

# Spreading the word or reducing the term spread? Assessing spillovers from euro area monetary policy

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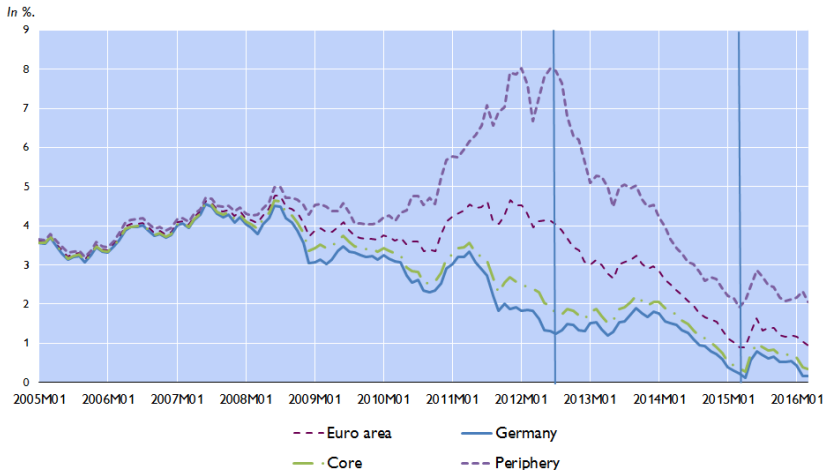
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# Compression of the yield curve?

## 10Y government bond yields

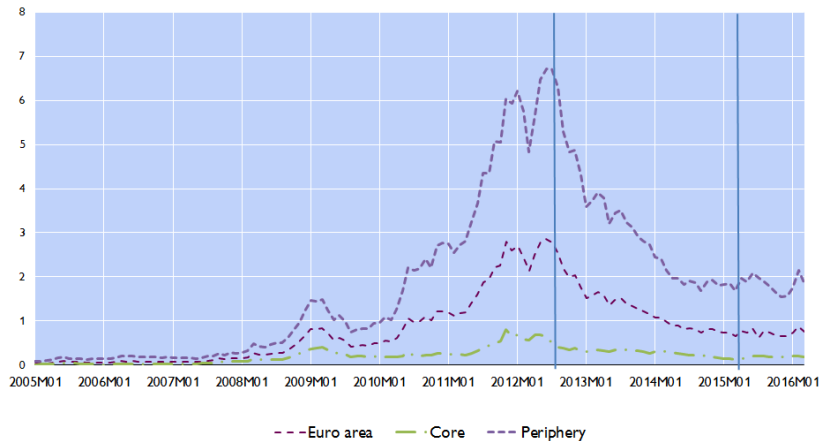


Source: Eurostat.

# Narrowing of risk spreads?

Risk spread (spread of euro area country long-term yields over German long-term yields)

In %.



Source: Eurostat.

# Motivation & Research Questions

- What are the likely **international effects** of these measures?
- **Monetary easing** in the euro area given an anti-inflationary and an already low interest rate environment **might trigger investors to reallocate capital** to more profitable regions, e.g., non-euro area EU member states / Central, Eastern and Southeastern Europe (CESEE).
- ⇒ These economies, in turn, may face **appreciation pressures** on their domestic currencies.
- On the other hand, an increase in euro area aggregate demand should spur exports from CESEE and thus overall GDP growth
  - Which one of these two effects dominates?
  - Through which channels does the shock transmit?

# Literature review

## 1 Within euro area spillovers

- **Gambacorta et al. (2014)**: estimate a structural panel vectorautoregression (PVAR) for eight advanced euro area countries; exogenous increase in central banks' assets  $\Rightarrow$  temporary rise in economic activity, smaller effect on prices
- **Burriel and Galesi (2016)**: use a global vector autoregressive model; shock to central banks' balance sheet  $\Rightarrow$  rise in output, inflation, equity prices and new credit operations and a depreciation of the effective exchange rate; no effects on inflation expectations.

## 2 Spillovers to non-euro area countries

- **Bluwstein and Canova (2016)** use two-country mixed frequency structural vector autoregressions  $\Rightarrow$  positive but heterogeneous effects on output; evidence for financial channel
- **Hálová and Horváth (2015)** use a panel VAR framework  $\Rightarrow$  strong effects on output, while spillovers to prices are rather weak

# Our contribution

- We assess **spillovers** of euro area monetary policy **to non-euro area EU member states**
- For that purpose we use a Bayesian and flexible version of the **Global Vector AutoRegressive** framework that
  - explicitly takes **country-specifics** into account
  - models **second-round effects**
  - reduces estimation uncertainty by using **shrinkage priors**
  - features **stochastic volatility**
- We look at **two different angles** through which **recent euro area monetary policy** can affect the real economy.
- **Bayesian stance** allows to include **a broad set of macro- and financial variables** that should cover a range of different transmission channels.

