

Monetary Policy Macroprudential Policy and the Financial Cycle

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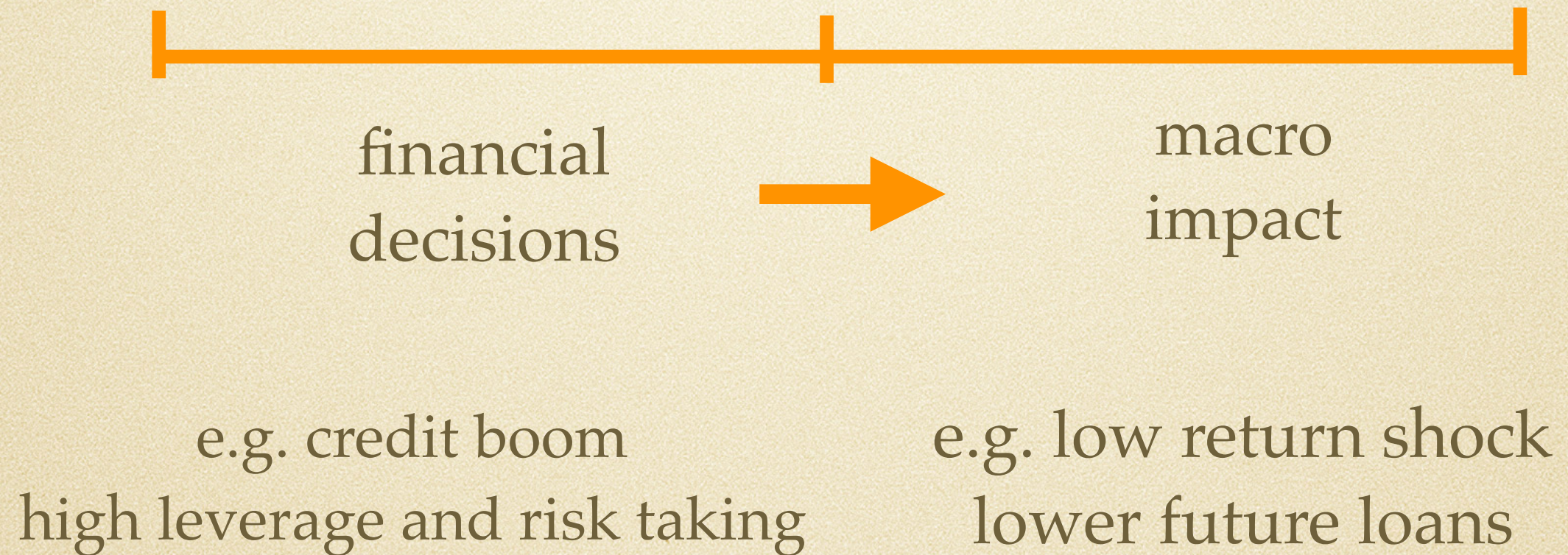
Macprudential Policy

- Macprudential policies motivation...
 - financial fragility
 - *aggregate demand* stabilization
 - monetary policy constraints or dilemmas
- Farhi-Werning (2013, 2014, 2015)...
 - Applications: capital controls, fiscal unions, deleveraging
 - General model: pecuniary + demand externalities
 - Formula: MPCs + Wedges
- New Today...
 - Financial intermediaries a la He-Krishnamurthy
 - Non-rational expectations, extrapolation

Main New Ingredients

- Financial Intermediaries
 - expert banks intermediate for households (He-Krishnamurthy, Gertler-Kiyotaki, Holmstrom-Tirole, etc.)
 - risk-taking capacity (capital requirements)
- Irrational Expectations
 - Credit and Financial Cycle (Jordà-Schularick-Taylor, López-Salido-Stein-Zakrajšek, Borio)
 - Diagnostic / Extrapolative Expectations evidence (Bordalo-Gennaioli-Ma-Shleifer)

Macprudential



Macprudential

macropru regulation



financial
decisions



macro
impact

e.g. credit boom
high leverage and risk taking

e.g. low return shock
lower future loans

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Is there a market failure?

Not necessarily.

Externality needed.

Macprudential

monetary policy?

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e.g. credit boom
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Is there a market failure?

Not necessarily.

Externality needed.

