_1^N], \ \Rightarrow \frac{dm_2}{dm_1} \big|_{dW_1 = 0} > 0 \ ; \\ & \forall u_1 - u_2 > 0, m_1 \in \ [m_1^N - \varepsilon, m_1^N], \Rightarrow \frac{dm_2}{dm_1} \big|_{dW_1 = 0} < 0. \end{split}$$

Thus
$$\forall u_1 - u_2 < 0, \omega_W = 0^\circ = 360^\circ; \forall u_1 - u_2 > 0, \omega_W = 180^\circ$$

and for the second ellipse W_2 :

$$\begin{aligned} \forall u_1, u_2, & \lim \frac{dm_2}{dm_1} \big|_{dW_1=0} = \infty \Rightarrow tg(\omega_{W_1}) = \infty \\ and & \exists \varepsilon > 0 \quad \big| \quad \forall u_1 - u_2 < 0, m_2 \in \left. + \big[m_2^N - \varepsilon, m_2^N \big], \right. \Rightarrow \frac{dm_1}{dm_2} \big|_{dW_1=0} < 0 ; \\ \forall u_1 - u_2 > 0, m_2 \in \left. \big[m_2^N - \varepsilon, m_2^N \big], \Rightarrow \frac{dm_1}{dm_2} \big|_{dW_1=0} > 0. \end{aligned}$$

$$Thus \quad \forall u_1 - u_2 < 0, \omega_{W_2} = 90^\circ ; \quad \forall u_1 - u_2 > 0, \omega_{W_1} = 270^\circ$$

$$It \text{ follows then that } \forall u_1 - u_1 < 0 \Rightarrow \omega_{W_2} < \omega_T < \omega_{W_1}; \\ \forall u_1 - u_2 > 0 \Rightarrow \omega_W < \omega_T < \omega_W \end{aligned}$$

and the target line is precisely the bisectrix of the angle formed by the tangents to both ellipses. Thus, the target zone will always cross the bargaining area.

Proceeding as before we obtain that, for supply shocks $(u_1=u_2=0)$:

$$\frac{dm_2}{dm_1}\Big|_{dW_1=0} = -\frac{0}{\sigma 2\theta [(1+\sigma)x_1 + 2\theta x_2 + (1+\sigma - 2\theta)\tau(x_2 - x_1)]} = 0$$

$$\frac{dm_2}{dm_1}\Big|_{dW_2=0} = -\frac{\sigma 2\theta [(1+\sigma)x_2 + 2\theta x_1 + (1+\sigma - 2\theta)\tau(x_1 - x_2)]}{0} = \infty$$

For W_1 and W_2 , we have now:

$$x_2 \le -\frac{2\theta + (1 + \sigma - 2\theta)\tau}{1 + \sigma - (1 + \sigma - 2\theta)\tau} x_1 \Rightarrow \omega_{w_1} = 90^{\circ} ; x_2 \ge -\frac{2\theta + (1 + \sigma - 2\theta)\tau}{1 + \sigma - (1 + \sigma - 2\theta)\tau} x_1 \Rightarrow \omega_{w_1} = 270^{\circ}$$

 $2\theta + (1 + \sigma - 2\theta)\tau < (1 + \sigma) - (1 + \sigma - 2\theta)\tau$. Thus, the following cases arise:

$$\forall x_1 < 0$$
:

(a)
$$-\frac{2\theta + (1 + \sigma - 2\theta)\tau}{1 + \sigma - (1 + \sigma - 2\theta)\tau} x_1 \le x_2 \le -\frac{1 + \sigma - (1 + \sigma - 2\theta)\tau}{2\theta + (1 + \sigma - 2\theta)\tau} \Rightarrow tg(\omega_{W_i}) = 360^\circ; tg(\omega_{W_i}) = 270^\circ$$
(b)
$$x_2 > -\frac{1 + \sigma - (1 + \sigma - 2\theta)\tau}{2\theta + (1 + \sigma - 2\theta)\tau} \Rightarrow tg(\omega_{W_i}) = 180^\circ; tg(\omega_{W_i}) = 270^\circ$$
(c)
$$x_2 < -\frac{2\theta + (1 + \sigma - 2\theta)\tau}{1 + \sigma - (1 + \sigma - 2\theta)\tau} \Rightarrow tg(\omega_{W_i}) = 360^\circ; tg(\omega_{W_i}) = 90^\circ$$

(b)
$$x_2 > -\frac{1+\sigma-(1+\sigma-2\theta)\tau}{2\theta+(1+\sigma-2\theta)\tau} \Rightarrow tg(\omega_{w_1}) = 180^\circ; tg(\omega_{w_2}) = 270^\circ$$

