Government Procurement and Access to Credit: Firm Dynamics and Aggregate Implications

Julian di Giovanni*, Manuel García-Santana Priit Jeenas Priit Jeenas Josep Pijoan-Mas

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 - Large fraction of economic activity (10-15% of GDP in EU-27 and U.S.)
 - It is spread across many industries of the economy
- Recurrent policy debate: should governments target specific types of firms?
 - Target big firms to build "national champions"
 - Target small firms to help them grow (e.g., U.S. Small Business Act or European Parliament)

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- Study the effects of public procurement on firm outcomes and the macroeconomy
 - o Focus on severity and type of firms' financial frictions
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 - o Focus on severity and type of firms' financial frictions
 - Show how allocation of contracts to firms can have first-order effects
- New administrative data set and a model of firm dynamics with a government sector to analyze:
 - Firm selection into procurement
 - o Treatment effect of procurement on firm dynamics
 - ⇒ Quantify the *long-run macroeconomic consequences* of alternative procurement allocation systems in Spain



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 - o Including whether a loan features posted (tangible) collateral
 - Loan applications for "new" firm-bank relations
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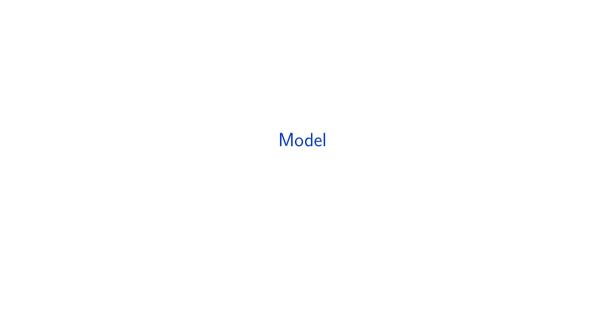


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- Onsistent with earnings from the public sector being more pledgeable
- 4.a/ Procurement contract significant when controlling for future sales growth Fact 4
- 4.b/ Procurement associated with higher leverage growth ("structural", more below)



Model's main ingredients

- Build on standard framework of firm dynamics with financial frictions (Midrigan and Xu, 2014)
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 - a. Exogenous differences in productivity across firms
 - b. Firms can borrow and save
 - c. Borrowing is subject to a financial constraint
- We extend this setting to allow for:
 - d. Downward-sloping demands in both the private and public sectors
 - e. Endogenous choice to compete for procurement projects
 - f. Earnings-based borrowing constraints

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 - Private good uses all varieties
 - \circ Public good only uses a subset $I_g \subset [0,1]$ of varieties (w/ measure m_g)

$$Y_p = \left(\int_{[0,1]} y_{ip}^{\frac{\sigma-1}{\sigma}} di\right)^{\frac{\sigma}{\sigma-1}} \quad \text{ and } \quad Y_g = m_g \frac{1}{1-\sigma} \left(\int_{I_g} y_{ig}^{\frac{\sigma-1}{\sigma}} di\right)^{\frac{\sigma}{\sigma-1}}$$

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- Each Intermediate good produced by a different firm, with CRS technology $y_i = s_i k_i$
- Firms compete independently in each sector facing the following demands

$$p_{ip} = B_p [y_{ip}]^{-1/\sigma}$$
, where $B_p \equiv P_p Y_p^{1/\sigma}$
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Public procurement

- Procurement allocation system:
 - o Firms compete for contracts by preparing costly applications
 - Firms must invest $b_{it} > 0$ at t in order to obtain a procurement contract at t+1 ($d_{it+1} = 1$)
 - o Better applications more likely to succeed, but there is always uncertainty

$$Pr(d_{it+1} = 1 \mid b_{it}) = 1 - e^{-\eta_0 b_{it}^{\eta_1}}$$

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Equilibrium

 \circ η_0 ensures that the fraction of firms obtaining a procurement project equals m_g

First principles

• Firm i owned by entrepreneur i, w/ survival probability θ and preferences:

$$\sum_{t=0}^{\infty} (\beta \theta)^t \mathbb{E} \left[\frac{c_{it}^{1-\mu} - 1}{1-\mu} \right]$$

