

# Inefficient employment decisions, entry costs, and the cost of fluctuations

Wouter J. Den Haan (University of Amsterdam & CEPR) and  
Petr Sedlacek (University of Amsterdam)

May 26, 2010

# Our twist

Fluctuations have negative *level* effects

Theory applies to

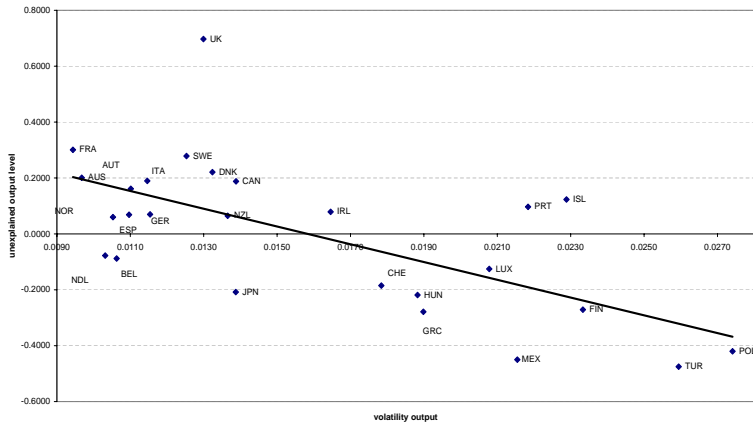
- business cycle fluctuations

- sectoral fluctuations

- regional fluctuations

- etc

Relationship level GDP &amp; volatility



# Key ingredients of theory

- ❶ Decision to operate "project" is not efficient
  - ❷ Entry costs
  - ❸ Heterogeneity
- Not high risk aversion (in fact, agents are risk neutral)

# Quantitative assessment

Quantitative assessment is tough

- Requires info about projects that don't exist in existing world
- Construct measure to decompose GDP fluctuations into
  - extensive component
  - intensive component

# Model

- a continuum of workers/projects
- characterized by
  - *permanent* idiosyncratic productivity,  $\phi_p(i)$
  - *permanent* idiosyncratic entry cost,  $\phi_c(i)$
- workers of type  $i$  can only work in project  $i$

# Two decisions

- decision whether to create a project
- decision whether to continue operating

# Modelling production

Joint revenues equal to  $\Phi_{p,t}\phi_p(i)$

- no business cycles:
  - $\Phi_{p,t} = 1$  for all  $t$
- business cycles:
  - $\Phi_{p,t}$  stochastic with  $E[\Phi_{p,t}] = 1$



# Modelling aggregate shocks

- $\Phi_p \in \{\Phi_{\text{high}}, \Phi_{\text{low}}\}$
- probability  $\left\{ \Phi'_p = \Phi_p \right\} = \pi$

# Notation

- suppress  $(i)$  in  $\phi_c(i)$  and  $\phi_p(i)$
- ! no other parameters depend on  $i$

# Entry decision

Entry if

$$\phi_c \leq \mathbb{E}_t \sum_{j=0}^{\infty} (\beta\rho)^j \prod_{\tilde{j}=0}^j (\tilde{\rho}_{t+\tilde{j}}) (\phi_p \Phi_{p,t+j} - \mu)$$

where

$\rho$  exogenous destruction project  $0 < \rho < 1$   
 $\tilde{\rho}_t$  destruction due to inefficiencies  $\tilde{\rho}_t \in \{0, 1\}$

$$\prod_{\tilde{j}=0}^j (\tilde{\rho}_{t+\tilde{j}}) = \begin{cases} 1 & \text{if } \tilde{\rho}_t = \tilde{\rho}_{t+1} = \dots = \tilde{\rho}_{t+j} = 1 \\ 0 & \text{o.w.} \end{cases}$$

# Friction I - simple & ad hoc

$\phi_p \Phi_{p,t} < \chi$  relationship is not sustainable

- Regulation requires minimum efficiency level

## Friction II - elegant & still simple

- contractual fragility of Ramey and Watson (1997)

$$\begin{aligned} \phi_p \Phi_{p,t} + \text{value continuing relationship} < \\ \chi + \text{value continuing outside relationship} \end{aligned}$$

- Reduces to

$$\phi_p \Phi_{p,t} < \chi$$

if

- entrepreneur can simply rehire new worker after cheating
- matching probability for worker equal to 1

## Friction III - more general

$$\phi_p \Phi_{p,t} < \chi$$



cut-off value does not depend on  
other state variable  $\phi_c$

- Appendix: financial friction:
  - cut-off value could depend on  $\phi_c$
  - affects calibration, not the mechanism

