

Demographic Trends and the Real Interest Rate

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Bank of England

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Key points

- Unprecedented **rise in life expectancy** in recent decades in advanced economies
- Understand the **macroeconomic impact** of this change in the composition of the population
- A key implication: fall in the **neutral interest rate**

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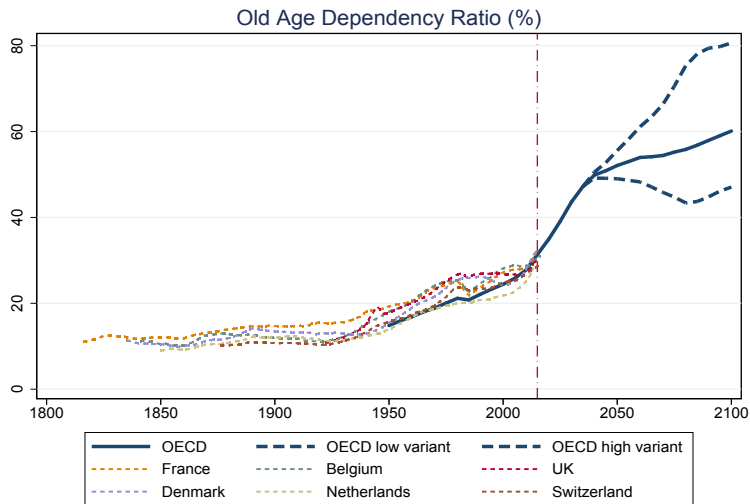
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- Understand the **macroeconomic impact** of this change in the composition of the population
- A key implication: fall in the **neutral interest rate**
- OLG model to **quantify** the effect of population ageing
- Across all advanced-countries, **ageing can explain**:
 - About 160bp of fall in **interest rates** since 1980, with a further 40bp still to come
 - More than 75% of the rise in **house prices** and **private credit** to GDP
 - Some of the **labour productivity** slow down since the 2000s
 - Just under 30% of the variation in **net foreign asset positions**

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 - Just under 30% of the variation in **net foreign asset positions**
- Without a reversal of life expectancy, these effects will be **permanent**

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- Intuition - The neutral rate in the neoclassical model
- Methodology - Outline of our model and calibration
- Results - Macroeconomic implications of population ageing
- Sensitivities - Robustness and Extensions
- Conclusions - Summary and some caveats

