

# “Unfunded Liabilities” and Uncertain Fiscal Financing

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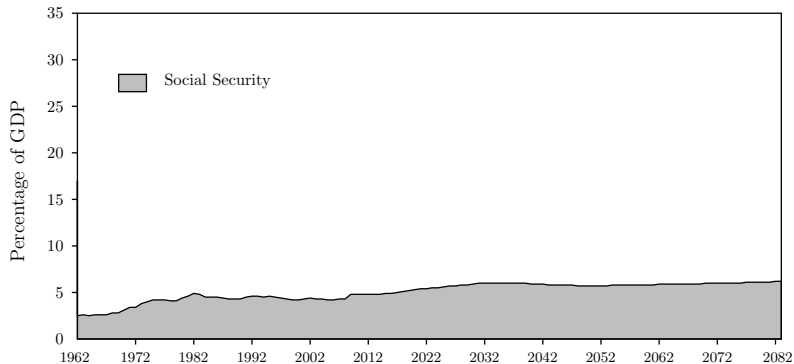
† Indiana University

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# Introduction

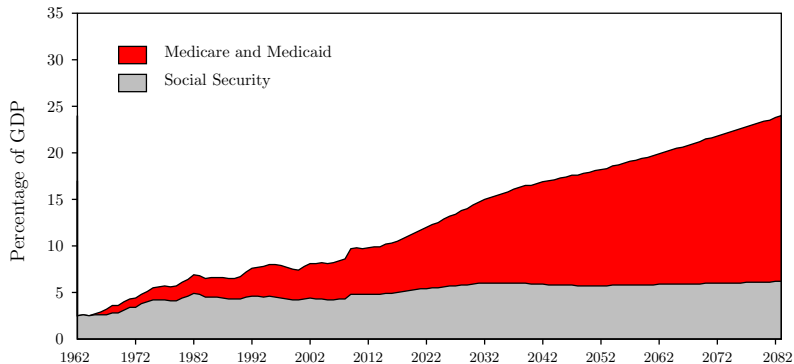
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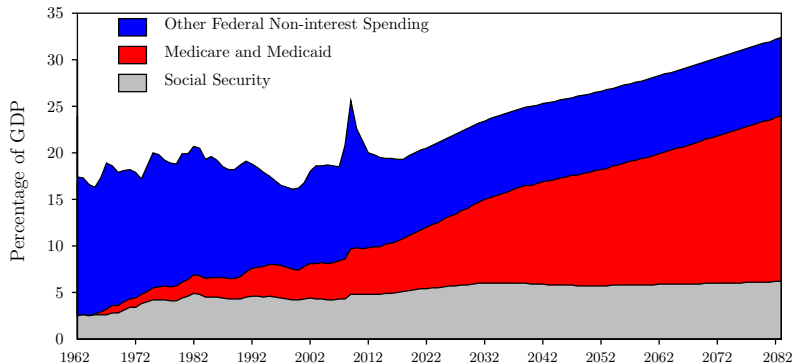
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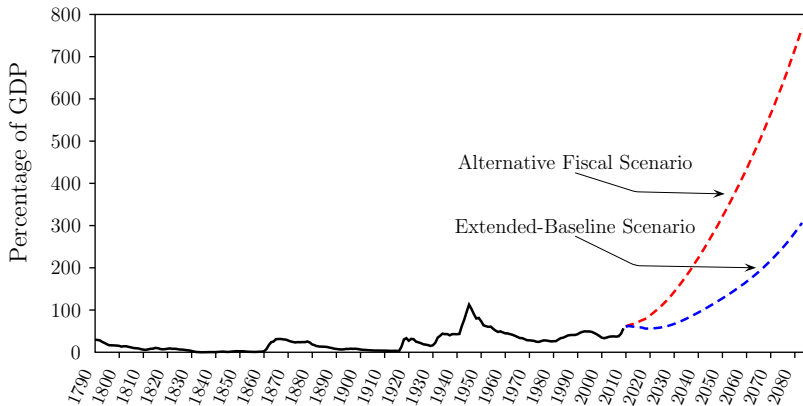
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- ▶ **Unfunded liabilities** is not an economically meaningful term—inconsistent with equilibrium
  - ▶ The government will renege on promised transfers (i.e. “liabilities” do not exist)
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# Rolling Spending Commitments into Debt



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⇒ future policy will change...**how and when?**

# Introduction

- ▶ Nearly every advanced economy faces this problem

# What We Do

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  5. Debt default  $\Rightarrow$  Are U.S. Treasuries risk-free assets?