(c)
$$x_2 < -\frac{2\theta + (1 + \sigma - 2\theta)\tau}{1 + \sigma - (1 + \sigma - 2\theta)\tau} \Rightarrow tg(\omega_{w_1}) = 360^\circ; tg(\omega_{w_1}) = 90^\circ$$

$$\forall x_1 > 0$$

(a)
$$-\frac{1+\sigma-(1+\sigma-2\theta)\tau}{2\theta+(1+\sigma-2\theta)\tau}x_1 \le x_2 \le -\frac{2\theta+(1+\sigma-2\theta)\tau}{1+\sigma-(1+\sigma-2\theta)\tau} \Rightarrow tg(\omega_{W_1}) = 90^\circ; tg(\omega_{W_1}) = 270^\circ$$
(b)
$$x_2 < -\frac{1+\sigma-(1+\sigma-2\theta)\tau}{2\theta+(1+\sigma-2\theta)\tau} \Rightarrow tg(\omega_{W_1}) = 360^\circ; tg(\omega_{W_2}) = 90^\circ$$
(c)
$$x_2 > -\frac{2\theta+(1+\sigma-2\theta)\tau}{1+\sigma-(1+\sigma+2\theta)\tau} \Rightarrow tg(\omega_{W_1}) = 180^\circ; tg(\omega_{W_2}) = 270^\circ$$

(b)
$$x_2 < -\frac{1+\sigma-(1+\sigma-2\theta)\tau}{2\theta+(1+\sigma-2\theta)\tau} \Rightarrow tg(\omega_{W_1}) = 360^\circ; tg(\omega_{W_2}) = 90^\circ$$

(c)
$$x_2 > -\frac{2\theta + (1 + \sigma - 2\theta)\tau}{1 + \sigma - (1 + \sigma + 2\theta)\tau} \Rightarrow tg(\omega_{w_1}) = 180^\circ; tg(\omega_{w_2}) = 270^\circ$$

Thus, the target line constitutes the bisectrix of the angle formed by the tangents to both ellipses in cases labelled (a); for the rest of cases, the target line is perpendicular to the bisectrix and consequently are ruled out. The range of shocks for which the target line crosses the bargaining area can then be established:

$$\forall x_i > 0, i, j=1, 2, i \neq j, if -\frac{(1+\sigma)-(1+\sigma-2\theta)\tau}{2\theta+(1+\sigma-2\theta)\tau} x_i \leq x_j \leq -\frac{2\theta+(1+\sigma-2\theta)\tau}{(1+\sigma)-(1+\sigma-2\theta)\tau} x_i \Rightarrow \exists \Lambda \mid T(\Lambda) \cap A$$

<u>Proof of propositions 3 and 6 (Pareto optimal points)</u>. Let us consider the bliss line B, instead of the contract curve, since the latter is too complex to work with. As a previous step, it is claimed that if the target line intersects the bliss line it also implies intersects the contract curve. We prove this claim as follows.

Since the contract curve, the target line and the bliss line are continuous and differentiable, we can express:

$$m_2^C = f(\delta)$$
 as a function of $m_1^C = g(\delta)$: $m_2^C = f(g^{-1}(m_1^C) = C'(m_1^C))$
 $m_2^T = f'(\Lambda)$ as a function of $m_1^T = g'(\Lambda)$: $m_2^T = f'(g^{-1}(m_1^T) = T'(m_1^T))$
 m_2^B as a function of m_1^B : $m_2^B = B(m_1^B)$

Then the lemma below, based on the Bolzano-Weierstrass theorem can be directly applied and our claim is proved.

The coordinates for which T=B are now found for the two different types of shocks. The intersection between B and T is obtained by equating expressions [IV] and [V].

For demand shocks $(x_1=0,x_2=0)$, we get

$$m_1^T = m_1^B = -m_2^T = -m_2^B = \frac{1}{2} \frac{u_1 - u_2}{2\theta}$$

which corresponds precisely to the middle point of the bliss line. Thus, in the case of demand shocks the target line will always cross the contract curve.

The resolution is more complex when <u>supply shocks</u> hit the economies $(u_1=u_2=0)$. Equating the target and bliss lines, the intersection is given by

$$\begin{split} m_1^T &= m_1^B = -\left[\frac{(1+\sigma)x_1 + 2\theta x_2}{2\theta(1+\sigma-2\theta)} + \frac{\tau(x_2 - x_1)}{2\theta}\right] \frac{(1-\tau)x_2 + \tau x_1}{(1-2\tau)(x_2 - x_1)};\\ m_2^T &= m_2^B = \left[\frac{(1+\sigma)x_1 + 2\theta x_1}{2\theta(1+\sigma-2\theta)} + \frac{\tau(x_1 - x_2)}{2\theta}\right] \frac{(1-\tau)x_1 + \tau x_2}{(1-2\tau)(x_2 - x_1)} \end{split}$$

where it is not straightforward to ascertain whether this point falls within the relevant segment of the bliss line. Thus, all the possible combinations of supply shocks are examined to obtain the range of shocks which permits the target line to intersect the bliss <u>segment</u>. The solution is given by the following range:

$$\begin{split} &\forall x_i \! > \! 0, \! i, \! j \! = \! 1, \! 2, \! i \! \neq \! j, \; if \\ &- \frac{(1 \! + \! \sigma) \! - \! (1 \! + \! \sigma \! - \! 2\theta)\tau}{2\theta \! + \! (1 \! + \! \sigma \! - \! 2\theta)\tau} x_i \! \leq \! x_j \! \leq \! - \frac{2\theta \! + \! (1 \! + \! \sigma \! - \! 2\theta)\tau}{(1 \! + \! \sigma) \! - \! (1 \! + \! \sigma \! - \! 2\theta)\tau} x_i \implies \exists \Lambda, \delta \; \mid \; \varUpsilon(\Lambda) \! = \! C(\delta), \end{split}$$

the same than in proposition 5 above.

<u>Lemma (Bolzano-Weierstrass)</u> The lines $C(\delta)$ and B have two common points, at $\delta=0$, $\delta=1$. Then, if $\exists m_i \mid T(\lambda) = B \Rightarrow \exists m_i \mid T(\lambda) = C(\delta)$.

PROOF: The claim is that $\exists m_1'' \mid (T'-C')m_1''=0$. Adding and substracting B, we get $(T'-B+B-C')m_1''$. Let us assume that $\exists m_1' \mid B(m_1')=T'(m_1')=m_2'$. Recall that $C(0)=B_2$, $C(1)=B_1$ so that $(C'-B)m_1^{B1}=(C'-B)m_1^{B2}=0$. Since B_2 , B_1 are the extremes of the bliss line, this implies that if

$$B(m_1^{Bi}) = C'(m_1^{Bi}) > T'(m_1^{Bi}), B(m_1^{Bj}) = C'(m_1^{Bj}) < T'(m_1^{Bj}), i,j = \{1,2\}, i \neq j$$

it follows that
$$\exists m_1'' \mid C'(m_1'') = T'(m_1'')$$

by Bolzano-Weierstrass, and the lemma is proved.

Proof of proposition 4 (and 7). (Optimal and incentive compatible points). From [VI], we observe that $m_1^T = -m_2^T$ on the target line in the absence of supply shocks. Substituting m_1 for $-m_2$ in the first order conditions of the cooperative solution (which corresponds to the left-side term and right-side term of the expression for $C(\delta)$ in [II]) and substituting Σ_i for the respective values, the following equalities must hold:

$$[\delta(1+\sigma)+(1-\delta)(2\theta)^{2}+2\theta]m_{1}^{T}=(\delta+(1-\delta)2\theta)(u_{1}-u_{2});$$

$$[(1-\delta)(1+\sigma)+\delta(2\theta)^{2}+2\theta]m_{1}^{T}=(\delta2\theta+(1-\delta))(u_{1}-u_{2});$$

Given the demand shocks, this is a non-linear system in δ and m_1^T . However, we showed that T intersects the bliss line at the middle point; this suggest that a reasonable guess for solving the system is $\delta = 1/2$. Indeed, it is immediate to see that $\delta = 1/2$ satisfy both equations. The Pareto optimal point on the target line is then given by:

$$C(\frac{1}{2}) = \{m_1^*, m_2^*\} \in T(\lambda) | m_1^* = \frac{(1+2\theta)(u_1-u_2)}{[\sigma+(1+2\theta)^2]} = -m_2^*$$

Substituting N and C(1/2) in the loss functions, the welfare loss is obtained:

$$W_1^N = W_2^N = \frac{\sigma}{2} \frac{1 + \sigma}{(1 + \sigma + 2\theta)^2} (u_1 - u_2);$$

$$W_1^* = W_2^* = \frac{(1 + \sigma + 2\theta^2)}{(1 + \sigma + 2\theta)^2 + (2\theta)^2 \sigma} W_1^N \implies W_i^* < W_i^N, \ i = 1, 2$$

and consequently the Pareto optimal point is incentive compatible.

<u>Proof of propositions 8 (optimal degree of commitment)</u> The money supplies of the cooperative solution [II] in the cases of demand and opposite supply shocks must belong to the target solution [V]. Noting that $x_1 = -x_2$ and $(\psi_1 - \psi_2)/(\psi_1^2 - \psi_2^2) = (1 + \sigma + 2\theta + 2\beta \rho')^{-1}$, it follows that:

$$m_{1}^{\circ} \mid_{C} = \frac{(1+2\theta)}{[\sigma+(1+2\theta)^{2}]} [(u_{1}-u_{2})-(1-2\tau)x_{1}] =$$

$$= \frac{(1+\beta\sqrt{\rho'})(\zeta\sqrt{\eta})(u_{1}-u_{2})-[(1-2\tau)+2\beta(\rho-\tau/\zeta)\sqrt{\rho'})/\sqrt{\eta}]x_{1}}{1+\sigma+2\theta+2\beta\rho'} = m_{1}^{\circ} \mid_{T}$$

