

Dormant Shocks and Fiscal Virtue

Francesco Bianchi
Duke University

Leonardo Melosi
London Business School

ESSIM - 2012

Relation between **fiscal discipline** and **inflation** is not stable:

- 1 Periods of fiscal imbalance are not necessarily inflationary
- 2 When they are, the spurs of inflation can be:
 - Short lasting and remarkably violent (emerging economies) or...
 - Unfolding over many decades, starting with small increases and then gaining momentum (USA in the '70s)

Traditional DSGE models have a hard time in generating:

- 1 **Heterogeneity** in the link over time and across countries
- 2 **Persistent** and **accelerating** increases in inflation

Dormant shocks and Fiscal Virtue

We build a model in which the current behavior of policy makers influence agents' beliefs about the way debt will be stabilized:

- Policy makers are generally **virtuous**
 - ① The fiscal authority controls debt
 - ② The monetary authority has full control of inflation

⇒ Shocks that hit the debt-to-GDP ratio are **dormant**
- Policy makers can deviate from the virtuous policy mix
- These deviations can be **short** or **long** lasting
- When observing a deviation, agents conduct Bayesian learning to infer its likely duration

Dormant shocks and Fiscal Virtue

- As agents observe **more and more deviations**, they grow **increasingly pessimistic** about a prompt return to the Virtuous regime
- **Drift in beliefs** \implies drift in inflation and uncertainty as **dormant shocks** start manifesting themselves
- Inflation **accelerates** as initially optimistic agents become relatively pessimistic
- The speed with which these effects unfold critically depends on the country's **Fiscal Virtue**

Main results

- 1 Spurs of inflation can unfold over **decades**. Inflation starts moving slowly, but it **accelerates** over time
- 2 Countries with similar levels of inflation during regular times can experience very different outcomes as they start deviating
- 3 The strict distinction between non-Ricardian and Ricardian regimes typical of the Fiscal Theory of Price Level breaks down
- 4 We compare the model with US data:
 - The model can explain the run-up in inflation of the '70s and the risk of deflation in the early 2000s
 - Past Fiscal Virtue can hide the current **risk of inflation**
 - Contradictory statements can conduct to undesirable outcomes

Related literature

- Sargent and Wallace (1981)
- Leeper (1991), Sims (1994), Woodford (1994, 1995, 2001), Cochrane (1998, 2001)
- Bianchi and Ilut (2012) and Sims (2009)
- DSGE models with parameter instability: Schorfheide (2005), Bianchi (2012), Davig and Doh (2011), Fernández-Villaverde et al. (2010), and Liu et al. (2011)
- Modeling the Evolution of Public Expectations and Uncertainty: Bianchi and Melosi (2012)

Two models

- To inspect the mechanism
 - Basic three equations new-Keynesian model augmented with a fiscal rule
- Quantitative analysis
 - Richer model based on Bianchi and Ilut (2012)

Household

 ▶ Linearized Model

- The representative household maximizes:

$$E_0 \left[\sum_{t=0}^{\infty} \beta^t e^{d_t} [\log(C_t) - h_t] \right]$$

subject to the budget constraint:

$$P_t C_t + B_t + P_t T_t = P_t W_t h_t + R_{t-1} B_{t-1}$$

- We assume $d_t = \rho_d d_{t-1} + \sigma_d \epsilon_{d,t}$

Firms ▸ Linearized Model

- Each of the monopolistically competitive firms faces a downward-sloping demand curve:

$$Y_t(j) = (P_t(j)/P_t)^{-1/v} Y_t$$

where $1/v$ is the elasticity of substitution between two differentiated goods

- Whenever a firm wants to change its price, it faces quadratic adjustment costs represented by an output loss:

$$AC_t(j) = \frac{\varphi}{2} \left(\frac{P_t(j)}{P_{t-1}(j)} - \Pi \right)^2 Y_t(j) \frac{P_t(j)}{P_t}$$

Technology

▸ Linearized Model

Labor is the only input in a linear production function:

$$Y_t(j) = A_t h_t(j)$$

where total factor productivity A_t evolves according to:

$$\begin{aligned} \ln A_t &= \ln \bar{A} + z_t \\ z_t &= \rho_z z_{t-1} + \sigma_z \epsilon_{z,t} \end{aligned}$$