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We model a *combination* of 1–3, emphasizing uncertainty about *which* policies adjust and *when* policies adjust.

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- ▶ Allow for switching among policy solutions
- ▶ Model fiscal limit as random variable =  $f(\text{fiscal variables})$
- ▶ Focus on expectational effects in otherwise standard macroeconomic DSGE model

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- ▶ Transfers grow at rate  $\mu$  financed by lump-sum taxes and debt

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- ▶ Government's Budget Constraint:

$$\frac{B_t}{P_t} + \tau_t = z_t + \frac{R_{t-1}B_{t-1}}{P_t}$$

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At time  $T$  economy reaches fiscal limit

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	Regime 1 $t = 0, 1, \dots, T - 1$	
Monetary Policy	$R_t^{-1} = R^{*-1} + \alpha \left( \frac{P_{t-1}}{P_t} - \frac{1}{\pi^*} \right)$	
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Fiscal limit may be *economic* (peak of Laffer curve) or *political* (intolerance of taxation)

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$$E_{t-1} \left( \frac{B_t}{P_t} - b^* \right) = E_{t-1}(z_t - z^*) + (\beta^{-1} - \gamma) \left( \frac{B_{t-1}}{P_{t-1}} - b^* \right)$$

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$\alpha/\beta > 1, \beta^{-1} - \gamma < 1 \Rightarrow$  Equilibrium  $\pi_t = \pi^*$

A Standard Monetary Equilibrium

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$\alpha = 0, \gamma = 0 \Rightarrow$  Actual Inflation

$$P_t = \frac{R_{t-1} B_{t-1}}{\left( \frac{1}{1 - \beta} \right) \tau^* - E_t \sum_{j=0}^{\infty} \beta^j z_{t+j}}$$

A Standard Fiscal Equilibrium

# Fiscal Limit: Reneging

	$t = 0, 1, \dots, T - 1$	$t = T, T + 1, \dots$
Monetary Policy	$R_t^{-1} = R^{*-1} + \alpha \left( \frac{P_{t-1}}{P_t} - \frac{1}{\pi^*} \right)$	same
Tax Policy	$\tau_t = \tau^* + \gamma \left( \frac{B_{t-1}}{P_{t-1}} - b^* \right)$	$\tau_t = \tau^{\max}$
Transfer Policy	$z_t$	$\lambda_t z_t$

$$E_{t-1}[B_t/P_t] + \tau^{\max} = E_{t-1}\lambda_t z_t + (\beta^{-1} - \gamma)(B_{t-1}/P_{t-1})$$

$$\pi_t = \pi^*$$

A Standard Monetary Equilibrium

# Fiscal Limit: No Reneging

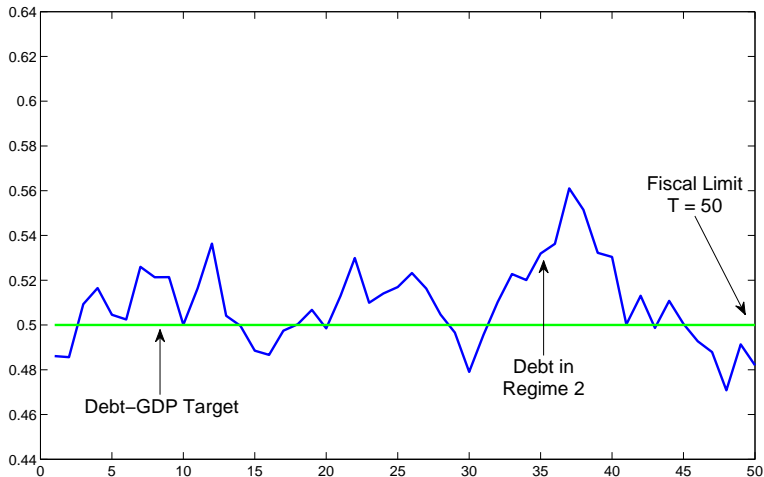
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Transfer Policy	$z_t$	same

$$E_t \left( \frac{P_t}{P_{t+1}} - \frac{1}{\pi^*} \right) = \frac{\alpha}{\beta} \left( \frac{P_{t-1}}{P_t} - \frac{1}{\pi^*} \right), \quad \frac{\alpha}{\beta} > 1$$