Considering each shock separately and equating both terms to solve for β^* , for a given value of ρ :

is the general expression for the <u>optimal</u> degree of commitment to a given exchange rate target. Given the values of the parameters, it is immediate to check that β is positive for demand shocks

$$\forall u_{1}^{-}u_{2}, \quad \beta^{*} = \frac{\sigma 2\theta \sqrt{\eta} \ \zeta}{\sqrt{\rho'} \left[(1+2\theta)^{2} + \sigma) - 2\zeta \sqrt{\eta} \ (1+2\theta) \sqrt{\rho'} \ \right]}$$

$$\forall x_{1}^{-} = -x_{2}, \quad \beta^{*} = \frac{(1-2\tau)\sigma 2\theta \sqrt{\eta}}{2\sqrt{\rho'} \left[(\rho - \tau/\zeta)((1+2\theta)^{2} + \sigma) - \sqrt{\eta} \ (1+2\theta)(1-2\tau) \sqrt{\rho'} \ \right]}$$

in the considered range of ρ ; on the contrary, for opposite supply shocks the function presents a discontinuity at $\rho^+ = 2\theta[1 + 2\theta * \sigma/(1 + 2\theta) - 5\sqrt{\eta}]^2 > 0$. Values lower than ρ^+ yield negative β^* . Taking the derivative of β^* with respect to ρ reveals that $\partial \beta/\partial \rho > 0$ for demand shocks and $\partial \beta/\partial \rho < 0$ for opposite supply shocks.

<u>Proof of proposition 9 (Positive externality)</u>. Substituting the value of the shocks in the Nash solution [VI] we get

$$\forall x_{i} > 0, x_{j} \notin \left[-\frac{1+\sigma - (1+\sigma - 2\theta)\tau}{2\theta + (1+\sigma - 2\theta)\tau} x_{i}, -\frac{2\theta + (1+\sigma - 2\theta)\tau}{1+\sigma - (1+\sigma - 2\theta)\tau} x_{i} \right], i=1,2, i \neq j \Rightarrow$$

$$\Rightarrow sign(m_{i}^{N}) = sign(m_{j}^{N})$$

$$\forall x_{i} > 0, -\frac{1+\sigma - (1+\sigma - 2\theta)\tau}{2\theta + (1+\sigma - 2\theta)\tau} \sum_{i} \leq x_{j} \leq -\frac{2\theta + (1+\sigma - 2\theta)\tau}{1+\sigma - (1+\sigma - 2\theta)\tau} x_{i}, i=1,2, i \neq j \Rightarrow$$

$$\Rightarrow sign(m_{i}^{N}) \neq sign(m_{j}^{N})$$

$$\forall u_{1}, u_{2} \Rightarrow m_{1}^{N} = -m_{2}^{N}$$

Note that the first case covers just the range of values for which neither optimal nor incentive compatible exchange targeting strategies can be devised and other two cases conveyed the range of shocks for which propositions 2-7 apply. Thus, the proposition is proved.

Bibliography

BARON,D. (1989),"Design of Regulatory Mechanism and Institutions" ch.24 in Schmalensee,R and R.Willig, (eds.), Handbook of Industrial Organization, Amsterdam: North-Holland.

CANZONERI M., D.HENDERSON (1988). 'Is Sovereign Policy Making Bad?'. Carnegie-Rochester Conference Series on Public Policy, 28, pp.93-140.

CANZONERI M, D.HENDERSON (1991). Monetary Policy in Interdependent Economies. MIT

HUGHES HALLET, A., G.HOLTHAM, G.HUTSON. (1989) 'Exchange rate targetting as surrogate international cooperation', in Miller, M. B.Eichengreen, R, Portes ed. Blueprints for Exchange Rate Management, CEPR, Academic Press, pp.239-81.

HUGHES HALLET, A. (1993). 'Exchange rates and asymmetric policy regimes: when does exchange rate targeting pay'. Oxford Economic Papers, 45, pp.191-206.

KENEN, P. (1989). Exchange rates and policy coordination. Manchester University Press.

MCKINNON R. (1984). An International Standard for Monetary Stabilization. Policy Analysis in International Economics,8. Institute for International Economics

PERSSON,T. G.TABELLINI, (1992), "Designing Institutions for Monetary Stability", IGIER Working Paper n.35.

ROGOFF,K. (1985)."The Optimal Degree of Commitment to an Intermediate Monetary Target", Quarterly Journal of Economics, 100.

WALSH,C. (1995),"Optimal Contracts for Central Bankers", American Economic Review 85, 817-

WILLIAMSON J. (1985). The Exchange Rate System. Washington. Institute for International Economics.