Policy Debate

- A debate...
 - **Monetary policy:** Use monetary policy to lean against credit booms (e.g. BIS view, Borio, Stein, ...)
 - **Macroprudential policy:** Monetary policy focused on targeting inflation and employment, other macroprudential policies and regulations should be used instead (e.g. Krugman, Evans, Svensson, ...)

General Model

- Farhi-Werning (2013, 2014, 2016)
- Arrow-Debreu with frictions:
 - price rigidities
 - constraints on monetary policy
- Instruments:
 - monetary policy
 - macroprudential policy
- Constrained efficient allocations (2nd best)

Results

- Monetary policy not sufficient...
 - private financial decisions
 - ➡ **aggregate demand externalities**
 - ... macroprudential policies beneficial
- Formula for optimal policies...
 - intuition
 - sufficient statistics: MPCs and wedges

Results

- Financial Intermediaries...
 - limited risk capacity
 - optimal macroprudential policy limits leverage (capital requirements)
 - monetary policy: IT / output gap target
- Irrational Beliefs...
 - rationale for deviating monetary policy
 - further motive for macropru
 - both paternalistic vs. non-paternalistic welfare

	Monetary	Monetary + Macropu
Rational Expectation		

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Rational Expectation	IT	

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Extrapolative Expectations		

	Monetary	Monetary + Macropru
Rational Expectation	IT	IT + Macropru
Extrapolative Expectations	Lean Against Boom	

	Monetary	Monetary + Macropru
Rational Expectation	IT	IT + Macropru
Extrapolative Expectations	Lean Against Boom	Lean Against Boom + Macropru

Outline

- General Model
- Financial Intermediaries
- Non-Rational Expectations

General Model

Farhi-Werning (2016)

- Agents $i \in I$
- Goods $\{X_{j,s}^i\}$ indexed by...
 - "state" $s \in S$
 - commodity $j \in J_s$
- "States":
 - states, periods
 - trade across states...financial markets
 - taxes or quantity controls available

(preferences)

$$\sum_{s \in S} U^i(\{X_{j,s}^i\}; s)$$

(preferences)

$$\sum_{s \in S} U^i(\{X_{j,s}^i\}; s)$$

(technology)

$$F(\{Y_{j,s}\}) \leq 0$$

(preferences)

$$\sum_{s \in S} U^i(\{X_{j,s}^i\}; s)$$

$$\sum_{s \in S} D_s^i Q_s \leq \Pi^i$$

$$\sum_{j \in J_s} P_{j,s} X_{j,s}^i \leq -T_s^i + (1 + \tau_{D,s}^i) D_s^i$$

$$\{X_{j,s}^i\} \in B_s^i$$

(technology)

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borrowing
constraints

macroprudential
financial tax

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borrowing
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$$\Gamma(\{P_{j,s}\}) \leq 0$$

(nominal rigidities
and monetary policy)

(preferences)

$$\sum_{s \in S} U^i(\{X_{j,s}^i\}; s)$$

$$\sum_{s \in S} D_s^i Q_s \leq \Pi^i$$

$$\sum_{j \in J_s} P_{j,s} X_{j,s}^i \leq -T_s^i + (1 + \tau_{D,s}^i) D_s^i$$

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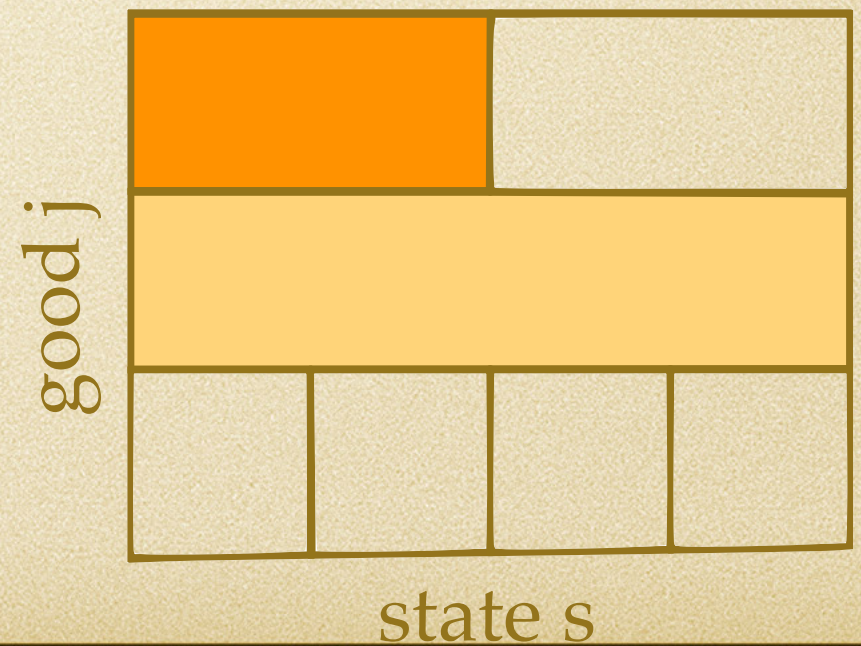
$$\{X_{j,s}^i\} \in B_s^i$$