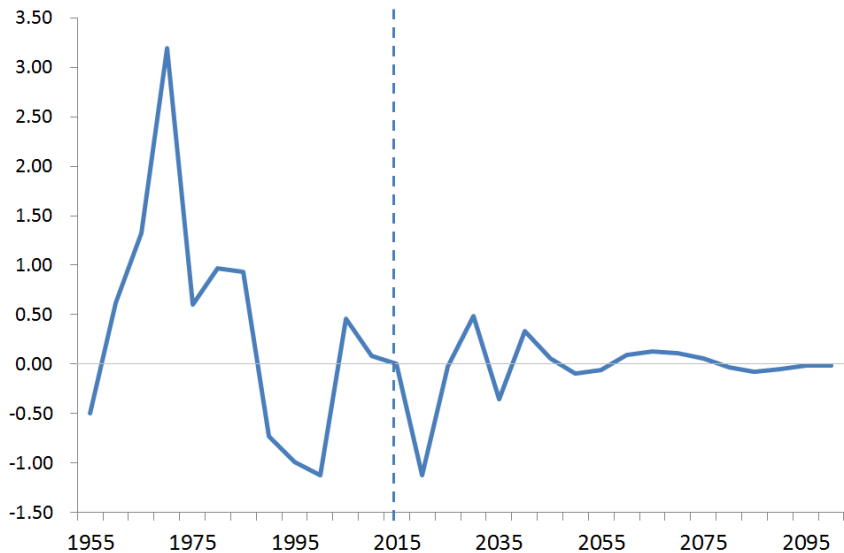
Unprecedented population ageing



Source: UN Population Statistics, Human Mortality Database

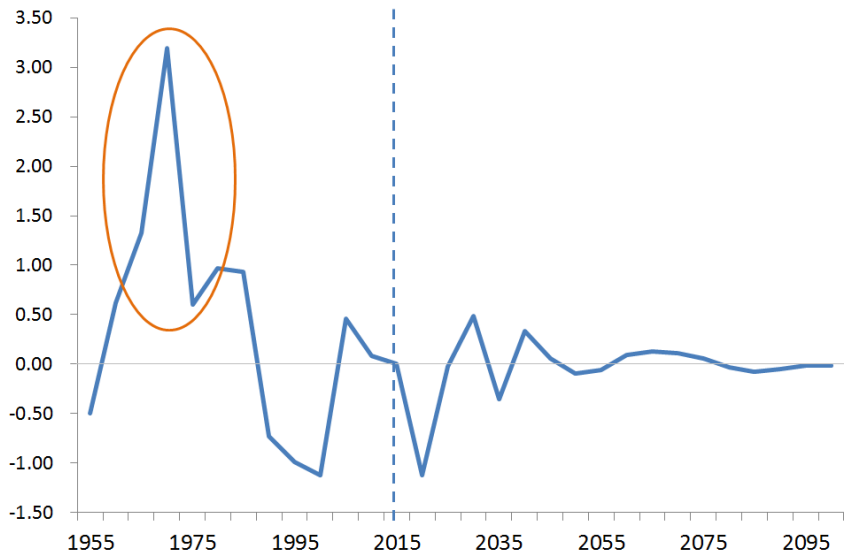
Population growth

Growth rate of 20-24 year old cohort

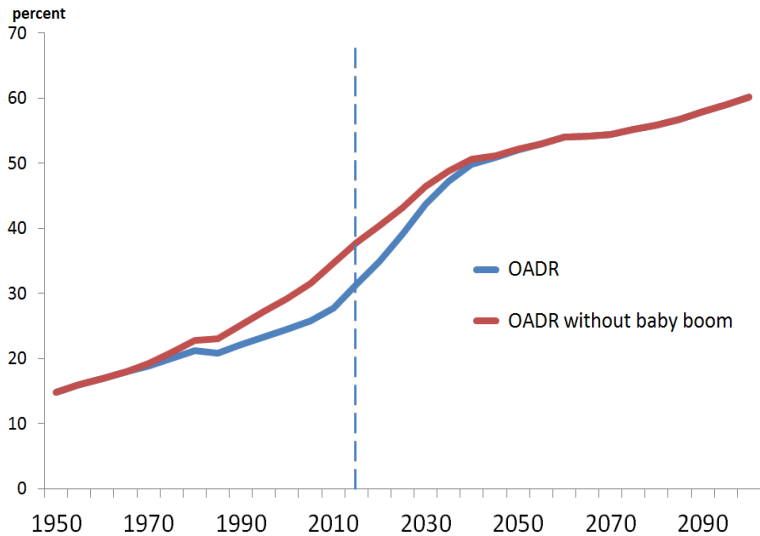


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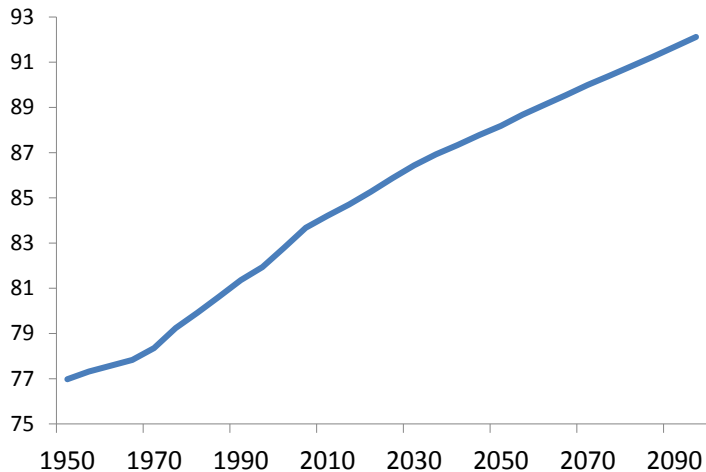


Baby boomers are not the main factor



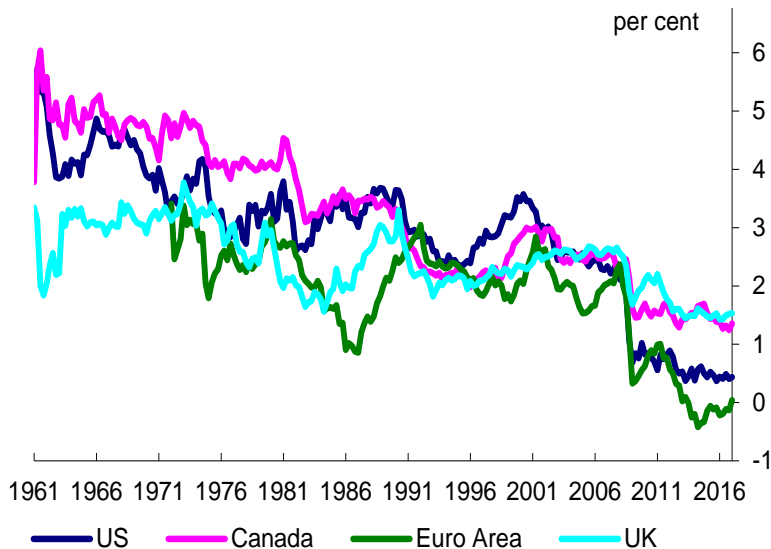
Source: UN Population Statistics, own calculations