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$$c_{it} + b_{it} + k_{it+1} + (1+r)l_{it} \le p_{ipt}y_{ipt} + p_{igt}y_{igt} + (1-\delta)k_{it} + l_{it+1} - tax_{it}$$

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- With the proper timing assumptions
 - \circ We can re-write the problem in terms of firm's net worth $a_{it} \equiv k_{it} l_{it}$
 - We can split the problem into a static production and a dynamic saving problems



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Dynamic problem:

- Entrepreneurs with lower levels of net worth (a = k l) have
 - o higher returns to asset accumulation (relax asset-based constraint),
 - o lower returns of winning a procurement project
- ⇒ Selection into procurement by firms with high net worth



Borrowing constraint

• We have 3 parameters in the borrowing constraint $(\varphi_k, \varphi_p, \varphi_g)$

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- Asset-based parameter (φ_k)
 - Match aggregate credit to capital ratio: $\varphi_k = 0.54$

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Benchmark economy: Selection and treatment

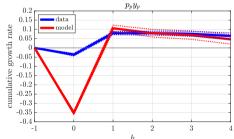
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• Treatment:

- Short-run crowding-out (scarce collateral split between two markets)
- Long-run crowding-in (higher revenues accelerates self-financing channel)



"set aside" policies

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 - ⇒ Average project size remains constant

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- The reform generates an 8% increase in P_g/P_p
 - At same expenditure, lower provision of public goods.

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 - o Captures the aggregation of the (long-run) crowding in effect
- **3** "Full" GE long-run \Rightarrow GDP \uparrow by 2.07%
 - o Captures changes in savings decisions, changes in selection, and GE effects



 Targeting small firms in procurement may increase GDP by strengthening self-financing channel of constrained firms

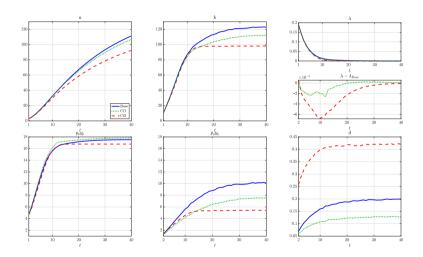
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 - ⇒ GDP would ↓ by 2.68% (much bigger reduction in big firms' incentives to save)
 - \circ In a world in which $\phi_g \simeq \phi_p$
 - ⇒ Effects of policies much less expansionary (may lead to GDP losses)



Life cycle of firms: high productivity firms



Benchmark economy: Aggregates

- Modest levels of misallocation
 - \circ TFP $_p$ gains of reallocating capital across firms: 4.7%
 - \circ TFP $_g$ gains of reallocating capital across firms: 3.3%
- But sizeable output costs of financial frictions
 - GDP increase of setting $\phi_a \rightarrow \infty$: 12.0%
- More efficient provision of public than private goods
 - $P_g/P_p = 0.90 < 1$
 - Selection on s: higher productivity of procurement firms
 - Selection on a and $\phi_q > \phi_p$: less misallocation of capital across procurement firms

Summary statistics

- Types and size of procurement projects
 - A lot of procurement outside construction (>80% of projects outside construction)
 - High presence of relatively small contracts (median ≈ 0.35-0.70 M euro)
- Procurement vs. non-procurement firms Go Go'
 - Procurement firms are larger and older on average (but large overlap in the support of firm size)
 - \circ Higher share of non-collateralized credit for procurement firms, despite larger net worth (86% vs. 71%)
- Back

Number and size of projects **Back**

Table: Value of Procurement projects (budget value in millions of euro), pool of years 2000-13

sector	mean	10th	25th	50th	75th	99th	obs.
Construction	5.28	0.13	0.23	0.74	4.00	70.84	22,549
Consulting	0.66	0.10	0.17	0.37	0.84	3.91	12,427
Services	1.22	0.11	0.20	0.42	1.05	13.47	44,581
Supplies	0.95	0.10	0.17	0.37	0.86	10.20	45,552
Others	1.99	0.09	0.15	0.35	0.99	38.18	5,524