(technology)

$$F(\{Y_{j,s}\}) \leq 0$$

$$\Gamma(\{P_{j,s}\}) \leq 0$$

(nominal rigidities
and monetary policy)



Equilibrium

1. Agents optimize
2. Government budget constraint satisfied
3. Technologically feasible
4. Markets clear
5. Nominal rigidities

Wedges

- Define wedges $\tau_{j,s}$ given reference good $j^*(s)$

$$\frac{P_{j^*(s),s}}{P_{j,s}} \frac{F_{j,s}}{F_{j^*(s),s}} = 1 - \tau_{j,s}$$

- First best... $\tau_{j,s} = 0$

Proposition (Corrective Financial Taxes).


$$\frac{\tau_{D,s}^i}{1 + \tau_{D,s}^i} = \sum_{j \in J_s} P_{j,s} X_{I,j,s}^i \tau_{j,s}$$

- Macropuru formula: linked to MPCs and wedges
- Result extends with...
 - incomplete markets, financial constraints with prices etc. (pecuniary externalities)
 - affect monetary policy condition, but not macropuru

Aggregate Demand Externalities

- Assume “state” where depressed economy
- Force agents with high propensity to spend to move income to that “state” ...
- ... increases spending...income...spending....
- ...stabilization benefits...
- ...not internalized by private agents

Aggregate Demand Externalities

- Assume “state” where depressed economy
- Force agents with high propensity to spend to move income to that “state” ...
 Keynesian cross
- ... increases spending...income...spending....
- ...stabilization benefits...
- ...not internalized by private agents

Financial Intermediaries

Financial Intermediaries

- He-Krishnamurthy (2013)
 - asset pricing model
 - adds nominal rigidities + optimal policy
- Incomplete markets...
 - risky asset (Lucas tree)
 - risk-free short-term bond
- Two agents...
 - households: save risk-free
 - bankers/experts
 - invest in risky asset
 - borrow risk-free
- Three periods $t=0,1,2$
- Consumption good produced 1-to-1 with labor
- Rigid wages, no inflation

Demand Determined Output
(rigid wage)

Endowment

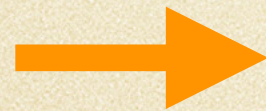
$t = 0$

$t = 1$

$t = 2$



household
borrow
from banks



ZLB binds

risky return
realized

Households and Bankers

- Household and Bankers: fractions ϕ^B and ϕ^H

- utility

$$\log c_0 - h(y_1) + \beta(\log c_1 - h(y_2)) + \beta^2 \log c_2$$

- budget constraint

$$c_t + q_t b_{t+1} + P_t a_{t+1} = y_t + b_t + (D_t + P_t) a_t$$

- Market segmentation

- households $a_t = 0$

- bankers a_t unrestricted

- Risky asset $D_0 = D_1 = 0$

Equilibrium

- All agents equally rationed in labor market $y_t = Y_t$
- Bankers hold all risky assets
- Households
 - save in risk free
 - constant fraction of wealth (log utility)
- Assuming ZLB binds at $t=1$ then $q_1 = 1$
- Policy instruments
 - monetary policy: q_0
 - macroprudential policy: B_1
 - redistributive taxes
- Solve equilibrium backwards from $t=1,2$, then planner