Life expectancy at 60



Source: UN Population Statistics

Natural interest rate in advanced economies since 1960

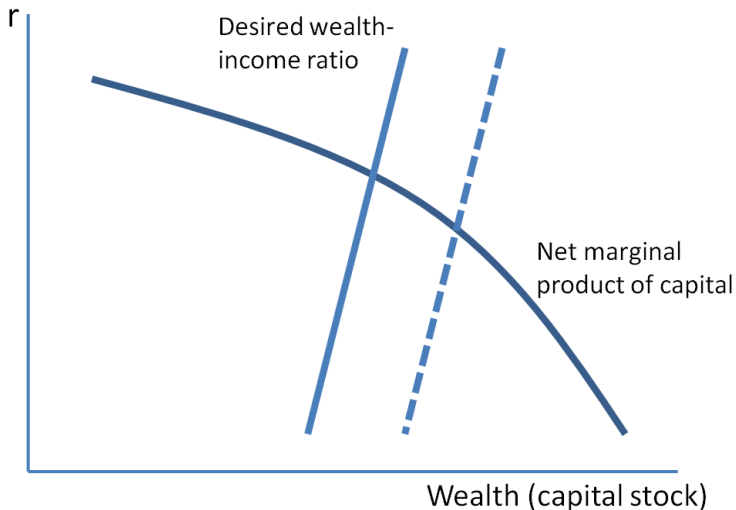


Source: Holston, Laubach and Williams (2017)

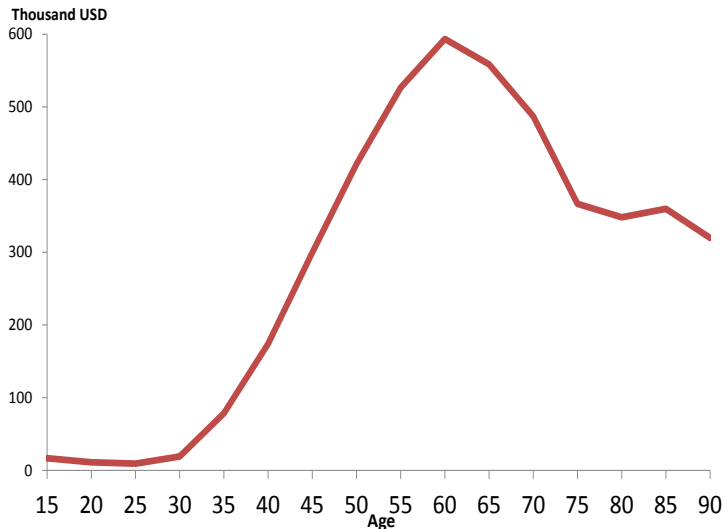
Plan for today

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Intuition: How demographics affect interest rates



Intuition: Age-wealth profile in the US



Source: Survey of Consumer Finances, Average Net Worth excl. Housing, 1989-2013

- Closed economy: Carvalho et al (2016), Eggertsson et al (2017), Gagnon et al (2016), Marx et al (2016)
- Open economy: Backus et al (2014), Domeij and Floden (2006), Krueger and Ludwig (2007)

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- **Calibrated neoclassical overlapping generations** model
- Households value **consumption, housing** and bequests
- They face a given **life-cycle profile of labour earnings**
- Net **savings of households invested** by firms
- Demographic change: variable **birth rates and life expectancy**
- Solved assuming **perfect foresight**

Model: Household's Problem

The household born at time t maximises:

$$\max_{\{c_{\tau,t}, a_{\tau,t}, h_{\tau,t}\}_{\tau=1}^T} \sum_{\tau=1}^T \beta_{\tau} \tilde{\psi}_{\tau,t} (\ln c_{\tau,t} + \theta_{\tau} \ln h_{\tau,t}) + \beta_T \tilde{\psi}_{T,t} \phi \ln a_{T,t}$$

subject to, for $\tau = 1, \dots, T$:

$$c_{\tau,t} + a_{\tau,t} + p_{t+\tau-1}^h (h_{\tau,t} - h_{\tau-1,t}) \leq w_{t+\tau-1} \epsilon_{\tau} l_{\tau,t} + (1 + r_{t+\tau-1}) a_{\tau-1,t} + \pi_{\tau,t}$$

τ : age ; t : birth year

$\tilde{\psi}_{\tau,t}$: survival probability up to age τ

Inelastic labor supply

Fixed number of periods when the household is able to “move”; otherwise, we impose $h_{\tau,t} = h_{\tau-1,t}$.