**Ingredients:**  $N$  countries, a vector  $\mathbf{x}_{i,t}$  of macroeconomic time series, a link matrix  $\mathbf{W}_i$ ,  $\mathbf{x}_{i,t}^*$ , to approximate global factors

- 1 For each country  $i$ , specify a VARX\*(p,q) model:

$$\mathbf{x}_{it} = \sum_{j=1}^p \underbrace{\mathbf{A}_{ij}\mathbf{x}_{it-j}}_{\text{domestic}} + \sum_{s=0}^q \underbrace{\mathbf{B}_{is}\mathbf{x}_{it-s}^*}_{\text{international}} + \varepsilon_{it} \quad (1)$$

where  $\mathbf{x}_{it}^* = \sum_{j=0}^N w_{ij}\mathbf{x}_{jt}$ , for  $i \in \{0, \dots, N\}$ ,  $w_{ij}$  a set of bilateral weights  $\varepsilon_{it} \sim N(0, \Sigma_{it})$

The **time varying** variance-covariance matrix  $\Sigma_{it}$  can be decomposed into:

$$\Sigma_{it} = \mathbf{U}_i \mathbf{H}_{it} \mathbf{U}_i'$$

with  $\mathbf{U}_i$  is lower triangular matrix with unit diagonal and  $\mathbf{H}_{it}$  a diagonal matrix with  $\mathbf{H}_{it} = \text{diag}(e^{h_{i1,t}}, \dots, e^{h_{ik_i,t}})$ .

For the **log-volatilities** we specify:

$$h_{ij,t} = \mu_{ij} + \rho_{ij}(h_{ij,t-1} - \mu_{ij}) + \kappa_{ij,t}, \quad (2)$$

where  $\kappa_{ij,t}$  denotes a white noise error with variance  $\varsigma_{ij}^2$ .

- 2 After some straightforward algebra, **single models** can be **stacked** to yield the **GVAR** representation:

$$\mathbf{G}\mathbf{x}_t = \sum_{n=1}^{\max(p,q)} \mathbf{F}_n \mathbf{x}_{t-n} + \boldsymbol{\eta}_t. \quad (3)$$

with  $\mathbf{x}_t = (\mathbf{x}'_{0t}, \dots, \mathbf{x}'_{Nt})'$  and  $\boldsymbol{\eta}_t$  is a  $k$ -dimensional vector white noise process with a block-diagonal matrix  $\boldsymbol{\Sigma}_t = \text{diag}(\boldsymbol{\Sigma}_{0t}, \dots, \boldsymbol{\Sigma}_{Nt})$



# Bayesian inference - prior setup I

Rewrite Eq. (1) into a standard regression model:

$$\mathbf{x}_{it} = \mathbf{C}_i \mathbf{z}_{it} + \varepsilon_{it}, \quad (4)$$

with  $\mathbf{z}_{it} = (\mathbf{x}'_{it-1}, \dots, \mathbf{x}'_{it-p}, \mathbf{x}^*_{it}, \dots, \mathbf{x}^*_{it-q})'$  a  $K_i = k_i p + k_i^* q$ -dimensional vector and  $\mathbf{C}_i = (\mathbf{A}_{i1}, \dots, \mathbf{A}_{ip}, \mathbf{B}_{i0}, \dots, \mathbf{B}_{iq})$  a  $k_i \times K_i$  matrix of stacked coefficients.

Akin to Huber and Feldkircher (JBES, 2016), **Normal-Gamma (NG)** prior on each element of  $\mathbf{c}_i = \text{vec}(\mathbf{C}_i)$ ,

$$c_{ij} | \tau_{ij}^2 \sim \mathcal{N}(0, 2/\lambda_i^2 \tau_{ij}^2), \quad \lambda_i^2 \sim \mathcal{G}(n_i, n_i), \quad \tau_{ij}^2 \sim \mathcal{G}(\vartheta_i, \vartheta_i) \quad (5)$$

Hereby we assume that the prior on  $c_{ij}$  depends on a **local scaling** parameter  $\tau_{ij}^2$ , a **country specific overall shrinkage** parameter  $\lambda_i^2$ , and  $\vartheta_i$  governing **excess kurtosis** of the marginal prior.