- Consumption at t=1

$$c_1^H = (1 - \beta)(B_1 + Y_1)$$

$$c_1^B = (1 - \beta)\left(\frac{P_1}{\phi^B} + Y_1 - \frac{\phi^H}{\phi^B} B_1\right)$$

$$c_2^B = \frac{D_2}{\phi^B} - \beta\left(\frac{\phi^H}{\phi^B} B_1 + \frac{\phi^H}{\phi^B} Y_1\right)$$

- Euler equations for Banker

$$\frac{1}{c_1^B} = \frac{\beta}{1 - \beta} E \left[\frac{\phi^B}{D_2 - \beta(\phi^H B_1 + \phi^H Y_1)} \right]$$

$$\frac{1}{c_1^B} = \frac{\beta}{1 - \beta} E \left[\frac{D_2}{P_1} \frac{\phi^B}{D_2 - \beta(\phi^H B_1 + \phi^H Y_1)} \right]$$

- Output

$$Y_1 = \phi^H c_1^H + \phi^B c_1^B$$

$$Y_1 = (1 - \beta)(\phi^H B_1 + \phi^H Y_1) + \frac{1 - \beta}{\beta} \frac{1}{E \left[\frac{1}{D_2 - \beta(\phi^H B_1 + \phi^H Y_1)} \right]}$$

- Output

$$Y_1 = \phi^H c_1^H + \phi^B c_1^B$$

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$$\frac{\partial Y_1}{\partial B_1} = \frac{\phi^H (1 - \beta) \left[1 - \frac{E \left[\frac{1}{D_2 - \beta(\phi^H B_1 + \phi^H Y_1)} \right]^2}{\left[E \left[\frac{1}{D_2 - \beta(\phi^H B_1 + \phi^H Y_1)} \right] \right]^2} \right]}{1 - \phi^H (1 - \beta) \left[1 - \frac{E \left[\frac{1}{D_2 - \beta(\phi^H B_1 + \phi^H Y_1)} \right]^2}{\left[E \left[\frac{1}{D_2 - \beta(\phi^H B_1 + \phi^H Y_1)} \right] \right]^2} \right]} < 0$$

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zero if no risk!

Intuition

- Output and Asset Price are linked...

$$Y_1 = (1 - \beta)(P_1 + Y_1)$$

$$\frac{\partial P_1}{\partial B_1} = \frac{\beta}{1 - \beta} \frac{\partial Y_1}{\partial B_1} < 0$$

- Two intuitions...
 - higher debt lower risk-taking capacity
 → higher risk premia → lower asset price
 → lower consumption
 - higher debt → higher precautionary motive
 → lower natural rate → lower consumption
- Risk always key here; without it, no effect.

Planning problem

- Value functions for $t=1,2$

$$V^H(B_1) = (1 - \beta) \log[(1 - \beta)(B_1 + Y_1(B_1))] \\ - (1 - \beta)h(Y_1(B_1)) + \beta \log[\beta(B_1 + Y_1(B_1))]$$

$$V^B(B_1) = (1 - \beta) \log[(1 - \beta)(\frac{1}{\phi^B} P_1(B_1) + Y_1(B_1) - \frac{\phi^H}{\phi^B} B_1)] - (1 - \beta)h(Y_1(B_1)) \\ + \beta E \left[\log[(\frac{1}{\phi^B} D_2 - \frac{\phi^H}{\phi^B} \beta(B_1 + Y_1(B_1)))] \right].$$

Monetary Policy

- Euler at $t=0$

$$1 = \frac{\beta}{1 - \beta} \frac{c_0^i}{c_1^i} R$$

- Guess and verify
 - $R=1/q$ affects c_0 but NOT c_1 nor B_1 ...
 - more general result (Werning, 2015 “IMAD”)
 - neutrality depends on log utility, but can go either way

Monetary Policy.

Cannot affect B_1 .

Optimum targets labor wedge at $t=0$.