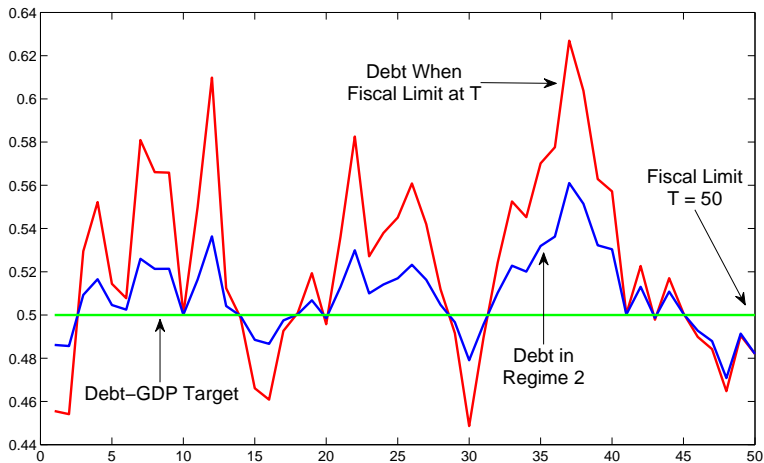
$$P_t = f(z_t; \gamma, \mu, \beta, \pi^*)$$

A New Fiscal Equilibrium Before the Limit

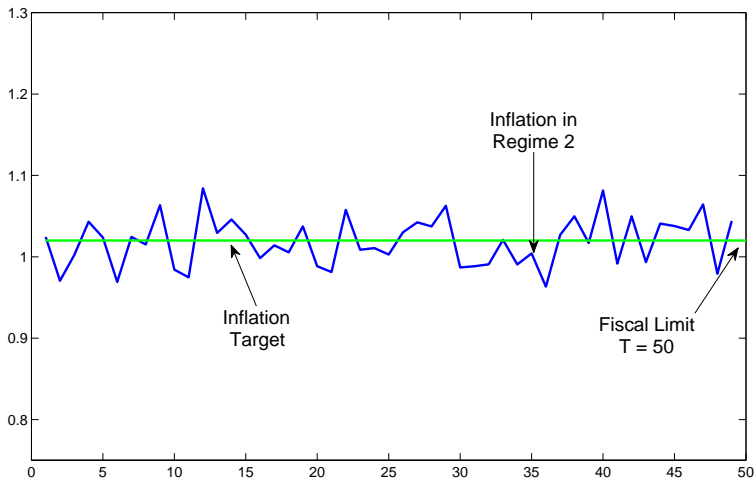
# Analytic Intuition: Debt



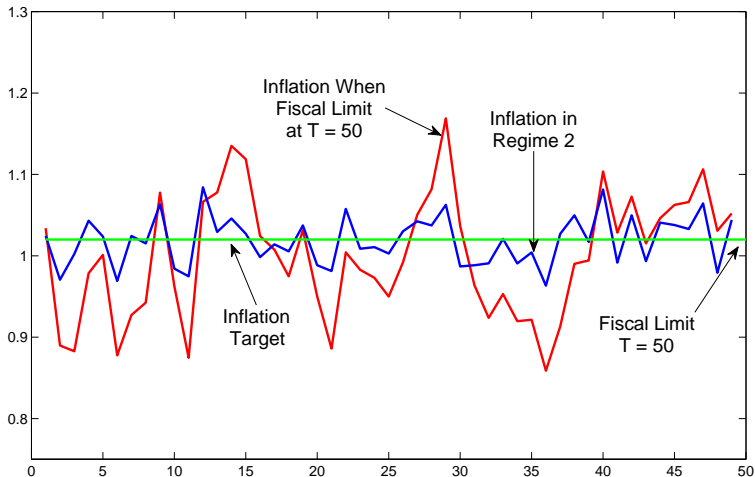
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# Analytic Intuition: Inflation