Monetary authority

▸ Linearized Model

The Central Bank moves the FFR according to the rule:

$$\frac{R_t}{R} = \left(\frac{R_{t-1}}{R} \right)^{\rho_R(\zeta_t)} \left[\left(\frac{\Pi_t}{\Pi} \right)^{\psi_\pi(\zeta_t)} \left(\frac{Y_t}{Y_t^n} \right)^{\psi_y(\zeta_t)} \right]^{(1-\rho_R(\zeta_t))} e^{\sigma_{R\epsilon_{R,t}}}$$

where R is the steady-state gross nominal interest rate, Y_t^n is natural output, Π is the target level for gross inflation, and ζ_t is a hidden variable that determines the regime in place at time t .

Fiscal authority ▸ Back

- The Government budget constraint is given by:

$$b_t = b_{t-1} (Y_t \Pi_t / Y_{t-1})^{-1} R_{t-1} - s_t$$

where $b_t = B_t / (P_t Y_t)$ and $s_t = S_t / (P_t Y_t)$

- The government moves primary surpluses according to the rule:

$$s_t = (1 - \rho_s) \delta_b (\xi_t) b_{t-1} + \rho_s s_{t-1} + \sigma_s \epsilon_{s,t}$$

- In order to completely isolate the effects of fiscal discipline, we assume that the government only provides a subsidy or raises taxes ($T_t = S_t$).

Households and firms ▸ Full Model

- Linearized Euler Equation:

$$y_t = E_t(y_{t+1}) - (R_t - E_t(\pi_{t+1})) + (1 - \rho_d) d_t \quad (1)$$

- Expectation augmented Phillips curve:

$$\pi_t = \beta E_t(\pi_{t+1}) + \kappa(y_t - z_t) \quad (2)$$

- Stochastic processes of the shocks:

$$d_t = \rho_d d_{t-1} + \sigma_d \epsilon_{d,t} \quad (3)$$

$$z_t = \rho_z z_{t-1} + \sigma_z \epsilon_{z,t} \quad (4)$$

where $\epsilon_{d,t} \sim N(0, 1)$ and $\epsilon_{z,t} \sim N(0, 1)$

Policy makers

- Linearized government budget constraint:

$$b_t = \beta^{-1} b_{t-1} + b\beta^{-1} (R_{t-1} - \pi_t - \Delta y_t) - s_t \quad (5)$$

- Fiscal rule:

$$s_t = \rho_s s_{t-1} + (1 - \rho_s) \delta_{b, \zeta_t} b_{t-1} + \sigma_s \epsilon_{s,t} \quad (6)$$

- Monetary rule:

$$R_t = (1 - \rho_{R, \zeta_t}) \left(\psi_{\pi, \zeta_t} \pi_t + \psi_{y, \zeta_t} [y_t - z_t] \right) \quad (7)$$

$$+ \rho_{R, \zeta_t} R_{t-1} + \sigma_R \epsilon_{R,t} \quad (8)$$

where $\epsilon_{R,t} \sim N(0, 1)$ and $\epsilon_{s,t} \sim N(0, 1)$

Monetary/Fiscal Policy Mix

When regimes are taken in **isolation**, the two policy rules and the linearized budget constraint are key to determine existence and uniqueness of a solution:

$$R_t = \rho_{R, \xi_t} R_{t-1} + \left(1 - \rho_{R, \xi_t}\right) \psi_{\pi, \xi_t} \pi_t + \dots$$

$$s_t = \rho_s s_{t-1} + (1 - \rho_s) \delta_{b, \xi_t} b_{t-1} + \dots$$

$$\begin{aligned} b_t &= \beta^{-1} b_{t-1} + \dots - s_t \\ \rightarrow b_t &= \left(\beta^{-1} - \delta_{b, \xi_t}\right) b_{t-1} + \dots \end{aligned}$$

Monetary/Fiscal Policy Mix

▸ Four cases

Leeper (1991) shows that two determinacy regions exist:

| | ψ_{π, ξ_t} | δ_{b, ξ_t} |
|---------------------------------|---------------------|---------------------|
| Active Monetary, Passive Fiscal | > 1 | $> \beta^{-1} - 1$ |
| Passive Monetary, Active Fiscal | < 1 | $< \beta^{-1} - 1$ |