# Efficient and inefficient discontinuation

$\phi_p \Phi_{p,t} < \mu$       efficient to separate

$\mu < \phi_p \Phi_{p,t} < \chi$       separation leads to loss of value

# Bottom line about inefficient separations

 $\Phi_p \uparrow$  $\implies$ 

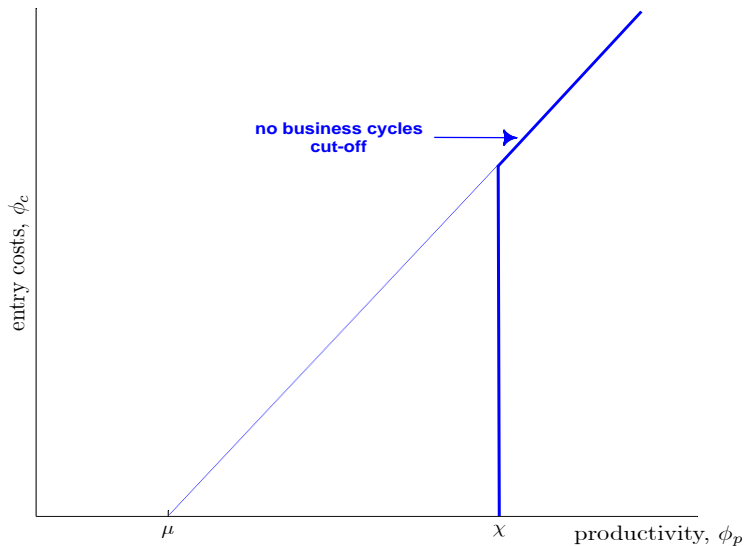
# of inefficient operating decisions  $\downarrow$

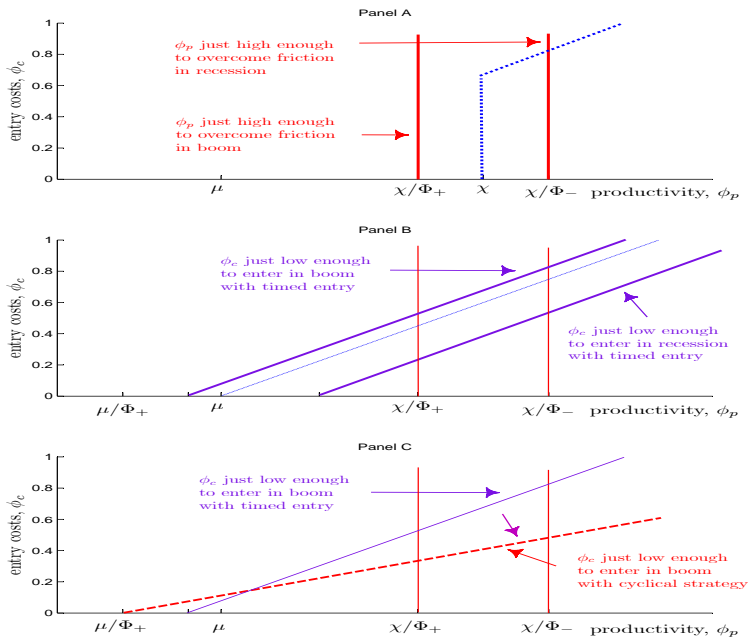


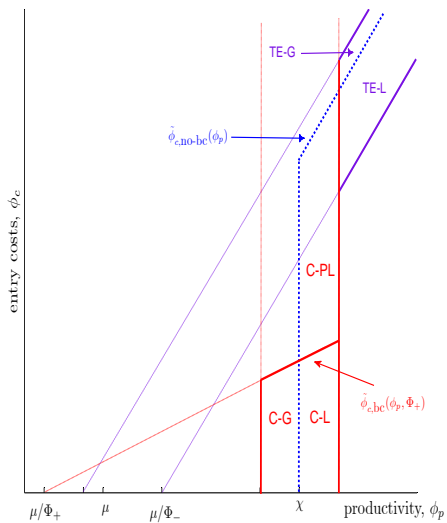
# Social planner & competitive equilibrium

- Social planner does not face the friction  $\phi_p \Phi_{p,t} \geq \chi$

## Competitive equilibrium: No business cycles







# Two types of losses

- **C-PL: permanent loss**
- **Cyclical jobs**
  - C-G: produce more during boom
  - C-L: produce less during recession