Model: Firm's Problem

At each period t , the firm maximises:

$$\max_{L_t, K_t} F(K_t, L_t) - w_t L_t - (r_t + \delta) K_t$$

$$F(K, L) = A \left[(1 - \alpha) L^{\frac{\sigma-1}{\sigma}} + \alpha K^{\frac{\sigma-1}{\sigma}} \right]^{\frac{\sigma}{\sigma-1}}$$

Model: Market Clearing

\tilde{X}_t : value of X_t per aggregate capita.

Market Clearing at every period t :

- Capital/Asset Market

$$\tilde{A}_{t-1} = \tilde{K}_t$$

- Labour Market

$$\tilde{\rho}' \epsilon \mathbf{1}_t = \tilde{L}_t$$

- Housing Market

$$\tilde{H}_t = \tilde{H}$$

- Goods Market

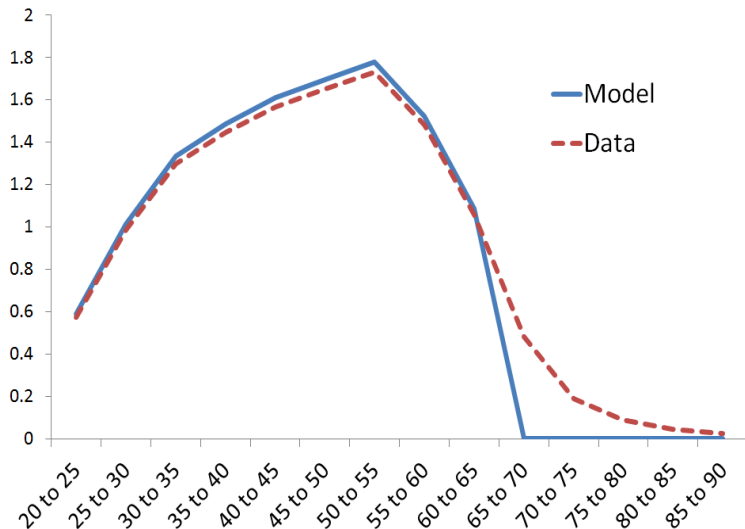
$$\tilde{Y}_t = \tilde{C}_t + \tilde{I}_t$$

Steady state exists in per capita terms.

Housing supply exogenously increases with total population size.

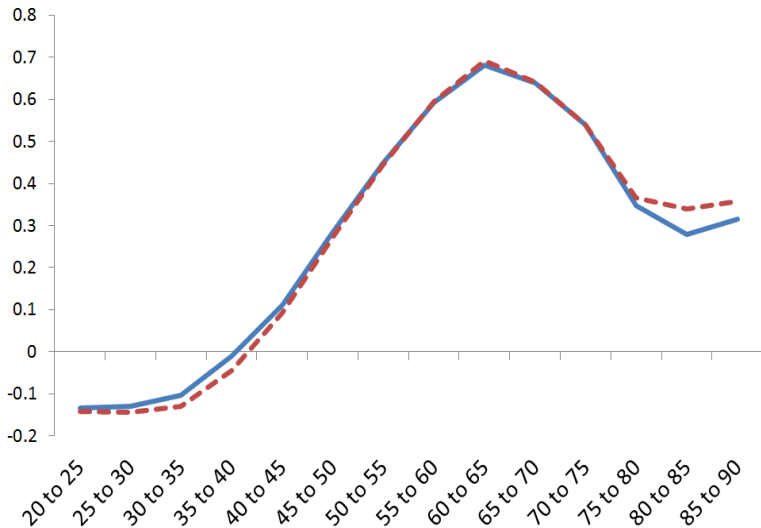
- Average **aggregate** values for advanced economies in the 1970s
 - World interest rate: 3.7%
 - Housing wealth/GDP ratio: 145%
 - Credit/GDP ratio: 45%
- **Life-cycle patterns** from the US Survey of Consumer Finances, from 1989 to 2013
 - Labour productivity
 - Net wealth (excluding housing)
 - Housing wealth
- **Demographics data** for advanced economies: Western Europe, North America, Japan, Australia, New Zealand [▶ details](#)