- AM/PF → Taylor principle is satisfied, fiscal police accommodates behavior of monetary authority → **Ricardian regime**
- PM/AF → Taylor principle is **not** satisfied, inflation is free to move to keep debt on a stable path → **non-Ricardian regime**

Allowing for regime changes

- We assume that the policy mix is generally **virtuous**:

$$AM/PF \rightarrow \psi_{\pi}(\zeta_t = 1) = \psi_{\pi}^A > 1, \delta_b(\zeta_t = 1) = \delta_b^P > \beta^{-1} - 1$$

- However, policy makers can **deviate** from the Virtuous regime:

$$PM/AF \rightarrow \psi_{\pi}(\zeta_t = 2) = \psi_{\pi}^P < 1, \delta_b(\zeta_t = 2) = \delta_b^A < \beta^{-1} - 1$$

$$PM/AF \rightarrow \psi_{\pi}(\zeta_t = 3) = \psi_{\pi}^P < 1, \delta_b(\zeta_t = 3) = \delta_b^A < \beta^{-1} - 1$$

Allowing for regime changes

- These deviations can be **short** or **long** lasting:

$$p_{22} \ll p_{33}$$

- Short lasting deviations are (conditionally) more frequent:

$$p_{12} > p_{13}$$

- Transition matrix:

$$H = \begin{bmatrix} p_{11} & p_{12} & p_{13} \\ 1 - p_{22} & p_{22} & \\ 1 - p_{33} & & p_{33} \end{bmatrix}$$

Model Solution

- Agents are **aware of the possibility of regime changes** \implies standard solution methods do not apply
- The solution algorithm employed in this paper is based on the work of Farmer, *et al.* (2010)
- When a solution exists, it can be characterized as a regime switching vector-autoregression:

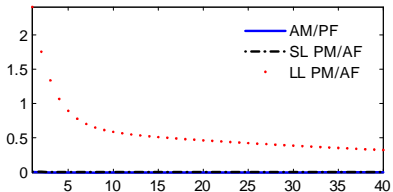
$$S_t = T(\zeta_t, \theta, H) S_{t-1} + R(\zeta_t, \theta, H) \varepsilon_t \quad (9)$$

Calibration

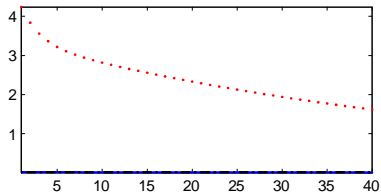
| Parameter | Value | Parameter | Value | Parameter | Value |
|----------------|-------|-----------|-------|---------------|-------|
| ψ_{π}^A | 2.00 | ρ_s | 0.90 | $100\sigma_R$ | 0.20 |
| ψ_y^A | 0.10 | ρ_z | 0.90 | $100\sigma_s$ | 0.50 |
| ρ_R^A | 0.75 | ρ_d | 0.90 | $100\sigma_z$ | 0.70 |
| δ_b^P | 0.03 | b | 1.00 | $100\sigma_d$ | 0.40 |
| ψ_{π}^P | 0.80 | κ | 0.05 | p_{11} | 0.95 |
| ψ_y^P | 0.10 | β | 0.99 | p_{12} | 0.495 |
| ρ_R^P | 0.75 | | | p_{22} | 0.70 |
| δ_b^A | 0 | | | p_{33} | 0.99 |