# Role of non-zero entry costs

- Business cycles are costly because

expected duration match  $\downarrow \implies$  less entry

- $\phi_c = 0 \implies$  less production during recessions is offset by more production during booms

# Role of inefficiency

Because

$$\mu < \chi$$

there are positive NPV projects that are not created

# Full model

- Production requires entrepreneur and worker
- Entrepreneur:
  - pays 100% posting costs
  - only receives  $\omega_e$  of surplus
  - $\implies$  inefficient entry



# Comparison

- Universe 1: Without business cycles
- Universe 2: With business cycles

# Result

- Timed-entry areas can be ignored
  - these areas depend on timing advantage of business cycles
  - quantitatively very tiny

# Welfare calculations (sloppy notation)

**Without business cycles:**

$$\begin{aligned} & \text{mass (C-PERM-Loss)} \quad \times \quad [NPV - \phi_c] \\ + & \text{mass (C-TEMP-Loss)} \quad \times \quad [NPV - \phi_c] \\ + & \text{mass (C-TEMP-Gain)} \quad \times \quad \left[ \frac{\mu\phi_p}{1-\beta} \right] \end{aligned}$$

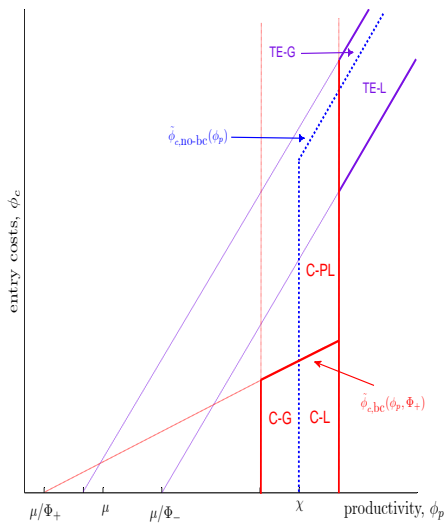
# Welfare calculations (sloppy notation)

With business cycles:

$$\begin{aligned}
 & \text{mass (C-PERM-Loss)} \times \left[ \frac{\mu\phi_p}{1-\beta} \right] \\
 + & \text{mass (C-TEMP-Loss)} \times \left( \begin{array}{c} \frac{1}{2} \text{ } NPV_{\text{boom}} - \phi_c \\ + \frac{1}{2} \text{ } NPV_{\text{recession}} - \phi_c \end{array} \right) \\
 + & \text{mass (C-TEMP-Gain)} \times \left( \begin{array}{c} \frac{1}{2} \text{ } NPV_{\text{boom}} - \phi_c \\ + \frac{1}{2} \text{ } NPV_{\text{recession}} - \phi_c \end{array} \right)
 \end{aligned}$$

# Welfare loss is a tedious straightforward function of

- ➊ Output produced by C-L & C-G projects during a boom
  - we need *extensive* margin of GDP fluctuations
- ➋ Mass of C-PL relative to C-L
  - (permanent loss to cyclical loss projects)
- ➌ Structural parameters



# Extensive measure of GDP

$$\begin{aligned} & GDP_{\text{boom}} - GDP_{\text{recession}} \\ & \approx \\ & \frac{\Phi_{p,\text{high}} - \Phi_{p,\text{low}}}{\Phi_{p,\text{low}}} GDP_{\text{recession}} \\ & + \\ & \text{mass of cyclical jobs} \times \phi_p \Phi_{p,\text{high}} \end{aligned}$$

# Extensive measure of GDP

$$\begin{aligned}
 & \frac{GDP_{\text{boom}} - GDP_{\text{recession}}}{GDP_{\text{recession}}} \\
 & \approx \frac{\Phi_{p,\text{high}} - \Phi_{p,\text{low}}}{\Phi_{p,\text{low}}} + \frac{\text{mass of cyclical jobs} \times \phi_p \Phi_{p,\text{high}}}{GDP_{\text{recession}}} \\
 & = \frac{\Phi_{p,\text{high}} - \Phi_{p,\text{low}}}{\Phi_{p,\text{low}}} + \Lambda
 \end{aligned}$$



# Extensive margin of GDP fluctuations

- ❶ Extensive margin of employment: Standard deviation employment (persons)  $\approx 2.2\% \implies$

$$\frac{E_{\text{boom}} - E_{\text{recession}}}{E_{\text{recession}}} = 4.4\%$$

- ❷ Suppose value added cyclical workers  
=40% of value added non-cyclical workers
- ❸ 1 & 2: Cyclical workers generate

$$(1.76 \times \Phi_{p,\text{high}} / \Phi_{p,\text{low}}) \% \text{ of } GDP_{\text{recession}}$$