## Bayesian inference - prior setup II

Similarly we impose a NG prior on the **off-diagonal elements of  $\mathbf{U}_i$**

$$u_{i,jn} | \kappa_{i,jn}^2 \sim \mathcal{N}(0, 2/\zeta_i^2 \kappa_{i,jn}^2), \quad \zeta_i^2 \sim \mathcal{G}(l_i, l_i), \quad \kappa_{i,jn}^2 \sim \mathcal{G}(v_i, v_i), \quad (6)$$

For the **log-volatilities** we specify (Kastner and SFS, 2014):

$$\mu_{ij} \sim \mathcal{N}(0, v_\mu) \quad (7)$$

$$\frac{\rho_{ij} + 1}{2} \sim \mathcal{B}(a_0, b_0) \quad (8)$$

$$\varsigma_{ij}^2 \sim \mathcal{G}(1/2, 1/2B_\varsigma). \quad (9)$$

# Data & country coverage

**Euro area (12)** : AT, BE, DE, FI, FR, NL, SK (= core)  
 ES, IE, IT, PT, GR (= periphery)

**Non-euro area EU member states + TR and RU (11)** : GB, SE, DK, CZ,  
 HU, PL, BG, SI, HR, RO, RU, TR.

**Other (4)** : US, CN, JP, CA.

⇒ good coverage of the euro area, non-euro area EU-member states and the G-8 industrialized advanced economies

## Monthly data from 2000m1-2015m12:

*y* ... industrial production

*p* ... consumer prices

*eq* ... equity prices

$i_s/i_l$  ... short- / long-term interest rates

*er* ... exchange rate vis-a-vis the euro ("-" depreciation of euro)

*sp* ... term spread / risk spread

# Shock identification

- Two shocks

- 1 **Term spread shock:** simultaneous shock to EA term spreads on average by 100 basis points
- 2 **Risk spread shock:** simultaneous shock to EA risk spreads (defined as the spread of euro area long-term yields over German long-term yields) on average by 100 basis points

- Two sets of impulse responses

- 1 **Structural impulse responses** (SIRF) based on recursive ordering in euro area country models  $x = (y, p, sp, eq)$  (see Walentin, 2014).
- 2 **Generalized impulse response functions** (GIRF), no ordering assumed but no structural interpretation of responses (see Pesaran and Shin, 1998)

# Model specification

## Term spread shock

Country	$y$	$p$	$i_s$	$i_l$	$sp$	$er$	$eq$	$y^*$	$p^*$	$i_s^*$	$i_l^*$	$sp^*$	$er^*$	$eq^*$
DE	✓	✓	✓	–	✓	–	✓	✓	✓	✓	–	✓	✓	✓
EA (excl., DE)	✓	✓	–	–	✓	–	✓	✓	✓	✓	–	✓	✓	✓
Non-EA	✓	✓	✓	–	✓	✓	✓	✓	✓	✓	–	✓	–	✓

## Risk spread shock

Country	$y$	$p$	$i_s$	$i_l$	$sp$	$er$	$eq$	$y^*$	$p^*$	$i_s^*$	$i_l^*$	$sp^*$	$er^*$	$eq^*$
DE	✓	✓	✓	✓	–	–	✓	✓	✓	✓	✓	✓	✓	✓
EA (excl., DE)	✓	✓	–	–	✓	–	✓	✓	✓	✓	✓	✓	✓	✓
Non-EA	✓	✓	✓	✓	–	✓	✓	✓	✓	✓	✓	✓	–	✓

In the spirit of Baumeister and Benati (2013) we **zero out** responses  $i_s$  for the term spread shock and  $i_l$  for the risk spread shock in the German country model.

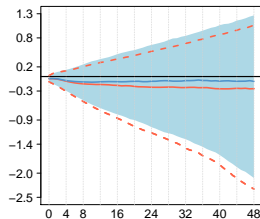
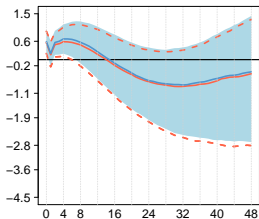
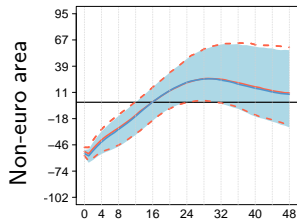
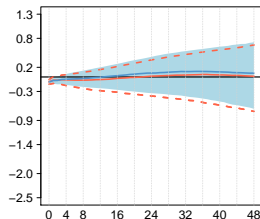
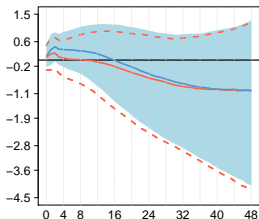
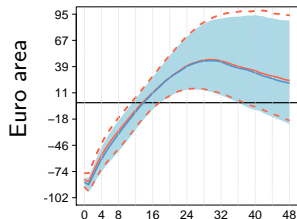
# Term spread shock I