Impulse responses: Primary deficit shock ▸ MP

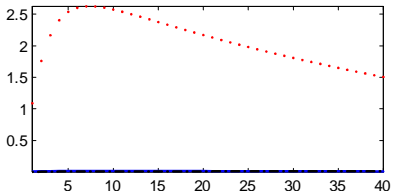
GDP



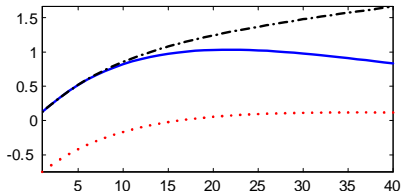
Inflation



FFR



B/GDP

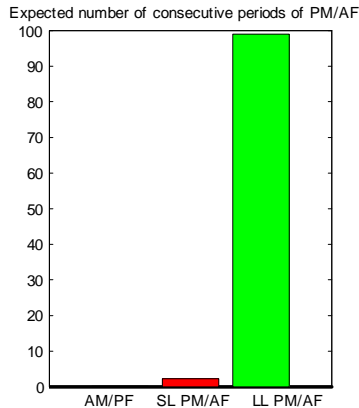
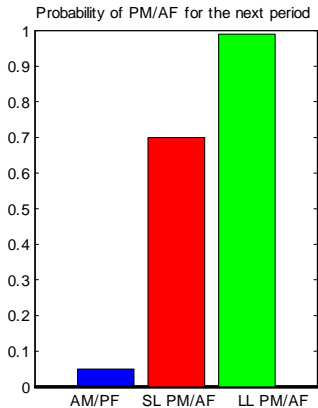


Agents' Beliefs

The interaction between agents' beliefs and policy makers' behavior implies that:

- 1 Virtuous regime and short lasting deviations are **Ricardian**
- 2 Long lasting deviations are **non-Ricardian**

Agents' Beliefs



Information set

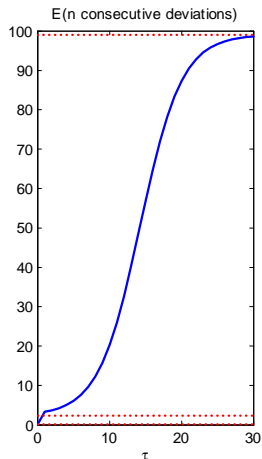
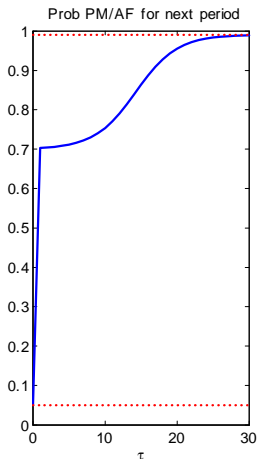
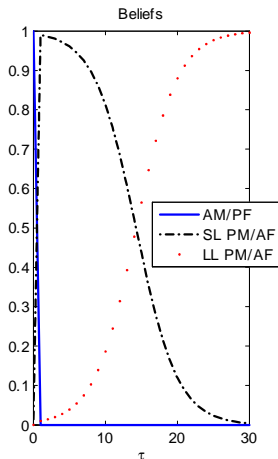
We assume that agents...

- ① ...can observe the history of the endogenous variables and structural shocks
- ② ...cannot observe the history of regimes, instead they conduct Bayesian learning

Then:

- ① The Virtuous regime is fully revealing
- ② The nature of an unobserved deviation is unknown \implies *As policy makers keep deviating, agents grow more and more pessimistic about moving back to the Virtuous regime*

Evolution of Agents' Beliefs ▸ Details



Solving the model with learning

Model dynamics cannot be captured by the three policy regimes:

- Expanded number of regimes defined as a combination between **policy makers' behavior** and **agents' beliefs**
- If $\tau = x$, the economy can only move to:

① $\theta^{AM/PF}, \tau = 0$

② $\theta^{PM/AF}, \tau = x + 1$

\implies Transition matrix $H \rightarrow$ transition matrix \tilde{H}

- **Upper bound to pessimism:** For each $\varepsilon > 0$, \exists integer $\tau^* > 0$ s.t.

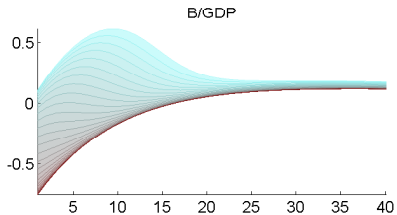
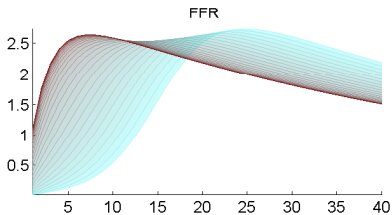
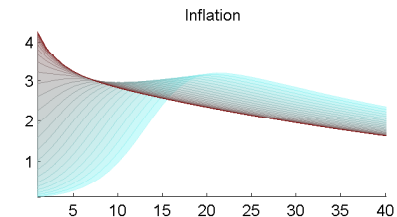
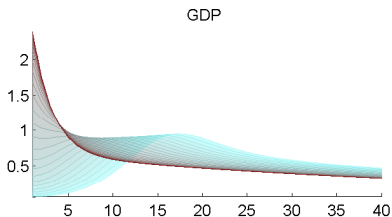
$$p_{33} - \text{prob} \{s_{t+1} \neq 1 | \tau = \tau^*\} < \varepsilon$$