	Monetary	Monetary + Macropu
Rational Expectation	IT	
Extrapolative Expectations		

$$\begin{aligned} \max \phi^H \lambda^H & [(1 - \beta) \log(c_0^H) - (1 - \beta)h(Y_0) + \beta V^H(B_1)] \\ & + \phi^B \lambda^B [(1 - \beta) \log(c_0^B) - (1 - \beta)h(Y_0) + \beta V^B(B_1)] \end{aligned}$$

$$\phi^H c_0^H + \phi^L c_0^B = Y_0$$

$$\begin{aligned} \max \phi^H \lambda^H [(1 - \beta) \log(c_0^H) - (1 - \beta)h(Y_0) + \beta V^H(B_1)] \\ + \phi^B \lambda^B [(1 - \beta) \log(c_0^B) - (1 - \beta)h(Y_0) + \beta V^B(B_1)] \end{aligned}$$

$$\phi^H c_0^H + \phi^L c_0^B = Y_0$$

$$\lambda^H \frac{1 - \beta}{c_0^H} = \lambda^B \frac{1 - \beta}{c_0^B} = \phi^H \lambda^H (1 - \beta) h'(Y_0) + \phi^B \lambda^B (1 - \beta) h'(Y_0)$$

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$$\tau_{0,L} = 0$$

$$\tau_{0,L} = \frac{\phi^H \lambda^H \frac{\tau_{0,L}^H}{1 - \tau_{0,L}^H} + \phi^B \lambda^B \frac{\tau_{0,L}^B}{1 - \tau_{0,L}^B}}{\phi^H \lambda^H + \phi^B \lambda^B}$$

$$\lambda^H \frac{1}{c_0^H} = \lambda^B \frac{1}{c_0^B}$$

$$\phi^H \lambda^H V^{H'}(B_1) + \phi^B \lambda^B V^{B'}(B_1) = 0$$



$$\lambda^H \frac{1}{c_0^H} = \lambda^B \frac{1}{c_0^B}$$

$$\phi^H \lambda^H V^{H'}(B_1) + \phi^B \lambda^B V^{B'}(B_1) = 0$$



$$\frac{c_0^H}{c_1^H} \left[1 + \tau_{1,L} Y_1'(B_1) \frac{\phi^H \lambda^H + \phi^B \lambda^B}{\phi^H \lambda^H} \frac{1 - \tau_{1,L}^H}{1 - \tau_{1,L}} \right] = \frac{c_0^B}{c_1^B}$$



$$\lambda^H \frac{1}{c_0^H} = \lambda^B \frac{1}{c_0^B}$$

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shadow tax on borrowing for banks



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shadow tax on borrowing for banks

- Negative effect on output from higher debt not internalized by private agents



discourage borrowing by banks

Optimal Policy:

1. Macroprou: Binding leverage / capital requirement.
2. Monetary policy: targets zero labor wedge.

- Maps into general framework
 - results broadly in line with previous applications
 - now connects with broad macro-finance literature
- Model very stylized, but likely generalizes

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Rational Expectation		

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Extrapolative Expectations		

Extrapolative Expectations

Extrapolative Expectations

- Two states G and B

$$D_{2G} > D_{2B}$$

- Probabilities...

- subjective

- objective

(π_G, π_B)

$(\bar{\pi}_G, \bar{\pi}_B)$

$$\mathbb{E}_t^{sub} R_{t+1} = (1 - \lambda) \mathbb{E}_t^{obj} R_{t+1} + \lambda R_t$$

- Can do this for

- $t=0$ irrational exuberance **TODAY**

- $t=1$ irrational pessimism

Planning Problem

- Policy tools: just as before
 - monetary policy at $t=0$
 - macropru at $t=0$
 - redistribution
- Two planning problems:
 - non-paternalistic: respect subjective beliefs
 - paternalistic: use objective beliefs

Feedback

- System as before, but with subjective beliefs

$$Y_1 = (1 - \beta)(\phi^H B_1 + \phi^H Y_1) + \frac{1 - \beta}{\beta} \frac{1}{E \left[\frac{1}{D_2 - \beta(\phi^H B_1 + \phi^H Y_1)} \right]}$$
$$P_1 = \frac{\beta}{1 - \beta} Y_1$$