SIRF in blue, GIRF in orange, 50% credible sets

Term spread

Industrial production

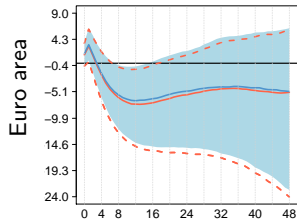
Consumer prices



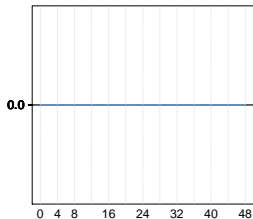
# Term spread shock II

SIRF in blue, GIRF in orange, 50% credible sets

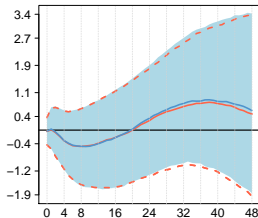
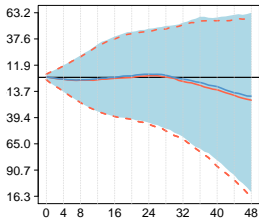
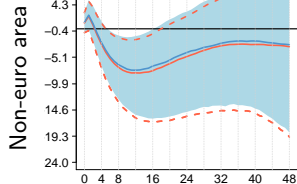
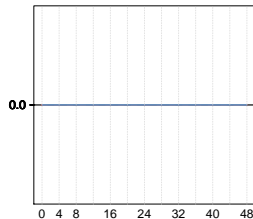
Equity prices



Short-term interest rate



Exchange rate



# Remarks: Term spread shock

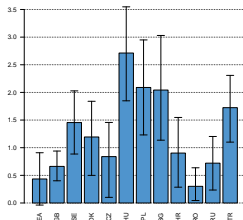
- Spillovers to long-term yields (about half of the size of within euro area effects)
- Positive and significant spillovers to industrial production in the short-run (although within euro area effects fraught with estimation uncertainty)
- No positive effects on consumer prices
- Reduction in long-term yields drive up equity prices
- Exchange rates in non-euro area EU member states strengthen against the euro in the short-run, but not significantly so
- Albeit overall effect on output within euro area non-significant, spillovers to non-euro area EU member states significant (in the short-run).



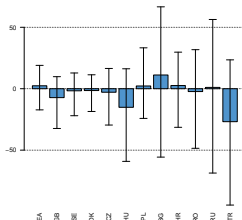
# Term spread shock III

Peak effects (SIRF, whiskers denote 50% credible intervals)

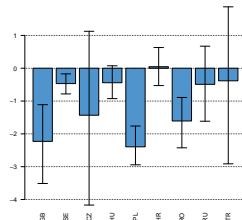
## Industrial production



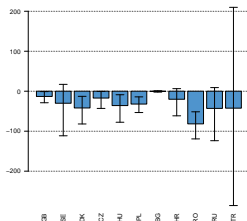
## Consumer prices



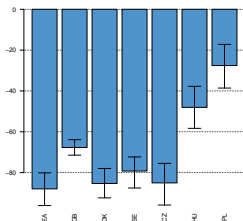
## Exchange rate



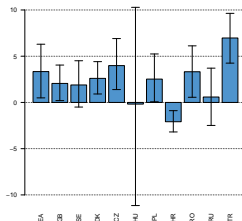
## Short-term int. rates



## Term spread



## Equity prices



## Regional remarks: Term spread shock

- Peak effects of industrial production significant throughout the region; HU, PL, BG, but also TR benefit most strongly
- Significant peak effects of the exchange rate (appreciation of local currency); most pronounced for PL, GB and RO, marked uncertainty for CZ
- To ease pressure on the exchange rate, policy rates decrease
- Significant peak effects of the term spread; in HU and PL smaller compared to other economies
- For most economies, equity prices tick up significantly; most pronounced for TR