Calibration: Labour productivity



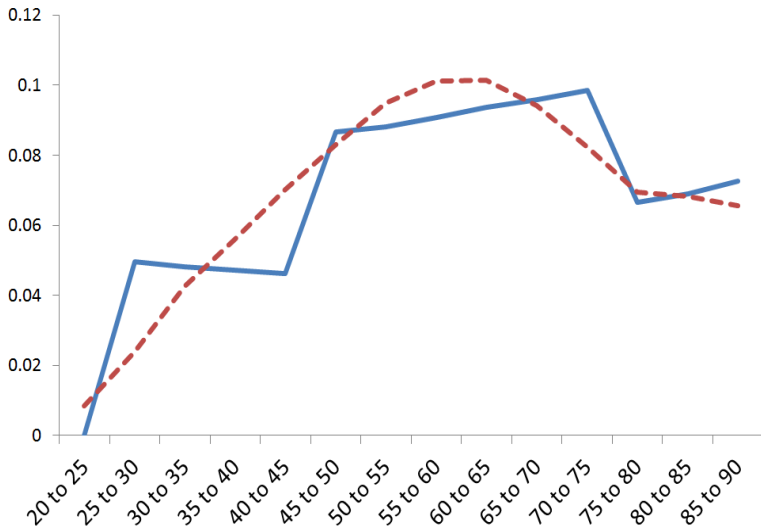
Source: Survey of Consumer Finances, Labour income, 1989-2013

Calibration: Net worth (excl. housing)



Source: Survey of Consumer Finances, Average Net Worth excl. Housing, 1989-2013

Calibration: Housing wealth



Source: Survey of Consumer Finances, Housing wealth, 1989-2013

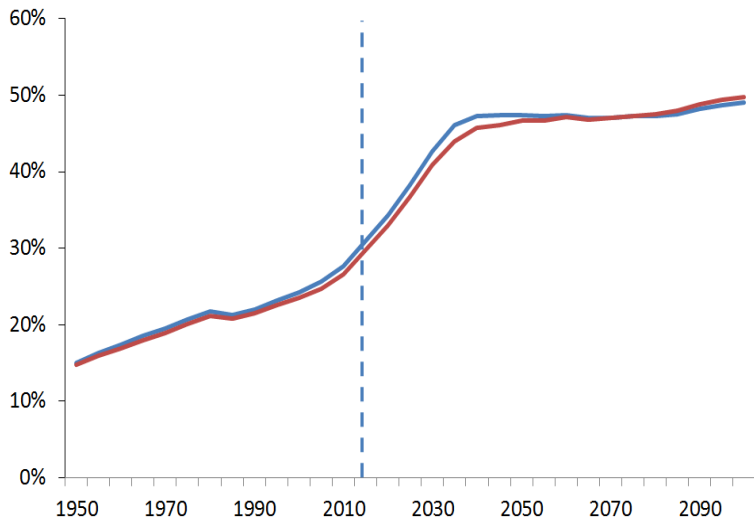
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Using the model

- Incorporate both the baby boom and the increase in life expectancy in our model
- Compute the transition from the 1950s to the 2100s according to the UN population predictions
- Match the data in the 1970s
- Let the model speak before and after these dates

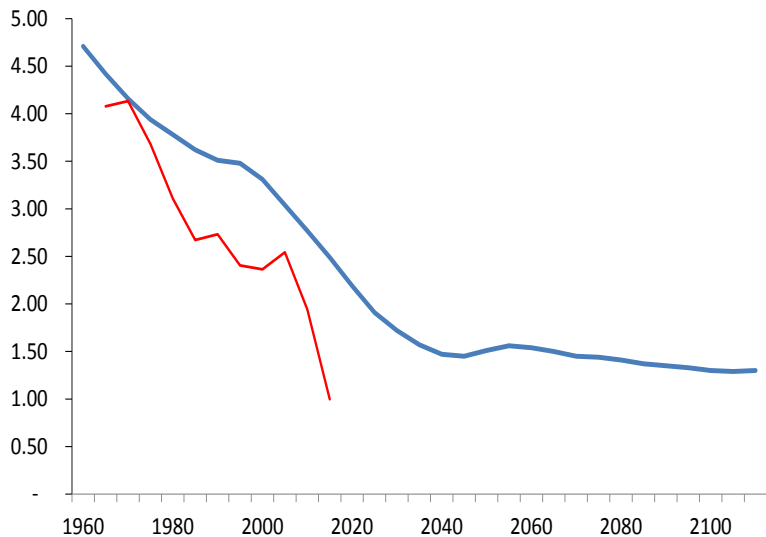
Calibration: Demographic change



Blue: model, Red: data (UN Population Statistics)