Procurement across industries Back

Sector	Description	Firms (1)	Emp. (2)	Sales (3)	Assets (4)	Credit (5)
19	Manufacture of coke & refined petroleum prod.	0.150	0.332	0.315	0.310	0.243
21	Manufacturing of Pharmaceutical Products	0.149	0.240	0.225	0.231	0.288
42	Civil Engineering	0.093	0.260	0.324	0.366	0.386
80	Security and investigation activities	0.064	0.198	0.299	0.269	0.312
30	Manufacturing of Transport Equipment	0.052	0.176	0.177	0.205	0.180
94	Activities of membership organisations	0.051	0.069	0.127	0.037	0.018
36	Collection, purification and distribution of water	0.040	0.116	0.117	0.088	0.121
61	Telecommunications	0.038	0.217	0.192	0.189	0.207
51	Air transportation	0.033	0.054	0.049	0.078	0.142
81	Services of Buildings Maintenance	0.031	0.137	0.232	0.151	0.211
63	Information services	0.026	0.127	0.100	0.080	0.087
62	Programming, consultancy, other IT activities	0.025	0.151	0.193	0.157	0.214
26	Manufacturing of IT, electronic, & optical prod.	0.025	0.087	0.095	0.125	0.165
71	Technical services of architecture & engineering	0.024	0.152	0.159	0.084	0.103
2	Forestry and logging	0.019	0.069	0.068	0.033	0.080
6	Extraction of crude petroleum and natural gas	0.017	0.021	0.036	0.016	0.026
91	Libraries, archives, museums and cultural activities	0.016	0.061	0.051	0.021	0.017
29	Manufacture of motor vehicles and trailers	0.015	0.030	0.036	0.030	0.086
72	R&D activities	0.014	0.017	0.014	0.003	0.003
17	Paper industry	0.014	0.033	0.032	0.038	0.067

Procurement and non-procurement firms

	mean		2	25th		50th		75th
	<u>Proc</u>	No.proc	<u>Proc</u>	No.proc	<u>Proc</u>	No.proc	<u>Proc</u>	No.proc
Age	20.42	10.95	12.00	5.00	17.00	10.00	24.00	15.00
Employment	73.56	12.75	16.00	3.00	45.00	6.00	155.0	12.00
Sales	8.96	1.19	1.14	0.10	4.22	0.28	16.89	0.86
Procurement/Sales	0.20	0.00	0.01	0.00	0.03	0.00	0.10	0.00
Fixed Assets	3.80	0.85	0.21	0.03	0.82	0.14	3.58	0.50
Credit	2.51	0.57	0.11	0.03	0.48	0.08	2.32	0.30
Coll. Credit (share)	0.14	0.29	0.00	0.00	0.00	0.00	0.14	0.74



Fact 1: Credit growth and procurement

	All firms	Bidde	rs only
		First	Second
	(1)	(2)	(3)
$PROC_{it}$	0.055^{a}	0.073^{a}	-0.061
	(0.004)	(0.028)	(0.049)
$log(Credit_{it-1})$	$\dot{-0.410}^{lpha}$	$\dot{-0.175}^{lpha}$	-0.229^{lpha}
J,,	(0.001)	(0.043)	(0.044)
Observations	700,780	8,310	3,683
R-squared	0.786	0.360	0.458
Sector×quarter FE	Yes	No	No
Firm×year FE	Yes	Yes	Yes
Quarter FE	No	Yes	Yes
Auction FE	No	Yes	Yes



Fact 2: Composition of credit growth and procurement

	All	firms				
			F	irst	Se	cond
	Collat. (1)	NoCollat. (2)	Collat. (3)	NoCollat. (4)	Collat. (5)	NoCollat. (6)
$PROC_{it}$	0.001 (0.006)	$0.070^{a} \ (0.005)$	-0.011 (0.029)	$0.080^{b} \ (0.031)$	-0.019 (0.044)	-0.058 (0.057)
Observations	224,011	557,873	2,690	8,110	1,423	3,606
R-squared	0.791	0.764	0.357	0.368	0.435	0.435
Sector×quarter FE	Yes	Yes	No	No	No	No
Firm×year FE	Yes	Yes	Yes	Yes	Yes	Yes
Quarter FE	No	No	Yes	Yes	Yes	Yes
Auction FE	No	No	Yes	Yes	Yes	Yes