- note: now P_1 feeds back into $E[.]$!
- solution: $Y_1(B_1, P_0) \quad P_1(B_1, P_0)$

$$\frac{\partial Y_1}{\partial B_1} = \frac{\phi^H(1-\beta) \left[1 - \frac{E \left[\frac{1}{D_2 - \beta(\phi^H B_1 + \phi^H Y_1)} \right]^2}{\left[E \left[\frac{1}{D_2 - \beta(\phi^H B_1 + \phi^H Y_1)} \right] \right]^2} \right]}{1 - \phi^H(1-\beta) \left[1 - \frac{E \left[\frac{1}{D_2 - \beta(\phi^H B_1 + \phi^H Y_1)} \right]^2}{\left[E \left[\frac{1}{D_2 - \beta(\phi^H B_1 + \phi^H Y_1)} \right] \right]^2} \right] - \frac{\frac{\partial \pi_G}{\partial P_1} \left[\frac{1}{D_{2B} - \beta(\phi^H B_1 + \phi^H Y_1)} - \frac{1}{D_{2G} - \beta(\phi^H B_1 + \phi^H Y_1)} \right]}{\left[E \left[\frac{1}{D_2 - \beta(\phi^H B_1 + \phi^H Y_1)} \right] \right]^2}} < 0$$

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extra negative term due to feedback on expectations!

$$\frac{\partial Y_1}{\partial B_1} = \frac{\phi^H (1 - \beta) \left[1 - \frac{E \left[\frac{1}{D_2 - \beta(\phi^H B_1 + \phi^H Y_1)} \right]^2}{\left[E \left[\frac{1}{D_2 - \beta(\phi^H B_1 + \phi^H Y_1)} \right] \right]^2} \right]}{1 - \phi^H (1 - \beta) \left[1 - \frac{E \left[\frac{1}{D_2 - \beta(\phi^H B_1 + \phi^H Y_1)} \right]^2}{\left[E \left[\frac{1}{D_2 - \beta(\phi^H B_1 + \phi^H Y_1)} \right] \right]^2} \right] - \frac{\frac{\partial \pi_G}{\partial P_1} \left[\frac{1}{D_{2B} - \beta(\phi^H B_1 + \phi^H Y_1)} - \frac{1}{D_{2G} - \beta(\phi^H B_1 + \phi^H Y_1)} \right]}{\left[E \left[\frac{1}{D_2 - \beta(\phi^H B_1 + \phi^H Y_1)} \right] \right]^2}} < 0$$

extra negative term due to feedback on expectations!

higher asset price now makes agents more optimistic...
.... further increasing asset price and output

$$\frac{\partial Y_1}{\partial B_1} = \frac{\phi^H (1 - \beta) \left[1 - \frac{E \left[\frac{1}{D_2 - \beta(\phi^H B_1 + \phi^H Y_1)} \right]^2}{\left[E \left[\frac{1}{D_2 - \beta(\phi^H B_1 + \phi^H Y_1)} \right] \right]^2} \right]}{1 - \phi^H (1 - \beta) \left[1 - \frac{E \left[\frac{1}{D_2 - \beta(\phi^H B_1 + \phi^H Y_1)} \right]^2}{\left[E \left[\frac{1}{D_2 - \beta(\phi^H B_1 + \phi^H Y_1)} \right] \right]^2} \right] - \frac{\frac{\partial \pi_G}{\partial P_1} \left[\frac{1}{D_{2B} - \beta(\phi^H B_1 + \phi^H Y_1)} - \frac{1}{D_{2G} - \beta(\phi^H B_1 + \phi^H Y_1)} \right]}{\left[E \left[\frac{1}{D_2 - \beta(\phi^H B_1 + \phi^H Y_1)} \right] \right]^2}} < 0$$

extra negative term due to feedback on expectations!

higher asset price now makes agents more optimistic...
.... further increasing asset price and output

no longer directly dependent on risk and prudence

$$\frac{\partial Y_1}{\partial B_1} = \frac{\phi^H (1 - \beta) \left[1 - \frac{E \left[\frac{1}{D_2 - \beta(\phi^H B_1 + \phi^H Y_1)} \right]^2}{\left[E \left[\frac{1}{D_2 - \beta(\phi^H B_1 + \phi^H Y_1)} \right] \right]^2} \right]}{1 - \phi^H (1 - \beta) \left[1 - \frac{E \left[\frac{1}{D_2 - \beta(\phi^H B_1 + \phi^H Y_1)} \right]^2}{\left[E \left[\frac{1}{D_2 - \beta(\phi^H B_1 + \phi^H Y_1)} \right] \right]^2} \right] - \frac{\frac{\partial \pi_G}{\partial P_1} \left[\frac{1}{D_{2B} - \beta(\phi^H B_1 + \phi^H Y_1)} - \frac{1}{D_{2G} - \beta(\phi^H B_1 + \phi^H Y_1)} \right]}{\left[E \left[\frac{1}{D_2 - \beta(\phi^H B_1 + \phi^H Y_1)} \right] \right]^2}} < 0$$

extra negative term due to feedback on expectations!