\implies Model approximated using $\tau^* + 1$ regimes

Solving the model with learning

- Agents *fully understand the model* and *they know that they do not know*
⇒ They take into account the impact of future policy makers' behavior on their future beliefs
- Different from anticipated utility/adaptive learning

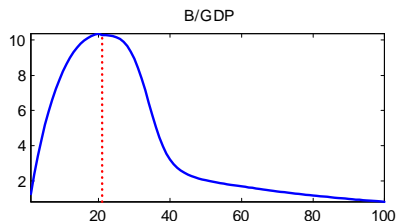
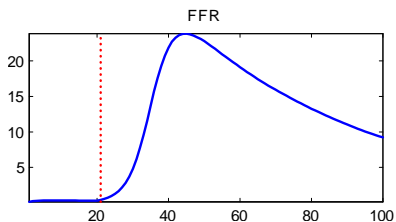
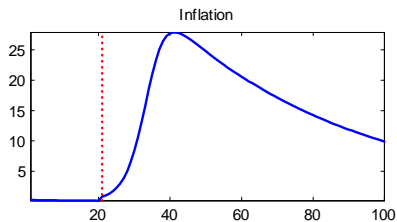
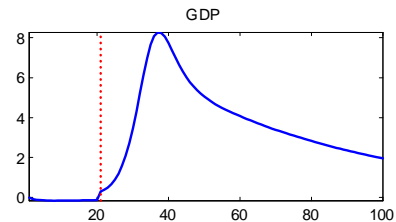
Impulse responses: Primary deficit ▶ MP



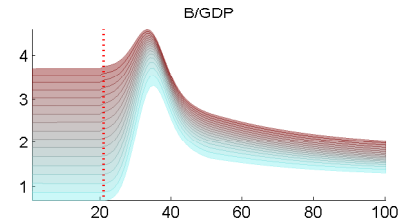
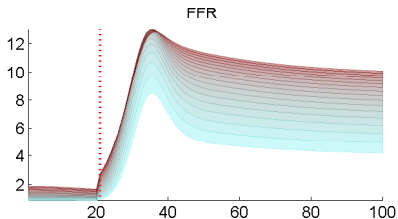
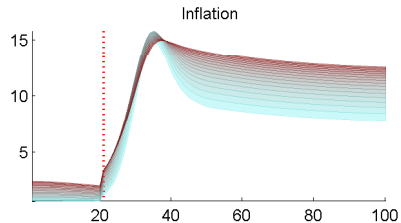
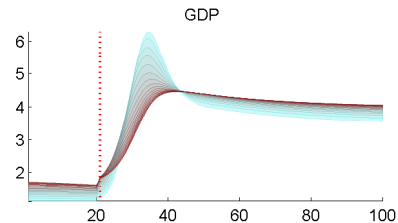
Dormant Shocks

- Consider the following scenario:
 - 1 An initial shock under the Virtuous regime
 - 2 After 5 years policy makers start deviating
- What are the consequences for inflation and the level of uncertainty in the economy?