WORKING PAPERS (1)

- 9010 Anindya Baner jee, Juan J. Dolado and John W. Galbraith: Recursive and sequential tests for unit roots and structural breaks in long annual GNP series.
- 9011 **Pedro Martínez Méndez:** Nuevos datos sobre la evolución de la peseta entre 1900 y 1936. Información complementaria.
- 9103 Juan J. Dolado: Asymptotic distribution theory for econometric estimation with integrated processes: a guide.
- 9106 **Juan Ayuso:** The effects of the peseta joining the ERM on the volatility of Spanish financial variables. (The Spanish original of this publication has the same number.)
- 9107 Juan J. Dolado and José Luis Escrivá: The demand for money in Spain: Broad definitions of liquidity. (The Spanish original of this publication has the same number.)
- 9109 Soledad Núñez: Los mercados derivados de la deuda pública en España: marco institucional y funcionamiento.
- 9110 Isabel Argimón and José M.º Roldán: Saving, investment and international mobility in EC countries. (The Spanish original of this publication has the same number.)
- 9111 José Luis Escrivá and Román Santos: A study of the change in the instrumental variable of the monetary control outline in Spain. (The Spanish original of this publication has the same number.)
- 9112 Carlos Chuliá: El crédito interempresarial. Una manifestación de la desintermediación financiera.
- 9113 Ignacio Hernando y Javier Vallés: Inversión y restricciones financieras: evidencia en las empresas manufactureras españolas.
- 9114 Miguel Sebastián: Un análisis estructural de las exportaciones e importaciones españolas: evaluación del período 1989-91 y perspectivas a medio plazo.
- 9115 Pedro Martínez Méndez: Intereses y resultados en pesetas constantes.
- 9116 Ana R. de Lamo y Juan J. Dolado: Un modelo del mercado de trabajo y la restricción de oferta en la economía española.
- 9117 Juan Luis Vega: Tests de raíces unitarias: aplicación a series de la economía española y al análisis de la velocidad de circulación del dinero (1964-1990).
- 9118 Javier Jareño y Juan Carlos Delrieu: La circulación fiduciaria en España: distorsiones en su evolución.
- 9119 Juan Ayuso Huertas: Intervenciones esterilizadas en el mercado de la peseta: 1978-1991.
- 9120 Juan Ayuso, Juan J. Dolado y Simón Sosvilla-Rivero: Eficiencia en el mercado a plazo de la peseta.
- 9121 José M. González-Páramo, José M. Roldán and Miguel Sebastián: Issues on Fiscal Policy in Spain.
- 9201 Pedro Martínez Méndez: Tipos de interés, impuestos e inflación.
- 9202 Víctor García-Vaquero: Los fondos de inversión en España.
- 9203 César Alonso and Samuel Bentolila: The relationship between investment and Tobin's Q in Spanish industrial firms. (The Spanish original of this publication has the same number.)
- 9204 Cristina Mazón: Márgenes de beneficio, eficiencia y poder de mercado en las empresas españolas.
- 9205 Cristina Mazón: El margen precio-coste marginal en la encuesta industrial: 1978-1988.
- 9206 Fernando Restoy: Intertemporal substitution, risk aversion and short term interest rates.
- 9207 Fernando Restoy: Optimal portfolio policies under time-dependent returns.
- 9208 Fernando Restoy and Georg Michael Rockinger: Investment incentives in endogenously growing economies.

- 9209 José M. González-Páramo, José M. Roldán y Miguel Sebastián: Cuestiones sobre política fiscal en España.
- 9210 Ángel Serrat Tubert: Riesgo, especulación y cobertura en un mercado de futuros dinámico.
- 9211 Soledad Núñez Ramos: Fras, futuros y opciones sobre el MIBOR.
- 9213 Javier Santillán: La idoneidad y asignación del ahorro mundial.
- 9214 María de los Llanos Matea: Contrastes de raíces unitarias para series mensuales. Una aplicación al IPC.
- 9215 Isabel Argimón, José Manuel González-Páramo y José María Roldán: Ahorro, riqueza y tipos de interés en España.
- 9216 Javier Azcárate Aguilar-Amat: La supervisión de los conglomerados financieros.
- 9217 **Olympia Bover:** An empirical model of house prices in Spain (1976-1991). (The Spanish original of this publication has the same number.)
- 9218 Jeroen J. M. Kremers, Neil R. Ericsson and Juan J. Dolado: The power of cointegration tests
- 9219 Luis Julián Álvarez, Juan Carlos Delrieu and Javier Jareño: Treatment of conflictive forecasts: Efficient use of non-sample information. (The Spanish original of this publication has the same number.)
- 9221 **Fernando Restoy:** Interest rates and fiscal discipline in monetary unions. (The Spanish original of this publication has the same number.)
- 9222 Manuel Arellano: Introducción al análisis econométrico con datos de panel.
- 9223 Ángel Serrat: Diferenciales de tipos de interés ONSHORE/OFFSHORE y operaciones SWAP.
- 9224 Ángel Serrat: Credibilidad y arbitraje de la peseta en el SME.
- 9225 **Juan Ayuso and Fernando Restoy:** Efficiency and risk premia in foreign exchange markets. (The Spanish original of this publication has the same number.)
- 9226 Luis J. Álvarez, Juan C. Delrieu y Antoni Espasa: Aproximación lineal por tramos a comportamientos no lineales: estimación de señales de nivel y crecimiento.
- 9227 **Ignacio Hernando y Javier Vallés:** Productividad, estructura de mercado y situación financiera
- 9228 Ángel Estrada García: Una función de consumo de bienes duraderos.
- 9229 **Juan J. Dolado and Samuel Bentolila:** Who are the insiders? Wage setting in spanish manufacturing firms.
- 9301 Emiliano González Mota: Políticas de estabilización y límites a la autonomía fiscal en un área monetaria y económica común.
- 9302 Anindya Banerjee, Juan J. Dolado and Ricardo Mestre: On some simple tests for cointegration: the cost of simplicity.
- 9303 Juan Ayuso and Juan Luis Vega: Weighted monetary aggregates: The Spanish case. (The Spanish original of this publication has the same number.)
- 9304 Ángel Luis Gómez Jiménez: Indicadores de la política fiscal: una aplicación al caso español.
- 9305 Ángel Estrada y Miguel Sebastián: Una serie de gasto en bienes de consumo duradero.
- 9306 Jesús Briones, Ángel Estrada e Ignacio Hernando: Evaluación de los efectos de reformas en la imposición indirecta.
- 9307 Juan Ayuso, María Pérez Jurado and Fernando Restoy: Credibility indicators of an exchange rate regime: The case of the peseta in the EMS. (The Spanish original of this publication has the same number.)
- 9308 Cristina Mazón: Regularidades empíricas de las empresas industriales españolas: ¿existe correlación entre beneficios y participación?