Fact 3: Probability of a new loan and procurement

	All firms		
	(1)	(2)	
$PROC_{it}$	0.024^a (0.008)	0.023^b (0.011)	
Observations	36,857	26,924	
R-squares	0.395	0.628	
Firm×bank FE	Yes	Yes	
Bank×quarter FE	No	Yes	
Sector×quarter FE	No	Yes	

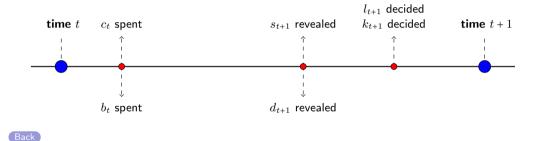


Fact 4: Credit growth and procurement, given future sales growth

	(-)	All firms	(-)
	(1)	(2)	(3)
$PROC_{it}$	0.053^{a}	0.043^{a}	0.041^{a}
	(0.006)	(0.006)	(0.006)
Sales growth $_{it+1}$	0.107^{a}	0.027^{b}	0.024^{c}
•	(0.020)	(0.011)	(0.011)
Observations	86,537	86,096	83,652
R-squared	0.051	0.282	0.330
Year FE	Yes	Yes	No
Firm FE	No	Yes	Yes
Sector×Year FE	No	No	Yes



Timing in the model





Preferences and constraints

Re-formulation

• Let $a_{it} \equiv k_{it} - l_{it}$ be the firm's net worth. We can re-write the constraints as:

$$c_{it} + b_{it} + a_{it+1} \leq (1+r)a_{it} + (1-\tau)\underbrace{\left[p_{ipt}y_{ipt} + p_{igt}y_{igt} - (r+\delta)k_{it}\right]}_{\pi_{it}}$$

$$k_{it} \leq \phi_a a_{it} + \phi_p p_{ipt}y_{ipt} + \phi_g p_{igt}y_{igt}$$

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$$k_{it} \leq \phi_a a_{it} + \phi_p p_{ipt}y_{ipt} + \phi_g p_{igt}y_{igt}$$

• The parameters in the borrowing constraint are re-defined as:

$$\phi_a \equiv \frac{1}{1 - \varphi_k}, \quad \phi_p \equiv \frac{\varphi_p}{1 - \varphi_k}, \quad \phi_g \equiv \frac{\varphi_g}{1 - \varphi_k}$$

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- The problem can be split into:
 - Static production problem
 - Dynamic saving problem



Static production problem

Set up

• The entrepreneur of type (s, a, d) chooses sizes $k_p(s, a, d)$ and $k_g(s, a, d)$:

$$\begin{split} \pi\left(s,a,d\right) &= \max_{k_p,k_g \geq 0} \left\{ p_p y_p + p_g y_g - (r+\delta) \left(k_p + k_g\right) \right\} \\ \text{subject to:} \\ &p_p y_p = B_p \left[s k_p \right]^{\frac{\sigma-1}{\sigma}} \\ &p_g y_g = B_g \left[s k_g \right]^{\frac{\sigma-1}{\sigma}} \times d \\ &k_p + k_g \leq \phi_k a + \phi_p p_p y_p + \phi_g p_g y_g \end{split}$$

• There will be a multiplier $\lambda\left(s,a,d\right)$ associated to the financial constraint

Back

Dynamic problem

Set up

- Entrepreneur chooses consumption c(s, a, d), savings a'(s, a, d) and investment in proc. b(s, a, d)
- The dynamic saving problem can be written in recursive form,

$$\begin{split} V\left(s,a,d\right) &= \max_{c,b,a'} \left\{ u\left(c\right) + \beta\theta \, \mathbb{E}_{s',d'\mid s,b} \left[V\left(s',a',d'\right) \right] \right\} \\ \text{subject to:} \\ c+b+a' &= \left(1+r\right)a + \left(1-\tau\right)\pi \left(s,a,d\right) \\ a' &\geq 0 \\ \mathbb{E}_{s',d'\mid s,b} \left[V\left(s',a',d'\right) \right] &= \Pr\left(d'=1|b\right)\mathbb{E}_{s'\mid s} V\left(s',a',1\right) + \Pr\left(d'=0|b\right)\mathbb{E}_{s'\mid s} V\left(s',a',0\right) \end{split}$$