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$$\frac{\partial Y_1}{\partial P_0} = \frac{1 - \beta}{\beta} \frac{\frac{\partial \pi_G}{\partial P_0} \left[\frac{1}{D_{2B} - \beta(\phi^H B_1 + \phi^H Y_1)} - \frac{1}{D_{2G} - \beta(\phi^H B_1 + \phi^H Y_1)} \right]}{\left[E \left[\frac{1}{D_2 - \beta(\phi^H B_1 + \phi^H Y_1)} \right] \right]^2} < 0$$

$$\frac{\partial Y_1}{\partial B_1} = \frac{\phi^H (1 - \beta) \left[1 - \frac{E \left[\frac{1}{D_2 - \beta(\phi^H B_1 + \phi^H Y_1)} \right]^2}{\left[E \left[\frac{1}{D_2 - \beta(\phi^H B_1 + \phi^H Y_1)} \right] \right]^2} \right]}{1 - \phi^H (1 - \beta) \left[1 - \frac{E \left[\frac{1}{D_2 - \beta(\phi^H B_1 + \phi^H Y_1)} \right]^2}{\left[E \left[\frac{1}{D_2 - \beta(\phi^H B_1 + \phi^H Y_1)} \right] \right]^2} \right] - \frac{\frac{\partial \pi_G}{\partial P_1} \left[\frac{1}{D_{2B} - \beta(\phi^H B_1 + \phi^H Y_1)} - \frac{1}{D_{2G} - \beta(\phi^H B_1 + \phi^H Y_1)} \right]}{\left[E \left[\frac{1}{D_2 - \beta(\phi^H B_1 + \phi^H Y_1)} \right] \right]^2}} < 0$$

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$$\frac{\partial Y_1}{\partial P_0} = \frac{1 - \beta}{\beta} \frac{\frac{\partial \pi_G}{\partial P_0} \left[\frac{1}{D_{2B} - \beta(\phi^H B_1 + \phi^H Y_1)} - \frac{1}{D_{2G} - \beta(\phi^H B_1 + \phi^H Y_1)} \right]}{\left[E \left[\frac{1}{D_2 - \beta(\phi^H B_1 + \phi^H Y_1)} \right] \right]^2} < 0$$

analogously, if previous boom was higher
crash is bigger

Planning Problem

- Policy tools: just as before
 - monetary policy at $t=0$
 - macropru at $t=0$
 - redistribution
- Two planning problems:
 - non-paternalistic: respect subjective beliefs
 - paternalistic: use objective beliefs

Planning Problem

$$\max \phi^H \lambda^H [(1 - \beta) \log(c_0^H) - (1 - \beta)h(Y_0) + \beta V^H(P_0, B_1)] \\ + \phi^B \lambda^B [(1 - \beta) \log(c_0^B) - (1 - \beta)h(Y_0) + \beta V^B(P_0, B_1)]$$

$$\phi^H c_0^H + \phi^B c_0^B = Y_0$$

$$c_0^B = c_0^B(P_0, B_1)$$

with

$$\frac{\phi^B c_0^B(P_0, B_1)}{(1 - \beta)(P_1(P_0, B_1) + \phi^B Y_1(P_0, B_1) - \phi^H B_1)} \frac{\beta}{1 - \beta} \frac{P_1(P_0, B_1)}{P_0} = 1$$