- 9.309 Juan Dolado, Alessandra Goria and Andrea Ichino: Immigration and growth in the host country.
- 9310 Amparo Ricardo Ricardo: Series históricas de contabilidad nacional y mercado de trabajo para la CE y EEUU: 1960-1991.
- 9311 Fernando Restoy and G. Michael Rockinger: On stock market returns and returns on investment.
- 9312 Jesús Saurina Salas: Indicadores de solvencia bancaria y contabilidad a valor de mercado.
- 9.313 Isabel Argimón, José Manuel González-Páramo, Maria Jesús Martín and José María Roldán: Productivity and infrastructure in the Spanish economy. (The Spanish original of this publication has the same number.)
- 9314 Fernando Ballabriga, Miguel Sebastián and Javier Vallés: Interdependence of EC economies: A VAR approach.
- 9315 Isabel Argimón y M.ª Jesús Martín: Serie de «stock» de infraestructuras del Estado y de las Administraciones Públicas en España.
- 9316 P. Martínez Méndez: Fiscalidad, tipos de interés y tipo de cambio.
- 9317 P. Martínez Méndez: Efectos sobre la política económica española de una fiscalidad distorsionada por la inflación.
- 9.318 Pablo Antolin and Olympia Bover: Regional Migration in Spain: The effect of Personal Characteristics and of Unemployment, Wage and House Price Differentials Using Pooled Cross-Sections.
- 9319 Samuel Bentolila y Juan J. Dolado: La contratación temporal y sus efectos sobre la competitividad.
- 9.320 Luis Julián Álvarez, Javier Jareño y Miguel Sebastián: Salarios públicos, salarios privados e inflación dual.
- 9321 Ana Revenga: Credibility and inflation persistence in the European Monetary System. (The Spanish original of this publication has the same number.)
- 9322 María Pérez Jurado and Juan Luis Vega: Purchasing power parity: An empirical analysis. (The Spanish original of this publication has the same number.)
- 9323 **Ignacio Hernando y Javier Vallés:** Productividad sectorial: comportamiento cíclico en la economía española.
- 9324 Juan J. Dolado, Miguel Sebastián and Javier Vallés: Cyclical patterns of the Spanish economy.
- 9325 Juan Ayuso y José Luis Escrivá: La evolución del control monetario en España.
- 9326 Alberto Cabrero Bravo e Isabel Sánchez García: Métodos de predicción de los agregados monetarios.
- 9327 Cristina Mazón: Is profitability related to market share? An intra-industry study in Spanish manufacturing.
- 9328 Esther Gordo y Pilar L'Hotellerie: La competitividad de la industria española en una perspectiva macroeconómica.
- 9329 Ana Buisán y Esther Gordo: El saldo comercial no energético español: determinantes y análisis de simulación (1964-1992).
- 9330 Miguel Pellicer: Functions of the Banco de España: An historical perspective.
- 9401 Carlos Ocaña, Vicente Salas y Javier Vallés: Un análisis empírico de la financiación de la pequeña y mediana empresamanufacturera española: 1983-1989.
- 9402 P.G. Fisher and J. L. Vega: An empirical analysis of M4 in the United Kingdom.
- 9403 J. Ayuso, A. G. Haldane and F. Restoy: Volatility transmission along the money market yield curve.
- 9404 Gabriel Quirós: El mercado británico de deuda pública.