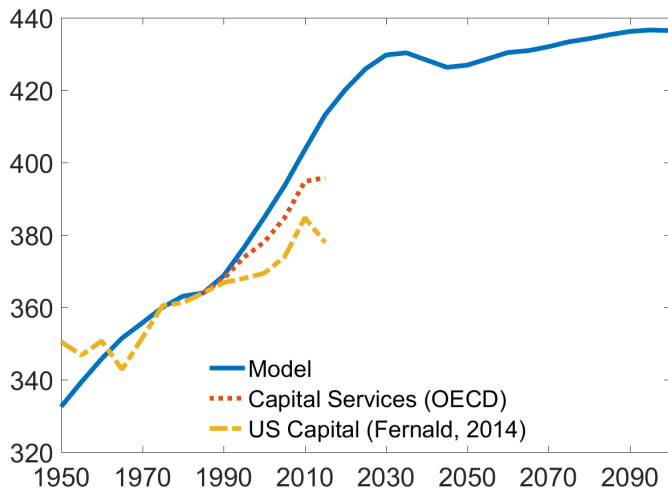
- Savings, **debt** and the **interest rate**
- **House prices** and the role of housing
- Labour **productivity**
- **Open economy** implications

Model outcome: Natural interest rate

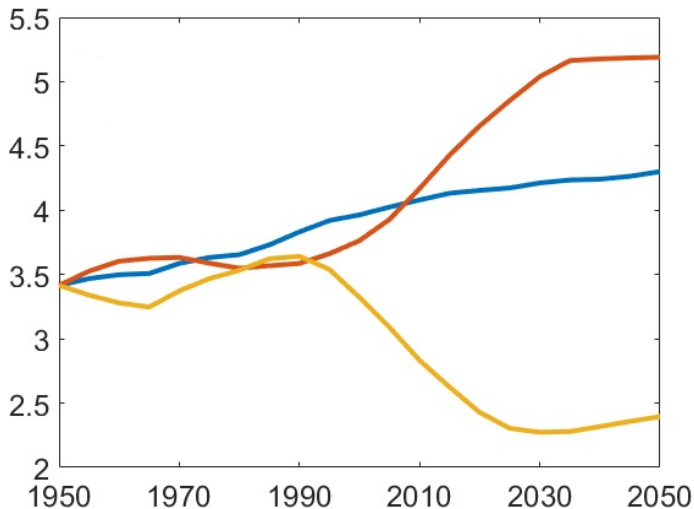


Blue: model, Red: data (Holston-Laubach-Williams Average)

Model outcome: capital-output ratio



Model outcome: Decomposing the drivers of savings



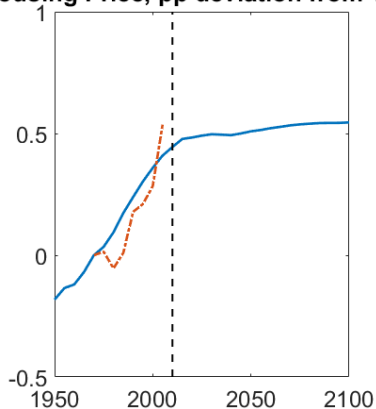
Blue: full simulation

Red: changing only the population age structure

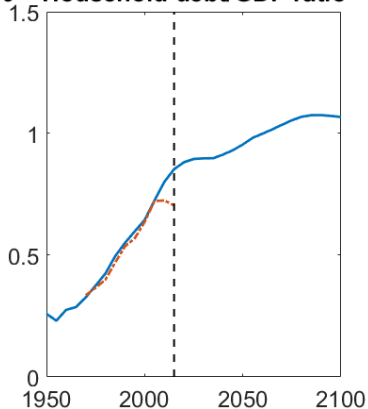
Yellow: changing only the household's optimal behaviour

Model outcome: Housing and credit

Housing Price, pp deviation from 1970

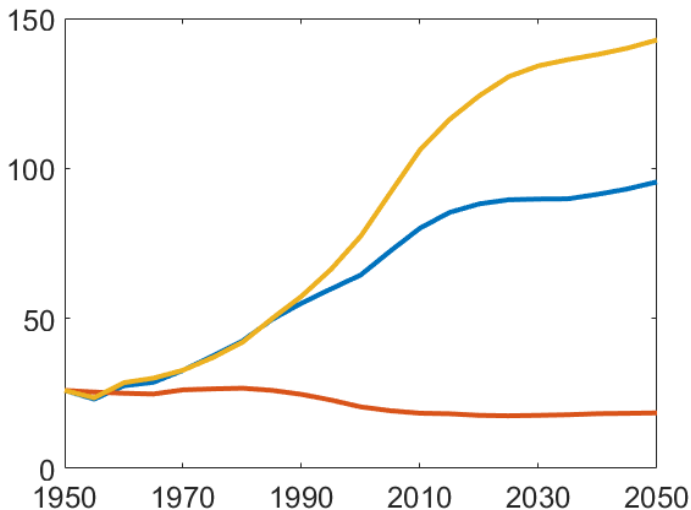


Household debt/GDP ratio



Blue: model, Red: data (BIS, Private credit, House price index)

