

# Optimal Progressivity with Age-Dependent Taxation (by HSV)

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# Motivation

- Classic Question: How progressive should income taxation be?
- In a recent paper (QJE 2017) authors, find little role for progressive income taxation.
- Literature: In general, as long as hours/consumption of households vary over their life cycle, there are gains from allowing *taxes to depend on age* both in
  - Ramsey-approach
  - Dynamic-Mirrlees setting
- **Key idea of paper:** Bigger role for redistribution/insurance policies under age-dependent-progressive income taxation.

Contribution: evaluate welfare gains of optimal **age-dependent** non-linear taxation in a framework with the following tradeoffs

- favoring progressivity
  - redistribution with respect to initial conditions
  - intertemporal redistribution (life-cycle) due to borrowing constraints.
  - social insurance due to missing markets
- against progressivity
  - labor supply distortion
  - human capital distortion.

## Welfare Gains

- Equivalent variation: % of lifetime consumption
- Computed **relative to the US tax/transfer system**

	Benchmark	U.S. BL	Natural BL
$(\lambda^*, \tau^*)$ constant	0.04	0.15	0.15
$\lambda^*$ age-varying, $\tau^*$ constant	3.00	1.88	1.43
$(\lambda^*, \tau^*)$ age-varying	3.70	2.12	1.47

## Why are gains of age-dependent taxes so large?

Labor supply is determined by FOC

$$\frac{1}{c} \frac{d[y - T(y)]}{dh} = \varphi h^\sigma$$

Using  $c = \lambda y^{1-\tau}$  yields:

$$(1 - \tau) \frac{1}{h} = \varphi h^\sigma$$

- Hours depend on preferences  $(\varphi, \sigma)$ , tax parameter  $\tau$ .
- $\tau = 0$  no distortion on labor supply.
- Optimal tax system will set  $\tau = 0$  at the age when individuals are the most productive (net of disutility cost of labor)

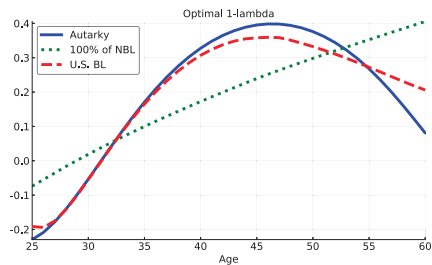
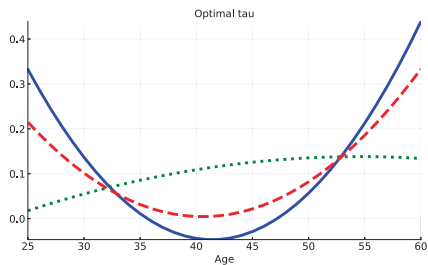
## Non-linear consumption prices ( $\tau \neq 0$ )

- Tax system imply:  $c = \lambda[\text{after tax cost of } c]^{1-\tau}$
- Average price of consuming  $c$  goods at age  $a$ :

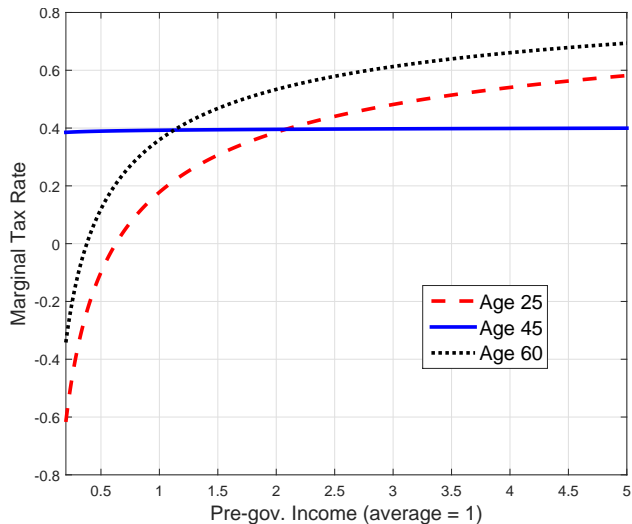
$$p_a^c = \frac{\text{after tax cost of } c}{c} = \frac{\lambda_a}{c^{\tau_a}}$$

- age variation in  $\lambda_a$  important for redistribution over the life cycle.
- $\tau_a >$  allows for social social insurance.
- Key: age-dependent taxes allow for more redistribution/insurance.

# No distortion at the top



# No distortion at the top



Age-dependent taxes reduce labor distortions allowing for more redistribution/insurance.



## Comments on explanation of findings

Paper has an extensive discussion on how different model features affect age-profile of tax parameters ( $\{\lambda_a, \tau_a\}_{a=25}^{60}$ ).

- How do model features affect welfare gains? (nice summary statistic)
- How do welfare gains vary across initial types? (high learning types may not like age-dependent taxes!)
- Report statistics on moments of labor wedges and intertemporal wedges.
- Compare answers to question above in age-dependent versus age-independent tax system

## Discussion on Intertemporal Wedge

- Tax function is effectively a progressive consumption tax:  
$$c_a = \lambda_a [p(s) \exp(x_a + \alpha) h_a + (1 + r)b_a - b'_a]^{1 - \tau_a}.$$
- Consider Euler equation in a model with linear taxation on consumption:

$$\frac{u'(c_a)}{1 + \tau_a^c} = \beta(1 + r) \frac{u'(c_{a+1})}{1 + \tau_{a+1}^c}$$
$$u'(c_a) = \beta(1 + r) \underbrace{\frac{1 + \tau_a^c}{1 + \tau_{a+1}^c}}_{1 + r(1 - \tau_a^k)} u'(c_{a+1})$$

- An interest income tax  $\tau_a^k$  gives exactly the same intertemporal tradeoff.
- $\tau_{a+1}^c > \tau_a^c \Rightarrow \tau_a^k > 0.$

▷ Consumption taxes should play a crucial role in an economy with capital (tax capital of initial old!).

## Discussion on US Tax Function

Paper estimates a tax function for the US that fits pretty well data on effective taxes paid at different level of incomes.

- Welfare benefits of reforms are compared relative to US estimated tax function.
- However, I suspect that tax function understates tax distortions in the US. Why?
- If so, welfare gains of tax reforms in the paper may be much larger.
- Alternative baseline: Solve for the initial equilibrium under us statutory tax rates (various tax brackets) and allow for a fixed deduction for each tax bracket (that might depend on age).
- Probably the US tax code has embedded age-dependent features: might be interesting to estimate a tax function that varies by age.

# Preferences

- Disutility from hours (rather than utility from leisure) imply
  - constant Frisch-elasticity of labor supply over the life cycle
  - all variation in labor supply is on the intensive margin
- Enhance role for age dependent taxation if model
  - preference for leisure.
  - retirement (extensive margin)

# Education

Probably the education decision is over-simplistic (utility cost, no modeling of time/goods input)

- Nonetheless, predictions of theory are consistent with standard results in taxation of human capital when human capital requires time inputs (linear taxes do not affect education decisions but progressive taxes do).
- Model can't address issues on the deductibility of expenditures in education.
- Life cycle profile or productivity and labor shocks might differ across education/occupation groups.

## Conclusions.

- Nice paper addressing an important question.
- Elegant and rich model that incorporate important tradeoffs.
- Transparent results.
- Large gains welfare from age-dependent progressive taxation.