- 9405 Luis J. Álvarez and Fernando C. Ballabriga: BVAR models in the context of cointegration: A Monte Carlo experiment.
- 9406 Juan José Dolado, José Manuel González-Páramo y José M.ª Roldán: Convergencia económica entre las provincias españolas: evidencia empírica (1955-1989).
- 9407 Ángel Estrada e Ignacio Hernando: La inversión en España: un análisis desde el lado de la oferta.
- 9408 Ángel Estrada García, M.º Teresa Sastre de Miguel y Juan Luis Vega Croissier: El mecanismo de transmisión de los tipos de interés: el caso español.
- 9409 Pilar Garcia Perea y Ramón Gómez: Elaboración de series históricas de empleo a partir de la Encuesta de Población Activa (1964-1992).
- 9410 F. J. Sáez Pérez de la Torre, J. M.º Sánchez Sáez y M.º T. Sastre de Miguel: Los mercados de operaciones bancarias en España: especialización productiva y competencia.
- 9411 Olympia Bover and Ángel Estrada: Durable consumption and house purchases: Evidence from Spanish panel data.
- 9412 **José Viñals:** Building a Monetary Union in Europe: Is it worthwhile, where do we stand, and where are we going? (The Spanish original of this publication has the same number.)
- 9413 Carlos Chuliá: Los sistemas financieros nacionales y el espacio financiero europeo.
- 9414 José Luis Escrivá and Andrew G. Haldane: The interest rate transmission mechanism: Sectoral estimates for Spain. (The Spanish original of this publication has the same number.)
- 9415 M.º de los Llanos Matea y Ana Valentina Regil: Métodos para la extracción de señales y para la trimestralización. Una aplicación: Trimestralización del deflactor del consumo privado nacional.
- 9416 José Antonio Cuenca: Variables para el estudio del sector monetario. Agregados monetarios y crediticios, y tipos de interés sintéticos.
- 9417 Ángel Estrada y David López-Salido: La relación entre el consumo y la renta en España: un modelo empírico con datos agregados.
- 9418 José M. González Mínguez: Una aplicación de los indicadores de discrecionalidad de la política fiscal a los países de la UE.
- 9419 Juan Ayuso, María Pérez Jurado and Fernando Restoy: Is exchange rate risk higher in the E.R.M. after the widening of fluctuation bands? (The Spanish original of this publication has the same number.)
- 9420 Simon Milner and David Metcalf: Spanish pay setting institutions and performance outcomes.
- 9421 Javier Santillán: El SME, los mercados de divisas y la transición hacia la Unión Monetaria.
- 9422 Juan Luis Vega: Is the ALP long-run demand function stable? (The Spanish original of this publication has the same number.)
- 9423 Gabriel Quirós: El mercado italiano de deuda pública.
- 9424 Isabel Argimón, José Manuel González-Páramo y José María Roldán: Inversión privada, gasto público y efecto expulsión: evidencia para el caso español.
- 9425 Charles Goodhart and José Viñals: Strategy and tactics of monetary policy: Examples from Europe and the Antipodes.
- 9426 Carmen Melcón: Estrategias de política monetaria basadas en el seguimiento directo de objetivos de inflación. Las experiencias de Nueva Zelanda, Canadá, Reino Unido y Suecia.
- 9427 Olympia Bover and Manuel Arellano: Female labour force participation in the 1980s: the case of Spain.