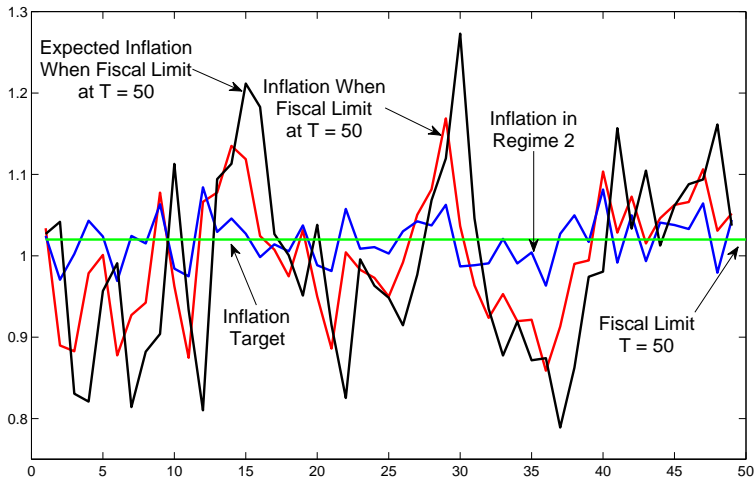


# Analytic Intuition: Inflation





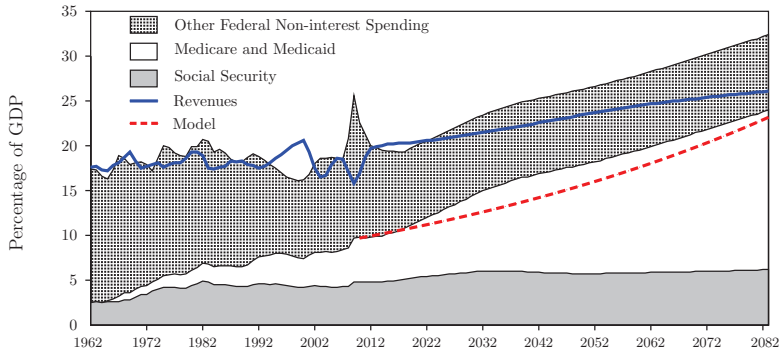
# Analytic Intuition: Expected Inflation



# Fiscal Limit: Implications

- ▶ Expectations of post-limit policies determine *pre*-limit equilibrium
- ▶ Inflation and debt *not* anchored on targets
- ▶ Expectations—and equilibrium—time varying as approach limit
- ▶ Pre-limit equilibrium converges to post-limit equilibrium

# Promised Transfers in a DSGE Model



# Full-Blown Model

- ▶ Standard DSGE model: capital accumulation, sticky prices, distorting taxation
- ▶ Government announces path of *promised* transfers
- ▶ Government debt and taxes grow until the economy hits **fiscal limit**
- ▶ Specify a set of policies that stabilize debt after fiscal limit
- ▶ Multiple layers of policy uncertainty

# Households and Firms

- ▶ Household utility depends on consumption, leisure and real balances
- ▶ Household's budget constraint is

$$C_t + K_t + \frac{B_t}{P_t} + \frac{M_t}{P_t} \leq (1 - \tau_t) \left( \frac{W_t}{P_t} N_t + R_t^k K_{t-1} \right) \\ + (1 - \delta) K_{t-1} + \frac{R_{t-1} B_{t-1}}{P_t} + \frac{M_{t-1}}{P_t} + \lambda_t z_t + \frac{D_t}{P_t}$$

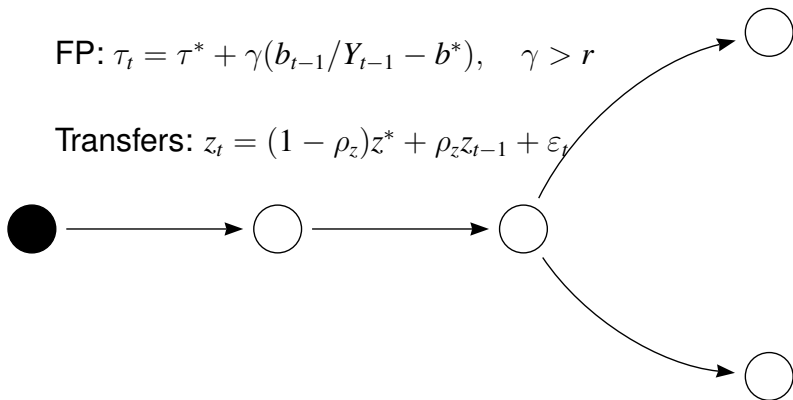
- ▶ Firms set prices as a markup over marginal costs (Rotemberg costly adjustment)