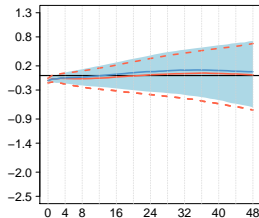
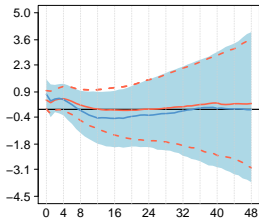
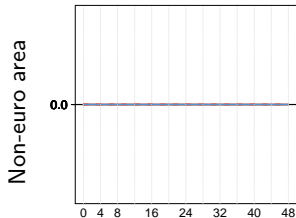
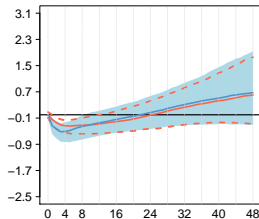
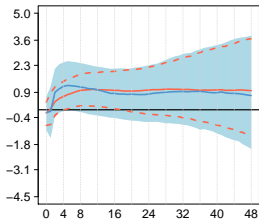
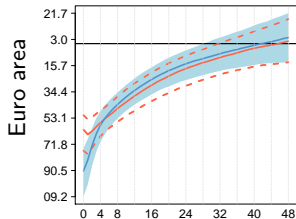
# Risk spread shock I

SIRF in blue, GIRF in orange, 50% credible sets

Risk spread

Industrial production

Consumer prices



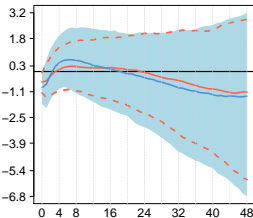
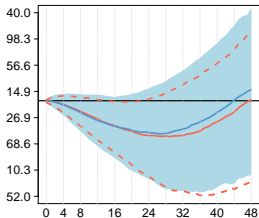
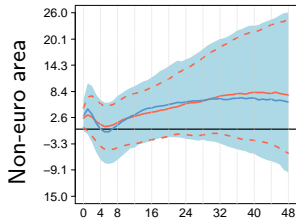
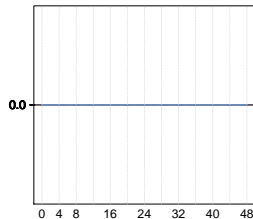
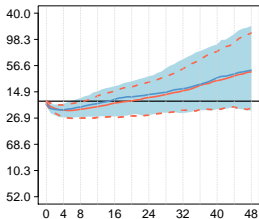
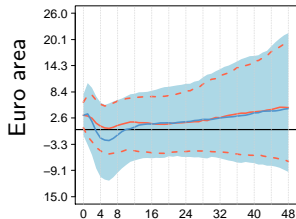
# Risk spread shock II

SIRF in blue, GIRF in orange, 50% credible sets

Equity prices

Short-term interest rate

Exchange rate



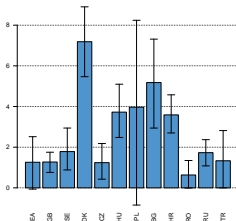
## Remarks: Risk spread shock

- Overall effects of the risk spread shock on industrial production are positive but not significant
- No positive effects on consumer prices
- Positive domestic and international effects on equity prices
- Local currencies tend to strengthen in the short-run; rebound in the medium-term
- Negative spillovers to long-term interest rates (not shown)  $\Rightarrow$  non-euro area EU member states benefit from a reduction in uncertainty and risk in the euro area

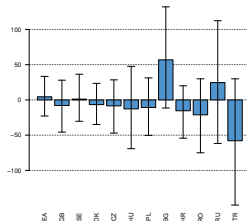
# Risk spread shock III

Peak effects (SIRF, whiskers denote 50% credible intervals)

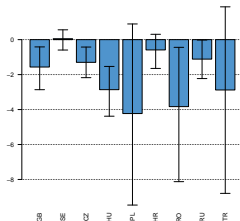
## Industrial production



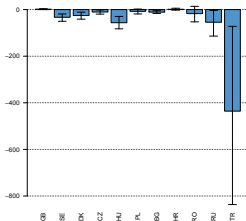
## Consumer prices



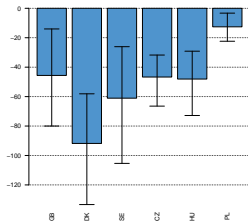
## Exchange rate



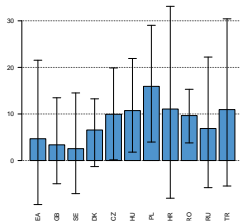
## Short-term int. rates



## Long-term int. rates



## Equity prices



## Regional remarks: Risk spread shock

- Peak effects of industrial production significant for most economies (BG, HU and PL again benefit strongly, but also HR)
- Significant peak effects of the exchange rate (appreciation of local currency); most pronounced for PL and RO
- To ease pressure on the exchange rate, policy rates decrease; most pronounced for TR and to a lesser extent RU and HU
- Significant reductions in long-term interest rates; effects more pronounced for advanced economies
- For most economies, equity prices tick up significantly, especially so in CEE economies