# Word of caution

- Cyclical jobs do not have to be the least productive ones
- High-productivity could have high  $\chi$  (e.g. big financing friction)
- Therefore, a direct measure is desirable

# Extensive margin of GDP fluctuations

- Use wage as measure of value added
  - IAB: monthly panel from German social security and unemployment records
  - covers 80% of German labor force
- Non-cyclical worker:
  - employed 24 months ago
  - during this period less than 30 days unemployed
- Cyclical worker: the other workers

# Extensive margin of GDP fluctuations

- $n$ : the *sum* of producing cyclical workers and new entrants
  - we only observe sum
- $N$ : other workers (constant in our framework)

# Extensive margin of GDP fluctuations

$$Y_- = n_- y_- + N \tilde{y}_-$$

$$Y_+ = n_+ y_+ + N \tilde{y}_+$$

$$\begin{aligned} \frac{Y_+ - Y_-}{Y_-} &= \frac{n_+ y_+ - n_- y_-}{Y_-} + \frac{(\tilde{y}_+ - \tilde{y}_-) N}{Y_-} \\ &= \frac{[n_- + (n_+ - n_-)] y_+ - n_- y_-}{Y_-} + \frac{(\tilde{y}_+ - \tilde{y}_-) N}{Y_-} \\ &= \frac{(n_+ - n_-) y_+}{Y_-} + \frac{(y_+ - y_-) n_- + (\tilde{y}_+ - \tilde{y}_-) N}{Y_-} \end{aligned}$$

# Extensive margin of GDP fluctuations

$$\frac{Y_+ - Y_-}{Y_-} = \frac{(n_+ - n_-) y_+}{Y_-} + \frac{(y_+ - y_-) n_- + (\tilde{y}_+ - \tilde{y}_-) N}{Y_-}$$

We measure

$$\frac{(n_+ - n_-) y_+}{Y_-} = \frac{n_+ y_+}{Y_-} - \frac{n_- y_-}{Y_-}$$

by looking how

$$\frac{n_t y_t}{Y_t}$$

increases if the economy gets out of a recession



# Extensive margin of GDP fluctuations

Estimate for  $\Lambda$ :            again  $\approx 2\%$



## Next step:

### **What do we now know?**

- Value generated by temporary loss projects

### **What do we also need to know?**

- Output generated by permanent loss projects

# Permanent loss projects

## What do we know about them?

- ➊ Same output level as temporary loss projects
- ➋ Maximum entry cost (simple function of structural parameters)
- ➌ Minimum entry cost (simple function of structural parameters)

# Permanent loss projects

**What don't we know about them?**

- ❶ How many there are

## Output generated by permanent loss projects

### Assumptions

- 1 lower bound for  $\phi_c = 0$ 
  - higher values will increase cost of fluctuations
- 2 uniform distribution  $\phi_c$  (conditional on  $\phi_p$ )

## Output generated by permanent loss projects

Output generated by permanent loss projects

=

$$\left( \frac{\tilde{\phi}_{c,\text{no-bc}} - \tilde{\phi}_{c,\text{bc}}}{\tilde{\phi}_{c,\text{bc}}} \right) \times \left( \begin{array}{c} \text{Output generated} \\ \text{by temporary loss projects} \end{array} \right)$$

# Parameter assumptions

- Persistence of booms and recessions:
  - $\pi = 0.875$
- Expected duration (if no business cycles)
  - $1/(1 - \rho) = 2, 3, \text{ and } 10$  years
- Value added outside relationship as fraction of  $\phi_p$ :
  - $\mu = 0.2$
- Current-period payoff entrepreneur as fraction of surplus:
  - $\omega_e = 0.1$

# Costs of business cycles

expected duration (years)		
2	3	10
0.56%	0.86%	2.45%

Costs corresponds to *permanent* increase in consumption as percentage of GDP

# Add lower bound to entry costs

$\underline{i}$  equals lower bound on  $\phi_c$

(expressed as average amount of entry costs paid each period when there are no business cycles)



# Costs of business cycles

	expected duration (years)		
	2	3	10
$\underline{i} = 0$	0.56%	0.86%	2.45%
$\underline{i} = 0.5\%$	0.62%	0.98%	3.54%

# Concluding comment

- This is just the cost of *business cycle* fluctuations