# Initial Period: Stationary Transfers

$$\text{MP: } R_t = R^* + \alpha(\pi_t - \pi^*), \quad \alpha > 1/\beta$$

$$\text{FP: } \tau_t = \tau^* + \gamma(b_{t-1}/Y_{t-1} - b^*), \quad \gamma > r$$

$$\text{Transfers: } z_t = (1 - \rho_z)z^* + \rho_z z_{t-1} + \varepsilon_t$$

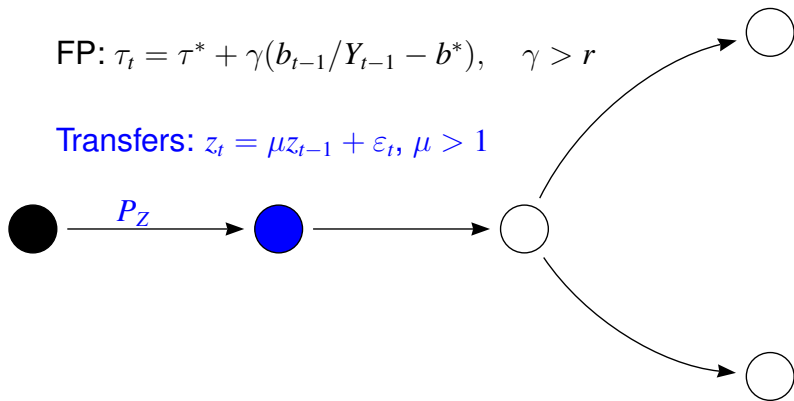


# Non-Stationary *Promised* Transfers

$$\text{MP: } R_t = R^* + \alpha(\pi_t - \pi^*), \quad \alpha > 1/\beta$$

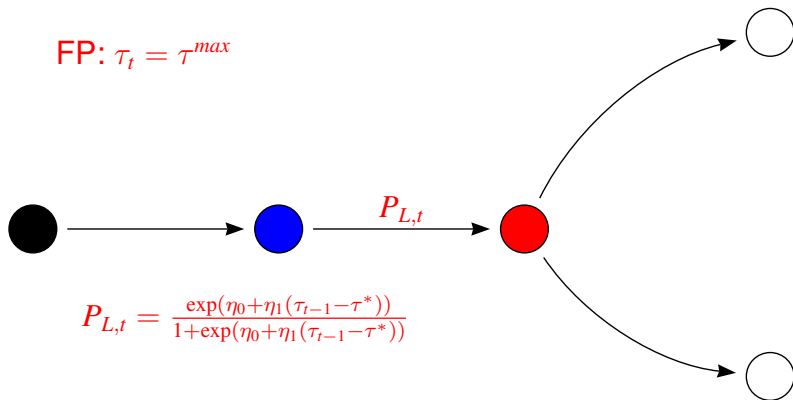
$$\text{FP: } \tau_t = \tau^* + \gamma(b_{t-1}/Y_{t-1} - b^*), \quad \gamma > r$$

$$\text{Transfers: } z_t = \mu z_{t-1} + \varepsilon_t, \quad \mu > 1$$



# Fiscal Limit

FP:  $\tau_t = \tau^{max}$



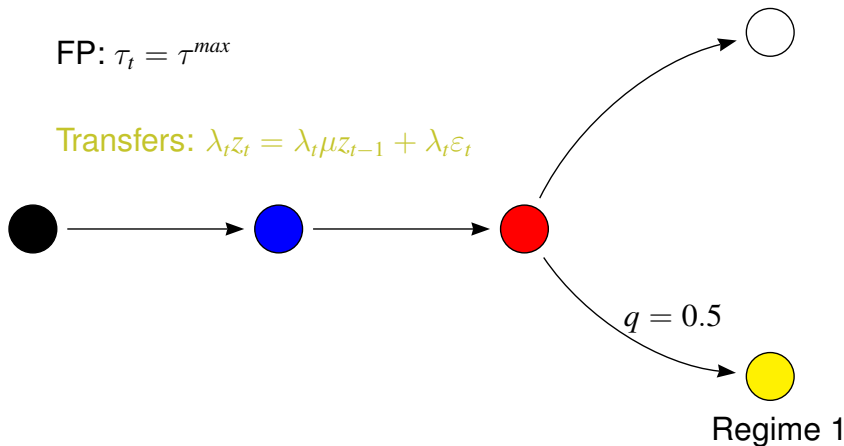


# Fiscal Limit: Regime 1 AM/AF/PT

$$\text{MP: } R_t = R^* + \alpha(\pi_t - \pi^*), \quad \alpha > 1/\beta$$

$$\text{FP: } \tau_t = \tau^{\max}$$

$$\text{Transfers: } \lambda_t z_t = \lambda_t \mu z_{t-1} + \lambda_t \varepsilon_t$$