Back

Equilibrium conditions I

- a) Entrepreneurs solve their optimization problem
- b) The probability measure Γ is stationary
- c) The market for the private good clears:

$$\int_{\mathbf{X}} p_p(a, s, d) u(a, s, d) y(s, a, d) d\Gamma = Y_p = \int_{\mathbf{X}} \left[b(s, a, d) + c(s, a, d) + \delta k(s, a, d) \right] d\Gamma$$

d) The market for the public good clears:

$$\int_{\mathbf{X}_{1}} p_{g}(a, s, 1) [1 - u(a, s, 1)] y(s, a, 1) d\Gamma = P_{g} Y_{g}$$

 The probability of obtaining procurement projects is consistent with the measure of goods bought by the public sector,

$$\int_{\mathbf{X}} Pr(d'=1 \mid b(s,a,d)) d\Gamma = \int_{\mathbf{X}_1} d\Gamma = m_g$$

f) The budget constraint of the government holds

$$PgYg = rD + \tau \int_{\mathbf{X}} \pi(s, a, d) d\Gamma + (1 - \theta) \left[\int_{\mathbf{X}} a'(s, a, d) d\Gamma - \int_{\mathbf{X}} a d\Gamma_0 \right]$$

g) By Walras law, the debt market clears.

$$D = \int_{\mathbf{X}} \left[k(s, a, d) - a(s, a, d) \right] d\Gamma$$



Structural leverage regressions

	(1)	(2)	(3)
$\Delta p_{it} y_{it} / k_{it}$ $\Delta p_{igt} y_{igt} / k_{it}$	0.425^{c} (0.227) 0.682^{c} (0.391)	0.543^{b} (0.257) 0.797^{c} (0.478)	0.419^{c} (0.229) 1.047^{c} (0.588)
Observations R-squared Sector×year FE Sample by age	579 0.391 Yes ≤ 10 yrs	403 0.437 Yes ≤ 9 yrs	282 0.421 Yes ≤ 8 yrs



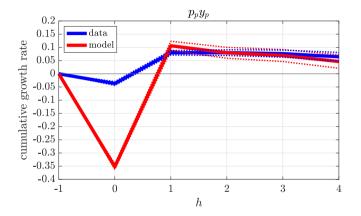
Calibration parameter values

	Panel A: parameters			Panel B: Moments	
		(1)	(2)		
		Baseline	$\phi_p = \phi_g$		
Block 1					
μ	CRRA coefficient	2.00	2.00		
σ_p	CES private sector	3.00	3.00		
σ_p	CES government	3.00	3.00	extscpredetermined	
β	Discount factor	0.94	0.94		
δ	Depreciation rate	0.10	0.10		
ρ_s	AR(1) correlation	0.80	0.80		
σ_s	AR(1) variance	0.30	0.30		
Block 2					Data = Model
ϕ_a	borrowing const. (a)	2.17	2.34	Credit/K	0.55
ϕ_p	borrowing const. $(p_p y_p)$	0.92	0.99	reg. coefficient (φ_p)	0.42
ϕ_g	borrowing const. $(p_g y_g)$	2.40	0.99	reg. coefficient $(\varphi_g - \varphi_p)$	0.68
Block 3					
η_0	probability function (level)	0.21	0.21	Consistency of $g(b)$ with m_g	-
η_1	probability function (slope)	0.53	0.55	Procurement premium	0.72
Y_g	demand shifter	0.83	0.63	Share of procurement in GDP	0.12
m_g	measure of procurement goods	0.038	0.038	Percentage of procurement firms	3.8%
Block 4					
D	Government lending	0.86	0.84	Interest rate	5%
\bar{s}	Productivity shifter	-6.51	-6.53	K/Y (aggregate)	3.88
heta	Survival probability	0.95	0.95	Exit rate	5%



Treatment in benchmark economy Back

Crowding out of private sales: model vs. data (local projection)



- Small/constrained firm cuts private sales initially when receiving procurement
- As firm constraints become less binding expands sales to private sector