# Conclusions I

- For both shocks, we find **positive and significant spillovers to industrial production** in non-euro area EU member states in the short-run, although to a varying degree
- **Heterogeneity of spillovers** partially explained by different within euro area spillovers (reduction of euro area term spreads stronger effects on euro area core, while narrowing of euro area long-term interest rates, stronger effects on periphery)
- Spillovers are transmitted via the **financial channel** (through interest rates and equity prices)



# Conclusions II

- Also, currencies tend to strengthen against the euro in the short-run (**exchange rate / trade channel**)
  
- Since overall effects on output positive, **benefits from euro area expansion seem to outweigh costs from appreciation of local currencies**
  
- **We do not find evidence of spillovers to consumer prices.**

# Martin Feldkircher



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- Current Position: Senior Economist, Foreign Research Division (AUSA), Oesterreichische Nationalbank (OeNB)
- Research interests: Empirical macroeconomics, multicountry models, forecasting, Bayesian analysis

# VARs & GVARs- Selected Readings I



Baumeister C. and Benati L. 2013.

Unconventional Monetary Policy and the Great Recession: Estimating the Macroeconomic Effects of a Spread Compression at the Zero Lower Bound  
*International Journal of Central Banking, Vol.9(2), pp 165–212.*



Crespo Cuaresma J. and Feldkircher M. and Huber F. 2016.

Forecasting with Global Vector Autoregressive Models: a Bayesian Approach  
*Journal of Applied Econometrics, forthcoming.*



Dovern J. and Feldkircher M. and Huber F. 2016.

Does joint modelling of the world economy pay off? Evaluating global forecasts from a Bayesian GVAR  
*Journal of Economic Dynamics and Control, 70, pp 86–100.*



Fadejeva L. and Feldkircher M. and Reininger T. 2017.

International Spillovers from Euro Area and US Credit and Demand Shocks: A focus on Emerging Europe  
*Journal of International Money and Finance, Vol. 70, pp 1-25.*

# VARs & GVARs- Selected Readings II



Feldkircher M. 2015.

A Global Macro Model for Emerging Europe.

*Journal of Comparative Economics*, Vol. 43, Issue 3, pp. 706-726.



Feldkircher M. and Huber F. 2016.

The international transmission of US shocks – Evidence from Bayesian global vector autoregressions

*European Economic Review*, Vol. 81, pp 167–188.



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*Journal of Business & Economic Statistics*, forthcoming.



Kastner G. and Frühwirth-Schnatter S. 2014.

Ancillarity-sufficiency interweaving strategy (ASIS) for boosting MCMC estimation of stochastic volatility models.

*Computational Statistics & Data Analysis*, 76, pp 408–423.



Pesaran H. and Shin Y. 2011.

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*Economics Letters*, Vol. 58(1), pp 17–29.

# Spillovers from euro area monetary policy



Bluwstein K. and Canova F. 2015.

Beggar-thy-neighbor? The international effects of ECB unconventional monetary policy measures.

*C.E.P.R. Discussion Papers, Nr. 10856.*



Burriel P. and Galesi A. 2016.

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*Mimeo, Banco de Espana .*



Gambacorta L. and Hofmann B. and Peersman G. 2014.

The Effectiveness of Unconventional Monetary Policy at the Zero Lower Bound: A Cross-Country Analysis.

*Journal of Money, Credit and Banking, 2014, 46 (4), 615–642.*



Hálová K. and Horváth R. 2015.

Spillovers of ECBs Unconventional Monetary Policy: The Effect on Central and Eastern Europe.

*Working Papers 351, Institut für Ost- und Südosteuropaforschung.*



Walentin K. 2014.

Business cycle implications of mortgage spreads.