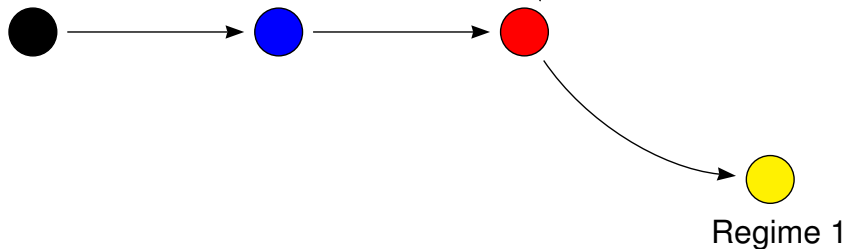


# Fiscal Limit: Regime 2 PM/AF/AT

MP:  $R_t = R^*$

FP:  $\tau_t = \tau^{max}$

Transfers:  $z_t = \mu z_{t-1} + \varepsilon_t$

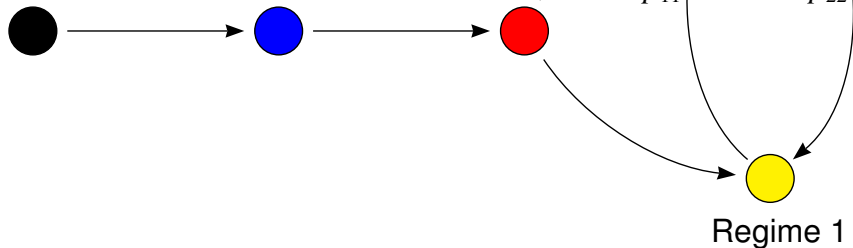


# Fiscal Limit: Switch Between Regimes

$$\text{MP: } R_t = \begin{cases} R^* + \alpha(\pi_t - \pi^*), & \alpha > 1/\beta \\ R^* \end{cases}$$

$$\text{FP: } \tau_t = \tau^{\max}$$

$$\text{Transfers: } z_t = \begin{cases} \lambda_t \mu z_{t-1} + \lambda_t \varepsilon_t \\ \mu z_{t-1} + \varepsilon_t \end{cases}$$



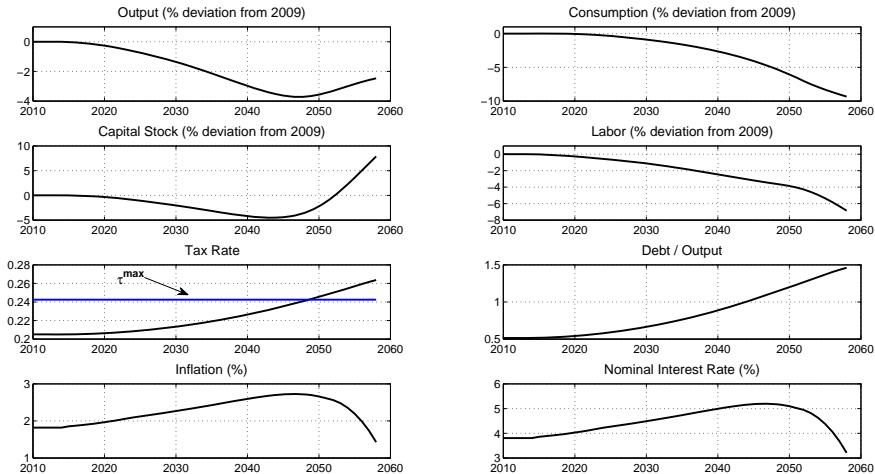
# Counterfactual Experiments

- ▶ Layers of uncertainty call for a probabilistic description of outcomes
- ▶ Report equilibrium transition paths conditional on *particular* realizations of policies
  - ▶ decision rules based on true probability distributions
  - ▶ agents always place probability on alternative future regimes
  - ▶ these are counterfactual exercises that induce policy regime *surprises* every period

# Pre-Limit as Transfers Grow

- ▶ Dominate forces are rising debt and taxes
- ▶ Rising tax rates discourage labor effort and reduce consumption
- ▶ Inflection point in dynamics arises at limit,  $\tau^{max}$
- ▶ Capital falls when  $\tau_t < \tau^{max}$ , then rises when  $\tau_t > \tau^{max}$ , in expectation of a future reduction in tax rates