Dormant Shocks: Expenditure on levels



Dormant Shocks: Expenditure on volatilities

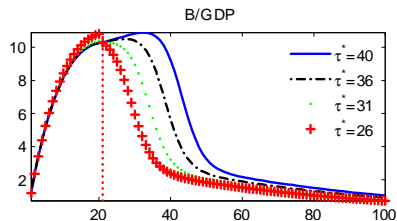
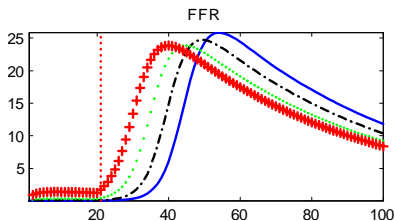
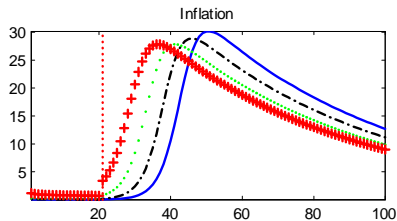
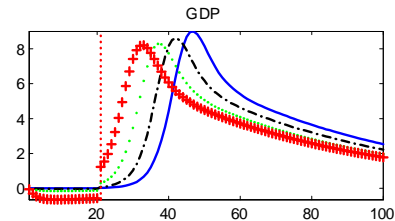


Fiscal Virtue: Conditional priors

- $p_{13} / (p_{12} + p_{13})$ controls the relative probability of a long lasting deviation in the aftermath of a first deviation
- When the ratio is high, agents' beliefs experience a larger jump following the first deviation

| $100p_{13} / (p_{12} + p_{13})$ | p_{22} | τ^* |
|---------------------------------|-------------|-----------|
| .04 | 0.70 | 40 |
| .20 | 0.70 | 36 |
| 1.00 | 0.70 | 31 |
| 5.00 | 0.70 | 26 |

Fiscal Virtue: Conditional priors



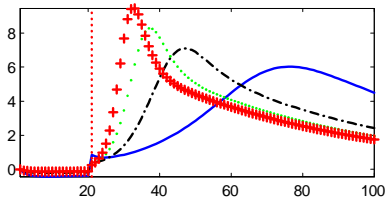
Fiscal Virtue: Conditional priors

- p_{22}/p_{33} controls the relative persistence of a short lasting versus a long lasting deviation
- When the ratio is high, agents are "tolerant"

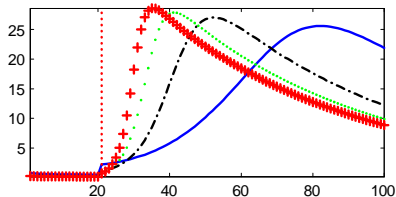
| $100p_{13}/(p_{12} + p_{13})$ | p_{22} | τ^* |
|-------------------------------|------------|-----------|
| 1.00 | .90 | 97 |
| 1.00 | .80 | 48 |
| 1.00 | .70 | 31 |
| 1.00 | .60 | 23 |

Fiscal Virtue: Relative persistences

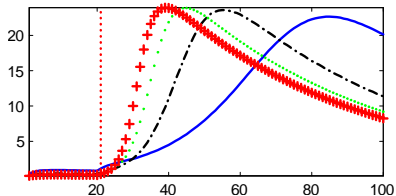
GDP



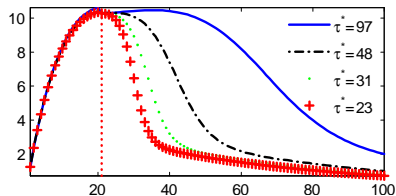
Inflation



FFR



B/GDP



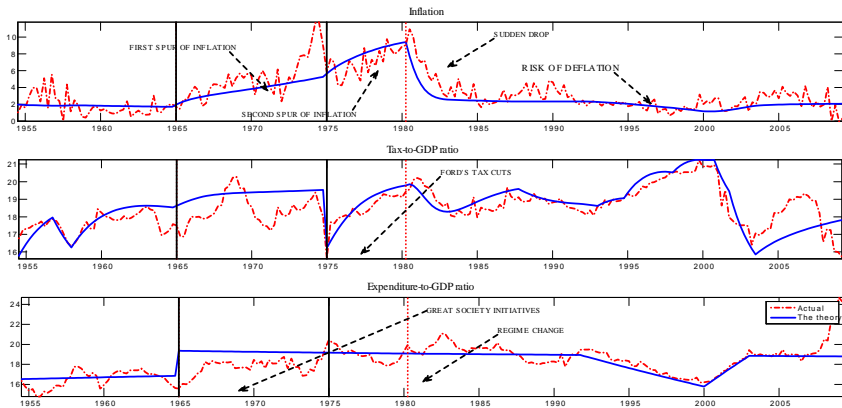
A look at the Past...