*Journal of Monetary Economics, 67, pp. 62–77.*

# BACKUP SLIDES

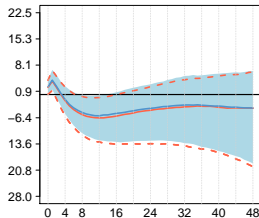
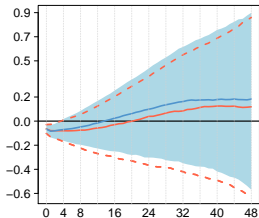
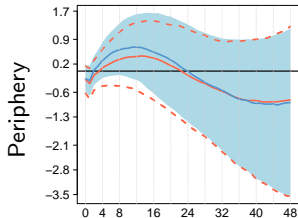
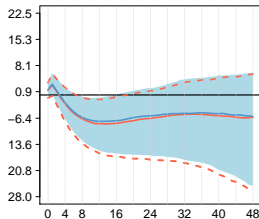
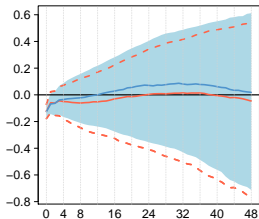
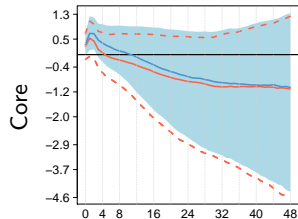
# Term spread shock

Core vs. periphery; SIRF in blue, GIRF in orange, 50% credible sets

Industrial production

Consumer prices

Term spread



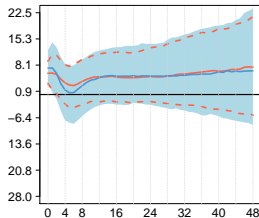
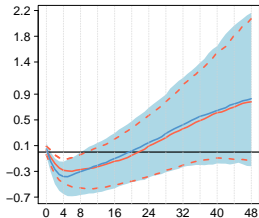
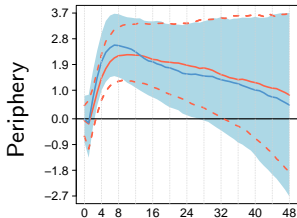
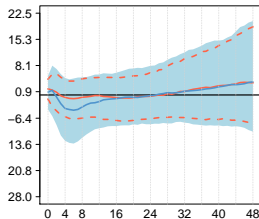
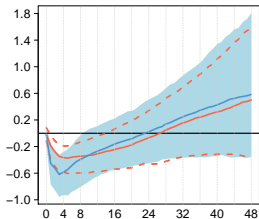
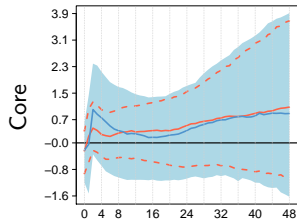
# Risk spread shock

Core vs. periphery; SIRF in blue, GIRF in orange, 50% credible sets

Industrial production

Consumer prices

Equity prices





# First Layer: Estimation of single model

- Each country is modeled as a country-specific VAR augmented with the foreign variables (VARX)
- VARX(1,1) is

$$\mathbf{x}_{it} = \underbrace{c_0 + c_1 \mathbf{t} + \psi_{i0} \mathbf{d}_t}_{\text{Deterministics}} + \Phi \mathbf{x}_{i,t-1} + \Lambda_{i0} \mathbf{x}_{it}^* + \Lambda_{i1} \mathbf{x}_{it-1}^* + \mathbf{u}_{it}$$

- In our example the model for the euro area would look like

$$\begin{bmatrix} \mathbf{y}_t \\ \mathbf{Dp}_t \end{bmatrix} = \Phi \begin{bmatrix} \mathbf{y}_{t-1} \\ \mathbf{Dp}_{t-1} \end{bmatrix} + \Lambda_{i0} \begin{bmatrix} \mathbf{y}_t^* \\ \mathbf{Dp}_t^* \end{bmatrix} + \Lambda_{i1} \begin{bmatrix} \mathbf{y}_{t-1}^* \\ \mathbf{Dp}_{t-1}^* \end{bmatrix} + \begin{bmatrix} \mathbf{u}_{y,t} \\ \mathbf{u}_{i,t} \end{bmatrix}$$

# First Layer: Estimation of Single Model

This model is then written in VECM form and estimated for  $i \in 1, \dots, N$

$$\Delta \mathbf{x}_t = c_0 + c_1 \mathbf{t} + \Phi_i \mathbf{x}_{t-1} + \Lambda_{i0} \Delta \mathbf{x}_{it}^* + \Psi_{i0} \Delta \mathbf{d}_t + \mathbf{u}_{it}$$

with  $\mathbf{u}_t \sim N(\mathbf{0}, \Sigma_u)$ ,  $\mathbf{d}_t$  denoting global variables (e.g., oil prices) and  $t$  a deterministic trend component.