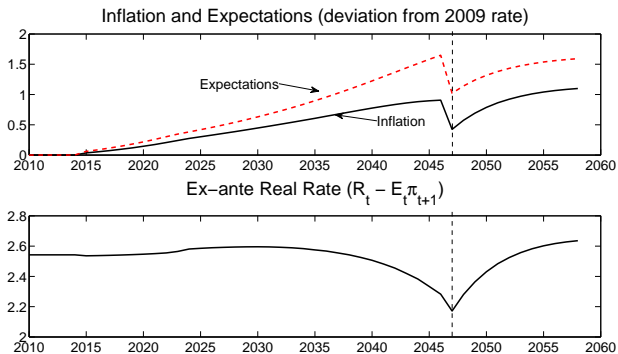
# Pre-Limit as Transfers Grow



Conditional on *not* triggering fiscal limit

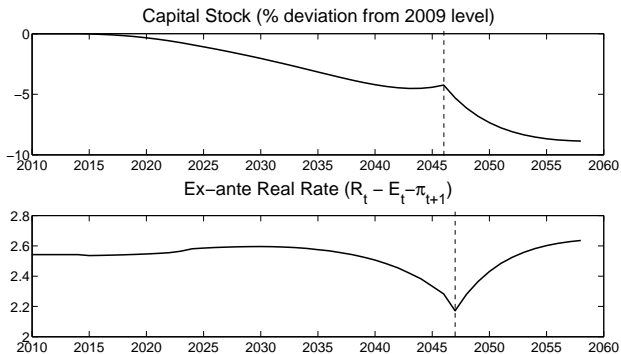
# Post-Limit Reneging ( $\lambda_t < 1$ )

- ▶ Monetary policy is active, but can't stabilize inflation
- ▶ Agents believe can return to regime without reneging, but with passive monetary policy



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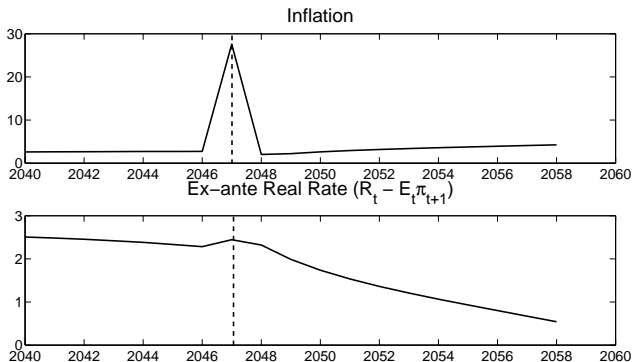
- ▶ Low real rates reduce savings
- ▶ Capital stock declines





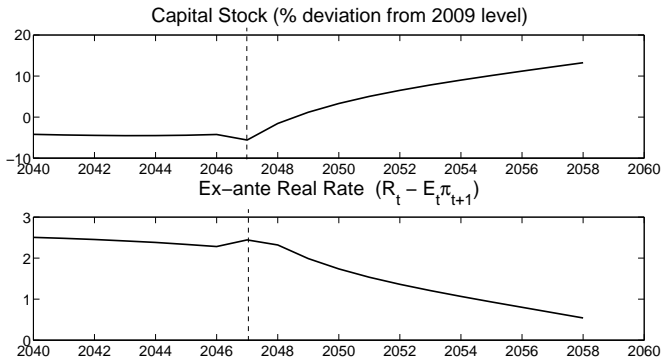
# Post-Limit Passive Monetary Policy

- ▶ Monetary policy is passive and  $\lambda_t = 1$
- ▶ Agents still believe can move to renegeing regime



# Post-Limit Passive Monetary Policy

- ▶ Possibility of renegeing in future increases savings and postpones consumption
- ▶ Drives capital accumulation



# Conclusions

- ▶ Profound uncertainty surrounds the future financing of promised transfers
- ▶ Fiscal pressures will likely impair efforts to achieve any inflation objective
  - ▶ Expected inflation will rise faster than inflation if households believe the economy may hit the fiscal limit
- ▶ In the presence of a fiscal limit, effects of the limit kick in even during “normal” times
- ▶ Underscores that to understand an intrinsically “fiscal issue,” must integrate monetary policy