Planning Problem

$$\max \phi^H \lambda^H [(1 - \beta) \log(c_0^H) - (1 - \beta)h(Y_0) + \beta V^H(P_0, B_1)] \\ + \phi^B \lambda^B [(1 - \beta) \log(c_0^B) - (1 - \beta)h(Y_0) + \beta V^B(P_0, B_1)]$$

$$\phi^H c_0^H + \phi^B c_0^B = Y_0$$

Irrational beliefs

$$c_0^B = c_0^B(P_0, B_1)$$

with

$$\frac{\phi^B c_0^B(P_0, B_1)}{(1 - \beta)(P_1(P_0, B_1) + \phi^B Y_1(P_0, B_1) - \phi^H B_1)} \frac{\beta}{1 - \beta} \frac{P_1(P_0, B_1)}{P_0} = 1$$

- First order condition

$$\lambda^H \frac{1 - \beta}{c_0^H} = \lambda^B \frac{1 - \beta}{c_0^B} - \frac{\nu}{\phi^B} = \phi^H \lambda^H (1 - \beta) h'(Y_0) + \phi^B \lambda^B (1 - \beta) h'(Y_0)$$

- First order condition

$$\lambda^H \frac{1-\beta}{c_0^H} = \lambda^B \frac{1-\beta}{c_0^B} - \frac{\nu}{\phi^B} = \phi^H \lambda^H (1-\beta) h'(Y_0) + \phi^B \lambda^B (1-\beta) h'(Y_0)$$

for small enough λ

$$\longrightarrow \tau_{0,L} = \nu \frac{1-\beta}{\phi^H \lambda^H + \phi^B \lambda^B} h'(Y_0) > 0$$

- First order condition

$$\lambda^H \frac{1-\beta}{c_0^H} = \lambda^B \frac{1-\beta}{c_0^B} - \frac{\nu}{\phi^B} = \phi^H \lambda^H (1-\beta) h'(Y_0) + \phi^B \lambda^B (1-\beta) h'(Y_0)$$

for small enough λ

$$\longrightarrow \tau_{0,L} = \nu \frac{1-\beta}{\phi^H \lambda^H + \phi^B \lambda^B} h'(Y_0) > 0$$

- Monetary policy tighter at $t=0$
- Intuition...
 - lower Y_0
 - lowers P_0
 - drop in price, less overreaction

Paternalistic Planner

- Now assume planner computes expected utility with objective probabilities
- Behavior still driven by subjective beliefs

Optimal Policy:

1. Macropru: Binding leverage / capital requirement.
2. Monetary policy tighter than zero labor wedge

Extrapolation $t=0,1$

- Previously low price makes you optimistic
- Now assume extrapolation is earlier

$$\frac{P_1^e}{P_0} = (1 - \lambda) \frac{P_1}{P_0} + \lambda \frac{P_0}{P_{-1}}$$

define

$$P_1^e(B_1, P_0) = (1 - \lambda) P_1(B_1) + \lambda \frac{P_0^2}{P_{-1}}$$

- As before

$$Y_1^e(B_1, P_0) = \frac{1 - \beta}{\beta} P_1^e(B_1, P_0)$$

- In background: create subject beliefs about dividends that justify these beliefs about prices

Results

- Now:
 - beliefs and ZLB no longer interact
 - does not change outlook at $t=1$
- Result:
 - standard macropru + undo wrong beliefs
 - ... even stronger macropru

Optimal Policy:

1. Macropru: Binding leverage / capital requirement.
2. Monetary policy targets zero labor wedge.

Conclusion

- General theory of macropru + monetary policy
 - workhorse for many applications
 - general formula: MPCs and wedges
- Financial Intermediaries
 - macroprudential capital requirements to protect risk-taking capacity
 - intuitions: via asset price and / or natural rate
- Non-Rational Expectations
 - expectation management: interventions attempt to mitigate financial crashes in prices
 - dilemma: may affect monetary policy

	Monetary	Monetary + Macropu
Rational Expectation		

	Monetary	Monetary + Macropu
Rational Expectation	IT	

	Monetary	Monetary + Macropu
Rational Expectation	IT	IT + Macropu

	Monetary	Monetary + Macropu
Rational Expectation	IT	IT + Macropu
Extrapolative Expectations		

	Monetary	Monetary + Macropru
Rational Expectation	IT	IT + Macropru
Extrapolative Expectations	Lean Against Boom	

	Monetary	Monetary + Macropru
Rational Expectation	IT	IT + Macropru
Extrapolative Expectations	Lean Against Boom	