Model outcome: Decomposing the drivers of debt

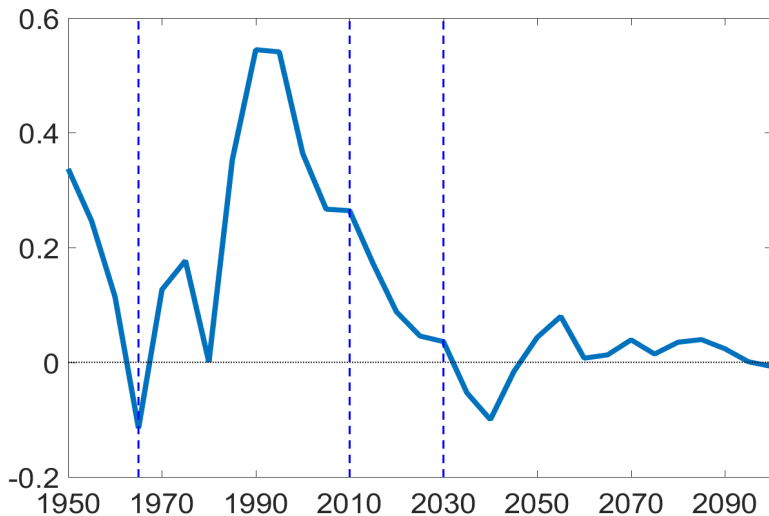


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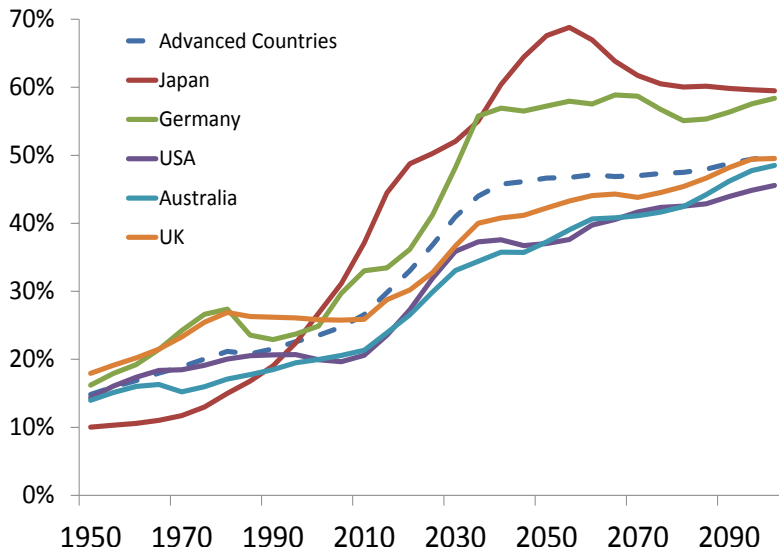
Yellow: changing only the household's optimal behaviour