- Richer model calibrated using estimates of Bianchi and Ilut (2012) and the following transition matrix:

$$H = \begin{bmatrix} .9200 & .0720 & .0080 \\ .0600 & .9400 & \\ .0050 & & .9950 \end{bmatrix}$$

- It takes a long time for agents to get convinced that they entered a long lasting deviation: p_{22} and p_{33} relatively close
- Even when under the Virtuous regime, agents are concerned about a long lasting deviation: $p_{13} = .8\%$

A look at the Past...

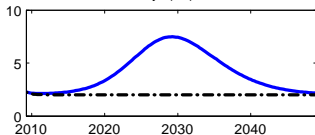
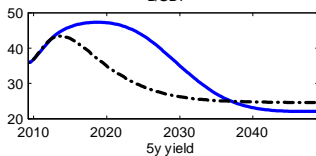
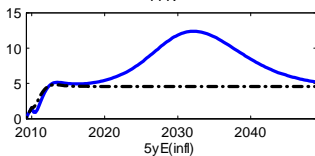
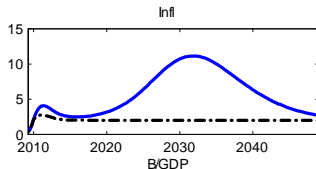
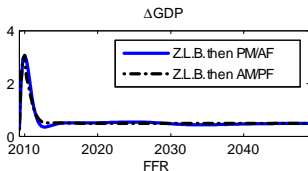


...to understand the Future

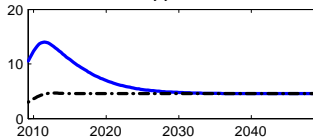
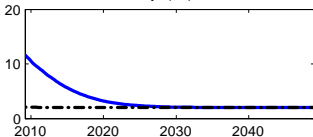
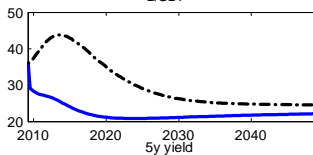
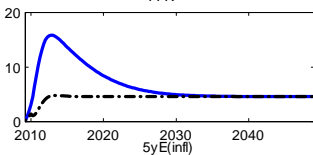
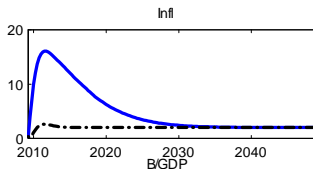
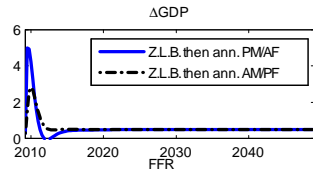
- What is the risk of high inflation for the US?
- Do low long term interest rates imply that agents attach little probability to a spur of high inflation?
- To answer this question we simulate the economy for 40 years
- Whenever agents regard a regime change as possible, we assume that it occurs after 5 years
- We assume:

$$H = \begin{bmatrix} .9750 & .0249 & .0001 \\ .0800 & .9200 & \\ .0100 & & .9900 \end{bmatrix}$$

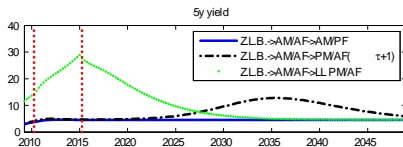
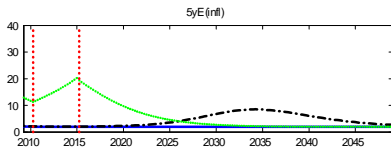
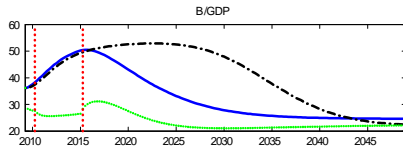
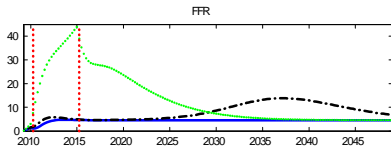
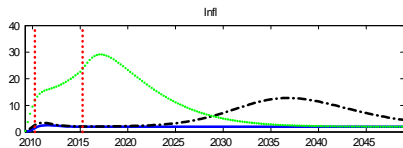
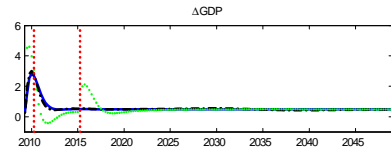
Risk of inflation?