Note:  $\mathbf{d}_t$  and  $\mathbf{x}_t$  allowed to enter the equation contemporaneously;  $\mathbf{x}_t$  assumed to be long-run forcing for  $\mathbf{y}_t$  (i.e., zero restrictions on  $\Phi_i$ , small economy assumption)

## Second Layer: Stacking the Single Models

- After the country-by-country estimation of the VECMX we can proceed to the second step of the GVAR modelling strategy
  - 1 Recover the parameters of the VARX models
  - 2 Combine the VARX into a global model
- The resulting model will have the form of a standard VAR where all variables will be "endogenous"
- This is a purely mechanical step: **no estimation is involved!**

## Second Layer: Stacking the Single Models

- Define a selection matrix that singles out the country under consideration from the global vector of endogenous variables

$$\mathbf{S}_{ea} = \begin{pmatrix} 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \end{pmatrix} \quad \mathbf{x}_t = \begin{pmatrix} \mathbf{y}_{us,t} \\ \mathbf{Dp}_{us,t} \\ \mathbf{y}_{ea,t} \\ \mathbf{Dp}_{ea,t} \\ \mathbf{y}_{ru,t} \\ \mathbf{Dp}_{ru,t} \end{pmatrix}$$

- This implies that  $\mathbf{x}_{ea,t} = \begin{pmatrix} \mathbf{y}_{ea} \\ \mathbf{Dp}_{ea} \end{pmatrix} = \mathbf{S}_{ea} \mathbf{x}_t$

# Second Layer: Stacking the Single Models

- VARX(1,1)

$$\mathbf{x}_{it} = \Phi \mathbf{x}_{i,t-1} + \Lambda_{i0} \mathbf{x}_{it}^* + \Lambda_{i1} \mathbf{x}_{i,t-1}^* + \mathbf{u}_{it}$$

- Use link matrix  $\mathcal{W}_i$  and selection matrix  $\mathbf{S}_i$

$$\mathbf{S}_i \mathbf{x}_t = \Phi \mathbf{S}_i \mathbf{x}_{t-1} + \Lambda_{i0} \mathcal{W}_i \mathbf{x}_t + \Lambda_{i1} \mathcal{W}_i \mathbf{x}_{t-1} + \mathbf{u}_{it}$$

- Rearrange

$$(\mathbf{S}_i - \Lambda_{i0} \mathcal{W}_i) \mathbf{x}_t = (\Phi \mathbf{S}_i + \Lambda_{i1} \mathcal{W}_i) \mathbf{x}_{t-1} + \mathbf{u}_{it}$$

- Relabel

$$\mathbf{G}_i \mathbf{x}_t = \mathbf{H}_i \mathbf{x}_{t-1} + \mathbf{u}_{it}$$

# The Global Model

- Stack all country-specific models

$$\begin{bmatrix} \mathbf{G}_{us} \\ \mathbf{G}_{ea} \\ \mathbf{G}_{ru} \end{bmatrix} \mathbf{x}_t = \begin{bmatrix} \mathbf{H}_{us} \\ \mathbf{H}_{ea} \\ \mathbf{H}_{ru} \end{bmatrix} \mathbf{x}_{t-1} + \begin{bmatrix} \mathbf{u}_{us,t} \\ \mathbf{u}_{ea,t} \\ \mathbf{u}_{ru,t} \end{bmatrix}$$

- More compact

$$\mathbf{G}\mathbf{x}_t = \mathbf{H}\mathbf{x}_{t-1} + \mathbf{u}_t$$

with

$$\mathbf{G} = (\mathbf{G}'_{us}, \mathbf{G}'_{ea}, \mathbf{G}'_{ru})', \mathbf{H} = (\mathbf{H}'_{us}, \mathbf{H}'_{ea}, \mathbf{H}'_{ru})', \mathbf{u} = (\mathbf{u}'_{us}, \mathbf{u}'_{ea}, \mathbf{u}'_{ru})'$$

- The **GVAR** model

$$\mathbf{x}_t = \underbrace{\mathbf{F}\mathbf{x}_{t-1}}_{\mathbf{F}=\mathbf{G}^{-1}\mathbf{H}} + \underbrace{\tilde{\mathbf{u}}_t}_{\mathbf{G}^{-1}\mathbf{u}_t}$$