Model outcome: Labour productivity



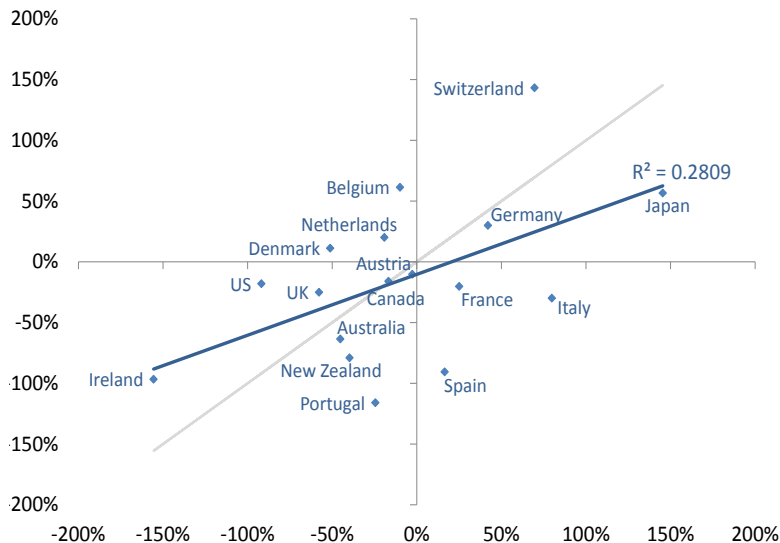
Deviation from trend, annualised growth

Open economy: OADR across countries



Source: UN Population Statistics

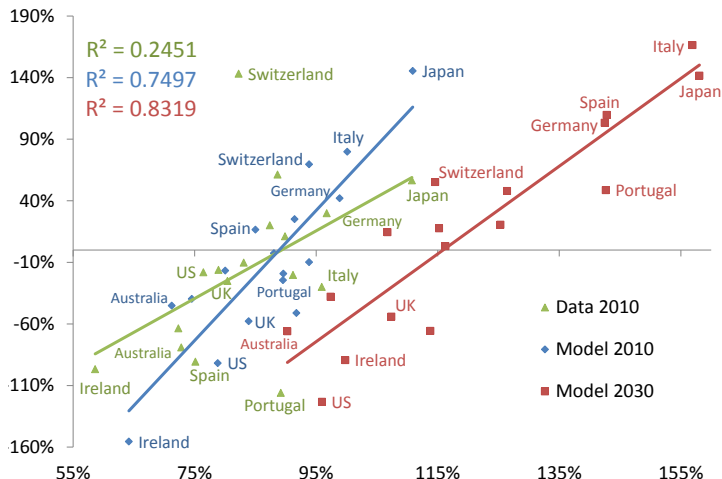
Open economy: Model vs data



Model on x-axis and Data on y-axis, grey line is the 45 degree line.

Open economy: model predictions

Demographic Changes and NFA accumulation



Note: HWR on x-axis and NFA/GDP on y-axis.

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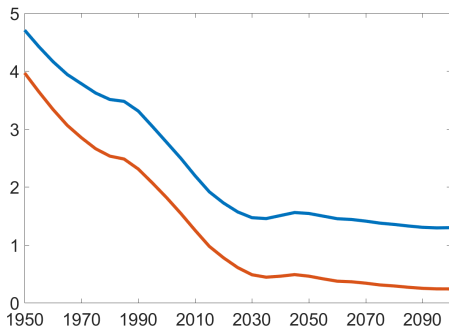
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- Housing
- Monopoly profits
- Retirement age

Sensitivities and extensions: housing

- Housing facilitates life-cycle saving, somewhat attenuating effects of demographics
- Prevents negative interest rates

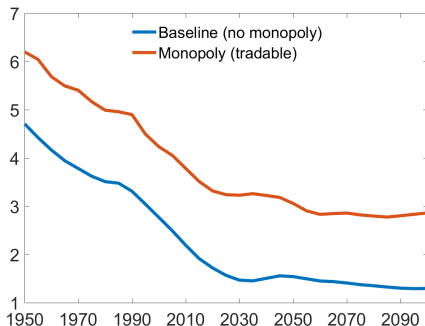
Figure: Simulations With and Without Housing



Sensitivities and extensions: monopoly profits

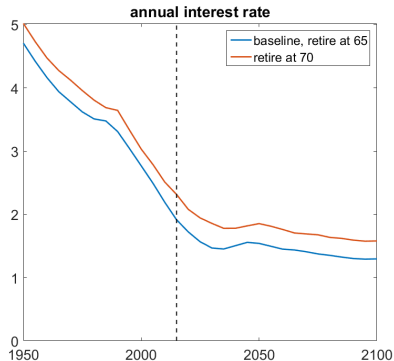
- Add monopolistic competition and supernormal profits to the corporate sector.
- In partial equilibrium, this pushes down on the interest rate $r_t = \frac{1}{\mu} \frac{\partial Y_t}{\partial K_t}$
- Tradable claims constitute an additional store of value, again attenuating fall and

Figure: Simulations With and Without Monopoly Power



Sensitivities and extensions: retirement age

Simulations varying retirement age by 5 years



Effects of retirement age increase surprisingly small

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Conclusions and some caveats

Conclusions:

- Population ageing mostly due to **persistent rise in longevity**
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Caveats:

- We have assumed **perfect foresight**, but not everyone plans ahead
- Not all the pressure of demographic change will fall on **private savings**
 - Retirees can instead **consume less** (no evidence so far)
 - Households will **work more**, or retire later (already some evidence)
 - Governments will provide part of the old-age pensions through **contemporaneous transfers**
- This is **not a forecast** that rates will remain low - many other factors at play

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Thank you!

Country list

Country list for UN population data: Australia, Austria, Belgium, Canada, Denmark, France, Germany, Ireland, Italy, Japan, Netherlands, New Zealand, Portugal, Spain, Switzerland, United Kingdom, United States of America

Population approximation before 1950: Belgium, Canada, Denmark, France, Italy, Netherlands, Spain, Switzerland, UK, USA

▶ [Back](#)