Stimulus?



Contradictory Announcements



Fiscal-Monetary Policy Coordination

- 1 The model can
 - replicate heterogeneity **over time and across countries**
 - generate **persistent and accelerating** increases in inflation
- 2 The strict distinction between non-Ricardian and Ricardian regimes typical of the Fiscal Theory of Price Level breaks down
- 3 When calibrated for US data:
 - The model can explain the run-up in inflation of the '70s with only two shocks and the risk of deflation in the early 2000s
 - Past Fiscal Virtue can hide the true risk of inflation
 - Contradictory statements can conduct to undesirable outcomes

Monetary/Fiscal Policy Mix [▶ Back](#)

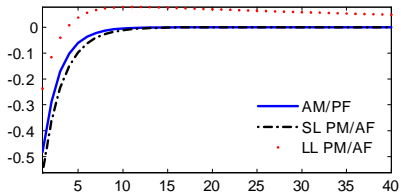
Following Leeper (1991) we can distinguish four cases:

| | Active Fiscal (AF) | Passive Fiscal (PF) |
|-----------------------|--------------------|---------------------|
| Active Monetary (AM) | No Solution | Determinacy |
| Passive Monetary (PM) | Determinacy | Indeterminacy |

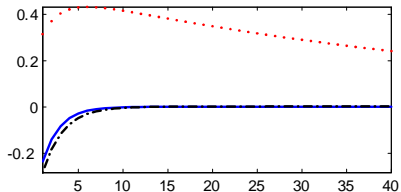
- Active Monetary Policy: Taylor principle is satisfied
 $(\psi_{\pi, \bar{\zeta}_t} > 1)$
- Passive Fiscal Policy: Taxes react strongly to debt
 $(\delta_{b, \bar{\zeta}_t}^{sp} > \beta^{-1} - 1 \rightarrow \beta^{-1} - \delta_{b, \bar{\zeta}_t} < 1)$
- We focus on the two determinacy areas
 - Active Monetary/Passive Fiscal: Fiscal policy is Ricardian
 - Passive Monetary/Active Fiscal: Fiscal policy is non-Ricardian

Impulse responses: Monetary policy shock ▶ Back

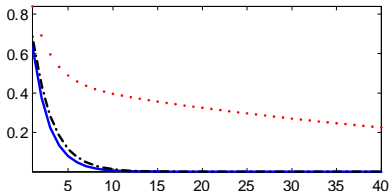
GDP



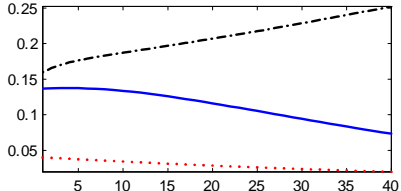
Inflation



FFR



B/GDP



- After the first deviation $\tau = 1$:

$$\text{prob} \{s_t = 2 | \mathcal{F}_t\} = \frac{p_{12}}{p_{12} + p_{13}}$$

- This represents a **lower** bound for agents' pessimism:

$$\text{prob} \{s_{t+1} \neq 1 | \mathcal{F}_t, \tau = 1\} = \frac{p_{12}}{p_{12} + p_{13}} p_{22} + \frac{p_{13}}{p_{12} + p_{13}} p_{33}$$

- After $\tau \geq 1$ consecutive deviations:

$$\text{prob} \{s_{t+1} \neq 1 | \mathcal{F}_t\} = \frac{p_{22} (p_{12} / p_{13}) (p_{22} / p_{33})^{\tau-1} + p_{33}}{(p_{12} / p_{13}) (p_{22} / p_{33})^{\tau-1} + 1} \quad (10)$$

- Pessimism has then an **upper** bound:

$$\lim_{\tau \rightarrow \infty} \text{prob} \{s_{t+1} \neq 1 | \mathcal{F}_t\} = p_{33} \quad (11)$$

Impulse responses: Monetary Policy shock ▶ Back