- 9428 Juan María Peñalosa: The Spanish catching-up process: General determinants and contribution of the manufacturing industry.
- 9429 Susana Núñez: Perspectivas de los sistemas de pagos: una reflexión crítica.
- 9430 José Viñals: ¿Es posible la convergencia en España?: En busca del tiempo perdido.
- 9501 Jorge Blázquez y Miguel Sebastián: Capital público y restricción presupuestaria gubernamental.
- 9502 Ana Buisán: Principales determinantes de los ingresos por turismo.
- 9503 Ana Buisán y Esther Gordo: La protección nominal como factor determinante de las importaciones de bienes.
- 9504 Ricardo Mestre: A macroeconomic evaluation of the Spanish monetary policy transmission mechanism.
- 9505 Fernando Restoy and Ana Revenga: Optimal exchange rate flexibility in an economy with intersectoral rigidities and nontraded goods.
- 9506 Ángel Estrada and Javier Vallés: Investment and financial costs: Spanish evidence with panel data. (The Spanish original of this publication has the same number.)
- 9507 Francisco Alonso: La modelización de la volatilidad del mercado bursátil español.
- 9508 Francisco Alonso y Fernando Restoy: La remuneración de la volatilidad en el mercado español de renta variable.
- 9509 Fernando C. Ballabriga, Miguel Sebastián y Javier Vallés: España en Europa: asimetrías reales y nominales.
- 9510 Juan Carlos Casado, Juan Alberto Campoy y Carlos Chuliá: La regulación financiera española desde la adhesión a la Unión Europea.
- 9511 Juan Luis Díaz del Hoyo y A. Javier Prado Domínguez: Los FRAs como guías de las expectativas del mercado sobre tipos de interés.
- 9512 José M.* Sánchez Sáez y Teresa Sastre de Miguel: ¿Es el tamaño un factor explicativo de las diferencias entre entidades bancarias?
- 9513 Juan Ayuso y Soledad Núñez: ¿Desestabilizan los activos derivados el mercado al contado?: La experiencia española en el mercado de deuda pública.
- 9514 M.º Cruz Manzano Frías y M.º Teresa Sastre de Miguel: Factores relevantes en la determinación del margen de explotación de bancos y cajas de ahorros.
- 9515 Fernando Restoy and Philippe Weil: Approximate equilibrium asset prices.
- 9516 Gabriel Quirós: El mercado francés de deuda pública.
- 9517 Ana L. Revenga and Samuel Bentolila: What affects the employment rate intensity of growth?
- 9518 Ignacio Iglesias Araúzo y Jaime Esteban Velasco: Repos y operaciones simultáneas: estudio de la normativa.
- 9519 Ignacio Fuentes: Las instituciones bancarias españolas y el Mercado Único.
- 9520 Ignacio Hernando: Política monetaria y estructura financiera de las empresas.
- 9521 Luis Julián Álvarez y Miguel Sebastián: La inflación latente en España: una perspectiva macroeconómica.
- 9522 Soledad Núñez Ramos: Estimación de la estructura temporal de los tipos de interés en España: elección entre métodos alternativos.
- 9523 Isabel Argimón, José M. González-Páramo y José M.* Roldán Alegre: Does public spending crowd out private investment? Evidence from a panel of 14 OECD countries.

- 9524 Luis Julián Álvarez, Fernando C. Ballabriga y Javier Jareño: Un modelo macroeconométrico trimestral para la economía española.
- 9525 Aurora Alejano y Juan M.ª Peñalosa: La integración financiera de la economía española: efectos sobre los mercados financieros y la política monetaria.
- 9526 Ramón Gómez Salvador y Juan J. Dolado: Creación y destrucción de empleo en España: un análisis descriptivo con datos de la CBBE.
- 9527 Santiago Fernández de Lis y Javier Santillán: Regímenes cambiarios e integración monetaria en Europa.
- 9528 Gabriel Quirós: Mercados financieros alemanes.
- 9529 **Juan Ayuso Huertas:** Is there a trade-off between exchange rate risk and interest rate risk? (The Spanish original of this publication has the same number.)
- 9530 Fernando Restoy: Determinantes de la curva de rendimientos: hipótesis expectacional y primas de riesgo.
- 9531 Juan Ayuso and María Pérez Jurado: Devaluations and depreciation expectations in the EMS.
- 9532 Paul Schulstad and Ángel Serrat: An Empirical Examination of a Multilateral Target Zone Model.
- 9601 Juan Ayuso, Soledad Núñez and María Pérez-Jurado: Volatility in Spanish financial markets: The recent experience.
- 9602 Javier Andrés e Ignacio Hernando: ¿Cómo afecta la inflación al crecimiento económico? Evidencia para los países de la OCDE.
- 9603 Barbara Dluhosch: On the fate of newcomers in the European Union: Lessons from the Spanish experience.
- 9604 Santiago Fernández de Lis: Classifications of Central Banks by Autonomy: A comparative analysis
- 9605 M.º Cruz Manzano Frías y Sofía Galmés Belmonte: Credit Institutions' Price Policies and Type of Customer: Impact on the Monetary Transmission Mechanism. (The Spanish original of this publication has the same number.)
- 9606 Malte Krüger: Speculation, Hedging and Intermediation in the Foreign Exchange Market.
- 9607 Agustín Maravall: Short-Term Analysis of Macroeconomic Time Series.
- 9608 Agustín Maravall and Christophe Planas: Estimation Error and the Specification of Unobserved Component Models.
- 9609 Agustín Maravall: Unobserved Components in Economic Time Series.
- 9610 Matthew B. Canzoneri, Behzad Diba and Gwen Eudey: Trends in European Productivity and Real Exchange Rates.
- 9611 Francisco Alonso, Jorge Martínez Pagés y María Pérez Jurado: Weighted Monetary Aggregates: an Empirical Approach. (The Spanish original of this publication has the same number.)
- 9612 Agustín Maravall and Daniel Peña: Missing Observations and Additive Outliers in Time Series Models.
- 9613 Juan Ayuso and Juan L. Vega: An empirical analysis of the peseta's exchange rate dynamics.
- 9614 Juan Ayuso Huertas: Un análisis empírico de los tipos de interés reales ex-ante en España.
- 9615 Enrique Alberola Ila: Optimal exchange rate targets and macroeconomic stabilization.
- (1) Previously published Working Papers are listed in the Banco de España publications catalogue.